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Transformations for polyhedral process networks

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Transformations for Polyhedral Process Networks

Sjoerd Meijer

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Transformations for Polyhedral Process Networks

Sjoerd Meijer. -

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