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## Evolution strategies for robust optimization

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# **Evolution Strategies for Robust Optimization**

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geboren te Nijmegen  
in 1983

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