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Conformal invariance and microscopic sensitivity in cosmic inflation

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Conformal invariance and microscopic sensitivity in cosmic inflation

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