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On metrics and models for multiplex networks

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The cover shows a depiction of "The Reach" by JK Rofling (<https://www.jkrofling.com/>).

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To Mom, Dad and Giorgia

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