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## Transport coefficients and low energy excitations of a strongly interacting holographic fluid

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# **Transport coefficients and low energy excitations of a strongly interacting holographic fluid**

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geboren te Bangkok (Thailand) in 1990

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The cover shows the private and public transport phenomena of electricity, heat, humans and other pollutants. Incidentally, this photo was taken at Wong-sawang junction (close to the author's house in Bangkok), infamous for its traffic congestion, a few seconds before a waterfall-like fluid (a.k.a. a tropical rain) starts to pour down and almost destroys the author's camera.





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