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## **Magnetic resonance force microscopy for condensed matter**

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# Nomenclature

## Constants

Name	Symbol	Value
Vacuum permeability	$\mu_0$	$4\pi \times 10^{-7} \text{ TmA}^{-1}$
Bohr magneton	$\mu_B$	$9.274 \times 10^{-24} \text{ JT}^{-1}$
Nuclear magneton	$\mu_N$	$5.051 \times 10^{-27} \text{ JT}^{-1}$
Planck's constant	$h$	$6.626 \times 10^{-34} \text{ Js}$
Reduced Planck's constant	$\hbar$	$1.055 \times 10^{-34} \text{ Js}$
Boltzmann constant	$k_B$	$1.381 \times 10^{-23} \text{ JK}^{-1}$

## Experimental parameters

Description	Symbol(s)	Units	Typical value	Page(s)
Friction cantilever	$\gamma$	kg/s	$1.3 \times 10^{-13} \text{ kg/s}$	27
Magnetic field	$B_0$	T	10 – 200 mT	48, 55, 71
Rotating magnetic field	$B_{rf}$	T	1 – 10 $\mu\text{T}$	55
Alternating magnetic field	$B_{rf,a}$	T	1 – 10 $\mu\text{T}$	87
Resonance slice thickness	$d$	m	31 – 90 nm	61, 76
Diameter magnetic particle	$D$	m	3.43 $\mu\text{m}$	27
Resonance frequency cantilever	$f_0, f_1$	Hz	$3.0 \times 10^3 \text{ Hz}$	26, 86, 106
Stiffness cantilever	$k_0$	N/m	$7.0 \times 10^{-5} \text{ N/m}$	26, 106
(Effective) mass cantilever	$m_{eff}$	kg	$2.0 \times 10^{-13} \text{ kg}$	27, 106
magnetic dipole	$m, M$	$\text{Am}^2$	$1.9 \times 10^{-11} \text{ Am}^2$	74, 106
Saturation magnetization	$M_r$	T	1.15 T	27, 106
Intrinsic quality factor cantilever	$Q_0$	1	$3 \times 10^4$	28
Saturation parameter	$s$	1	$> 1$	62, 71, 91
Spin-lattice relaxation time	$T_1$	s	–	13, 44, 78, 102
Spin-spin relaxation time	$T_2$	s	–	44, 74

