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Integer and fractional quantum hall effects in lattice magnets

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Integer and Fractional Quantum Hall effects in Lattice Magnets

J.W.F. Venderbos

Integer and Fractional Quantum Hall effects in Lattice Magnets

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volgens het besluit van het College voor Promoties
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Jörn Willem Friedrich Venderbos
geboren te Kleve, Duitsland, in 1984

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CONTENTS

1	Introduction	1
1.1	Strong correlations and topological states of matter	1
1.2	Strongly correlated electrons and electronic degrees of freedom	12
1.3	This thesis	18
I	Magnetism and the Double-Exchange Model	21
2	Introduction	23
2.1	Interacting electrons and spins	23
2.2	Kondo Lattice and Double Exchange models	24
3	The honeycomb lattice magnet	29
3.1	Introduction	29
3.2	Model and method	30
3.3	Results	31
3.4	Discussion	35
3.5	Conclusions	36
4	The checkerboard lattice magnet	37
4.1	Introduction	37
4.2	The itinerant checkerboard lattice magnet	38
4.3	Results for half-filling	41
4.4	Results for general filling	52
II	Lattice Fractional Quantum Hall Effects	65
5	Topological bands and orbital degrees of freedom	67
5.1	Introduction	67

5.2	Chiral spin ordering	70
5.3	Orbital degrees of freedom	70
5.4	FQH state induced by residual interactions	75
5.5	Discussion	78
6	t_{2g} triangular lattice systems	81
6.1	Introduction	81
6.2	t_{2g} orbitals on the triangular lattice	83
6.3	Multi-orbital interacting model	84
6.4	Mean field phase diagram	87
6.5	Conclusions	90
7	Triangular lattice Fractional Chern Insulator model	93
7.1	Introduction	93
7.2	Multi-orbital nearly flat band model	97
7.3	Triangular lattice Chern Insulator	103
7.4	Discussion and outlook	108
III	Symmetry and density-wave orders	113
8	Introduction	115
8.1	Overview	119
9	Density-wave states from a symmetry perspective in two dimensions	127
9.1	Electronic lattice symmetries	127
9.2	Interactions and mean-field theory	139
9.3	Condensates of the square lattice	151
9.4	Condensates of hexagonal lattices	171
10	Introduction to triplet states: spin-density waves	227
10.1	General considerations	227
10.2	Triangular lattice triplet states	231
10.3	Honeycomb lattice	239
10.4	Common features of condensates with M -point order	242
11	Summary and conclusions	249
	Appendices	257

A	Details of lattices	257
A.1	Square lattice	258
A.2	Triangular lattice	259
A.3	Honeycomb lattice	260
A.4	Kagome lattice	269
B	Lattice fermions in magnetic fields	273
B.1	Magnetic translation algebra on the lattice	273
B.2	Diagonalization of the Hamiltonian	275
C	Basic elements of group theory	279
C.1	Translational symmetry breaking and “extended” point groups	280
C.2	The point groups C_{4v} and C_{6v}	281
C.3	Symmetry properties with spin	284
	Bibliography	291
	Samenvatting	303
	Curriculum vitae	307
	List of publications	309
	Acknowledgements	311

