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Fermions, criticality and superconductivity

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Citation

She, J. H. (2011, May 3). *Fermions, criticality and superconductivity*. *Casimir PhD Series*. Faculty of Science, Leiden University. Retrieved from <https://hdl.handle.net/1887/17607>

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Note: To cite this publication please use the final published version (if applicable).

Fermions, Criticality and Superconductivity

P R O E F S C H R I F T

TER VERKRIJGING VAN DE GRAAD
VAN DOCTOR AAN DE UNIVERSITEIT LEIDEN, OP GEZAG VAN
RECTOR MAGNIFICUS PROF. MR. P. F. VAN DER HEIJDEN,
VOLGENS BESLUIT VAN HET COLLEGE VOOR PROMOTIES
TE VERDEDIGEN OP DINSDAG 3 MEI 2011
TE KLOKKE 13.45 UUR

DOOR

Jian-Huang She

GEBOREN TE RUDONG, CHINA,
IN 1981

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Casimir PhD Series, Delft-Leiden, 2011-06

ISBN 978-90-8593-095-2

The research described in this thesis was supported by the Netherlands Organisation for Scientific Research (NWO) through a Spinoza Prize grant.

To my family

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