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Galois representations of elliptic curves and abelian entanglements

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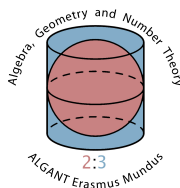
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L'UNIVERSITÉ BORDEAUX I

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par **Julio BRAU AVILA**

POUR OBTENIR LE GRADE DE

DOCTEUR

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Galois representations of elliptic curves and abelian entanglements

Directeurs de recherche : Peter STEVENHAGEN, Karim BELABAS

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