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## Seismology of magnetars

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# Seismology of Magnetars

M.B. van Hoven

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# Seismology of Magnetars

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*This is how the world works. All energy flows  
according to the whims of the Great Magnet.  
What a fool I was to defy him.*

HUNTER S. THOMPSON



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