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A flavour of family symmetries in a family of flavour models

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**A flavour
of family symmetries
in a family
of flavour models**

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Promotiecommissie

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