

# Satellite galaxies in semi-analytic models of galaxy formation with sterile neutrino dark matter

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## ABSTRACT

The sterile neutrino is a viable dark matter candidate that can be produced in the early Universe via non-equilibrium processes, and would therefore possess a highly non-thermal spectrum of primordial velocities. In this paper we analyse the process of structure formation with this class of dark matter particles. To this end we construct primordial dark matter power spectra as a function of the lepton asymmetry,  $L_6$ , that is present in the primordial plasma and leads to resonant sterile neutrino production. We compare these power spectra with those of thermally produced dark matter particles and show that resonantly produced sterile neutrinos are much colder than their thermal relic counterparts. We also demonstrate that the shape of these power spectra is not determined by the free-streaming scale alone. We then use the power spectra as an input for semi-analytic models of galaxy formation in order to predict the number of luminous satellite galaxies in a Milky Way-like halo. By assuming that the mass of the Milky Way halo must be no more than  $2 \times 10^{12} M_\odot$  (the adopted upper bound based on current astronomical observations) we are able to constrain the value of  $L_6$  for  $M_s \leq 8$  keV. We also show that the range of  $L_6$  that is in best agreement with the 3.5 keV line (if produced by decays of 7 keV sterile neutrino) requires that the Milky Way halo has a mass no smaller than  $1.5 \times 10^{12} M_\odot$ . Finally, we compare the power spectra obtained by direct integration of the Boltzmann equations for a non-resonantly produced sterile neutrino with the fitting formula of Viel et al. and find that the latter significantly underestimates the power amplitude on scales relevant to satellite galaxies.

**Key words:** dark matter.

## 1 INTRODUCTION

The identity and properties of dark matter remain among the most pressing questions in physics. For some 30 yr it has been understood that the dark matter particle should be kinematically cold (Davis et al. 1985) and non-baryonic in order to satisfy nucleosynthesis constraints and microwave background temperature anisotropy data (Larson et al. 2011; Planck Collaboration XIII 2015). However the precise identity of the dark matter particle remains elusive.

Many experiments have been devised to look for hypothetical weakly interacting massive particles (WIMPs) predicted by super-

symmetric theories (Ellis et al. 1984), models with extra dimensions (Servant & Tait 2003), and other models with new physics at the TeV scale. Although the CDMS-Si and DAMA direct detection experiments have reported signals consistent with WIMP dark matter (Agnese et al. 2013; Bernabei et al. 2013), other experiments such as XENON100 and LUX find the same parameter space to be ruled out (Aprile et al. 2012; Akerib et al. 2014). Other hints have come from the detection of unexplained astronomical signals which could be provided by annihilating WIMPs, such as  $\gamma$ -ray lines (e.g. Weniger 2012; Daylan et al. 2016),  $\gamma$ -ray excesses (Hooper & Goodenough 2011; Calore, Cholis & Weniger 2015), or cosmic ray positron excesses (Aguilar et al. 2013). However, many of these signals have since been ruled out (Ackermann et al. 2013; Boyarsky, Malyshev & Ruchayskiy 2013), or could potentially be explained

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by other astrophysical sources (e.g. Bartels, Krishnamurthy & Weniger 2016). Thus, after over a decade of increasingly sensitive experiments, a conclusive and consistent signal has not yet emerged.

The weak interaction of GeV–TeV dark matter candidates with ordinary matter requires a new symmetry to stabilize these particles from fast decays. If one does not assume such a symmetry, the dark matter candidate should be *superweakly interacting* and/or light. One such candidate of particular interest is the sterile neutrino (Dodelson & Widrow 1994; Shi & Fuller 1999; Abazajian, Fuller & Tucker 2001a; Abazajian, Fuller & Patel 2001b; Asaka, Blanchet & Shaposhnikov 2005; Asaka & Shaposhnikov 2005; Asaka, Laine & Shaposhnikov 2007), see Boyarsky, Iakubovskiy & Ruchayskiy (2012) for review. The existence of sterile neutrinos is motivated by the phenomenon of neutrino oscillations: the change of neutrino flavours could be due to mixing with these new particles. However, it has been recognized (Asaka et al. 2005; Boyarsky et al. 2006) that sterile neutrino dark matter particles do not contribute significantly to the neutrino oscillations. Therefore, at least three sterile neutrinos are required to explain the neutrino masses and mixing and provide a dark matter candidate. It turns out (Asaka & Shaposhnikov 2005; Canetti, Drewes & Shaposhnikov 2013a; Canetti et al. 2013b) that these same sterile neutrinos can be responsible for the generation of the matter–antimatter asymmetry in the early Universe. This three sterile neutrino model, with their masses below the electroweak scale, explains neutrino oscillations, the mechanism of baryogenesis and the dark matter candidate, and has been named the Neutrino Minimal Standard Model or  $\nu$ MSM (see Boyarsky, Ruchayskiy & Shaposhnikov 2009a, for review).

Sterile neutrino dark matter particles in the  $\nu$ MSM have keV-scale mass and thus have a sufficiently large free-streaming velocity to act as warm dark matter (WDM), see Section 2 below. The free-streaming of WDM particles erases perturbations in the early Universe below the *free-streaming horizon* and therefore suppresses the formation of dark matter haloes that could otherwise contain dwarf and satellite galaxies (see e.g. Weinberg et al. 2013). WDM models may be able therefore to ease tensions between simulated dark matter haloes and satellite galaxies, in both their abundance and structure (Bode, Ostriker & Turok 2001; Polisensky & Ricotti 2011; Lovell et al. 2012; Anderhalden et al. 2013); in this role WDM is an alternative or even a complement to proposed astrophysics-based processes such as reionization (Benson et al. 2002) and supernova feedback (Pontzen & Governato 2012; Zolotov et al. 2012; Governato et al. 2015). The abundance of satellite galaxies in particular is an attractive property to consider (Polisensky & Ricotti 2011; Kennedy et al. 2014; Lovell et al. 2014; Schneider 2015). Kennedy et al. (2014) used a semi-analytic galaxy formation model to constrain the properties of WDM particles. In this study we extend the analysis of Kennedy et al. (2014) to sterile neutrino dark matter in order to obtain constraints on both the mass of the sterile neutrino and an additional particle physics parameter, the lepton asymmetry with which the sterile neutrinos are generated.

Interest in sterile neutrinos has increased recently since multiple reported detections of an X-ray line from the *XMM–Newton*, *Chandra*, and *Suzaku* X-ray observatories at an energy of 3.5 keV in the Galactic Centre, M31, and numerous galaxy clusters (Boyarsky et al. 2014, 2015; Bulbul et al. 2014; Iakubovskiy et al. 2015), which could be generated by the decay of a 7 keV sterile neutrino. This hypothesis has been tested with new, deep observations of the Draco dwarf galaxy, however the results are inconclusive (Jeltema & Profumo 2016; Ruchayskiy et al. 2016). Below we pay special attention to the properties of such 7 keV particles.

This paper is organized as follows. In Section 2 we provide a review of the sterile neutrino model and discuss its influence on the matter power spectrum. The method for calculating the abundance of satellite galaxies is described in Section 3 and the results presented in Section 4. We draw conclusions in Section 5.

## 2 STERILE NEUTRINO DARK MATTER

In this section we provide an outline of how the sterile neutrinos are produced, describe their momentum distribution functions and matter power spectra, and discuss the differences with generic thermal relic WDM.

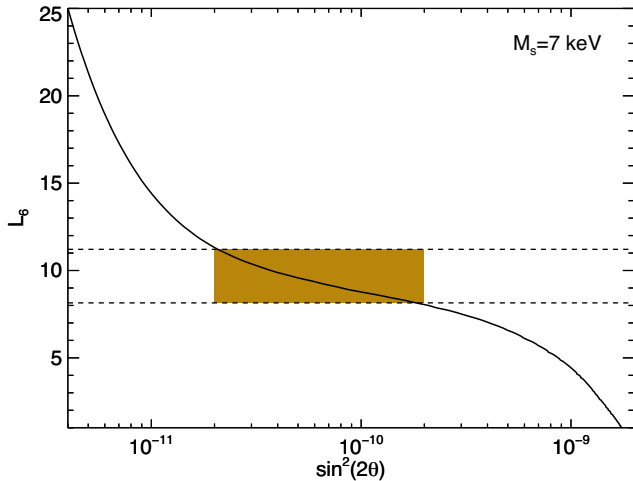
### 2.1 Production mechanisms

Sterile neutrinos were first suggested as a dark matter candidate by Dodelson & Widrow (1994). Their model considered a single sterile neutrino added to the standard model of particle physics. This new particle would be produced through mixing with active neutrinos in the early Universe. Although produced out of equilibrium, its primordial momentum distribution would resemble that of a (rescaled) Fermi–Dirac distribution (Dolgov & Hansen 2002). The production rate peaks at a temperature  $T_{\text{prod}} \sim 150 \text{ MeV} (M_s/1 \text{ keV})^{1/3}$  (Dolgov & Hansen 2002; Asaka et al. 2007) and the average momentum scales as  $\langle p \rangle \sim T_{\text{prod}}$ ; here  $M_s$  denotes the sterile neutrino mass. The particles are therefore produced relativistically in the range of masses up to  $\sim 2 \text{ MeV}$  (i.e. their average momentum,  $\langle p \rangle \gtrsim M_s$ ), and thus the sterile neutrino particle is a WDM candidate.

The WDM nature of these particles, together with the fact that sterile neutrinos decay into X-rays on a time-scale much longer than the age of the Universe (Abazajian et al. 2001a; Dolgov & Hansen 2002), has enabled very strong constraints to be placed on the particle’s properties: low-mass sterile neutrinos would free-stream out of large scale ( $k > 1 h \text{ Mpc}^{-1}$ ) primordial perturbations and prevent galaxies from forming, whilst high-mass sterile neutrinos would be readily detectable in X-rays since the particle lifetime,  $\tau \propto M_s^{-5}$ . The combination of these two constraints ultimately excluded the entire available sterile neutrino mass range of interest, and thus ruled out a purely non-resonantly produced sterile neutrino (Seljak et al. 2006; Viel et al. 2006; Boyarsky et al. 2009c).

However, being produced out of thermal equilibrium, sterile neutrinos are sensitive to the content of primordial plasma. In particular, the production of sterile neutrinos could be enhanced in the presence of a lepton asymmetry, i.e. an overabundance of leptons relative to antileptons (Shi & Fuller 1999). In this case, the lepton asymmetry increases the effective sterile neutrino mixing angle, much in the same way as the Mikheyev–Smirnov–Wolfenstein (MSW) effect (Wolfenstein 1978; Mikheev & Smirnov 1985) changes the mixing angles of active neutrinos passing through a medium. The lepton asymmetry required for this mechanism to work is much greater than the inferred value of the baryon asymmetry of the Universe, and should exist in the primordial plasma *after* the electroweak transition.

A sufficiently large lepton asymmetry appears naturally for a large part of the parameter space of the  $\nu$ MSM model in the temperature range 10–100 GeV (Shaposhnikov 2008; Canetti et al. 2013a,b), being generated by two other, unstable sterile neutrino species at the GeV scale, and leads to the resonant production of dark matter particles (Laine & Shaposhnikov 2008). The resonant enhancement applies to momenta below some threshold, so the dark matter can be cooler than in the non-resonant case and thus no



**Figure 1.**  $L_6$  as a function of the mixing angle,  $\sin^2(2\theta)$ , for the 7 keV sterile neutrino, such that the sterile neutrino abundance is equal to the dark matter abundance. The brown region delineates the mixing angle range inferred for the 3.5 keV line by Boyarsky et al. (2014). Further examples may be found in Boyarsky et al. (2009a); see also Abazajian (2014).

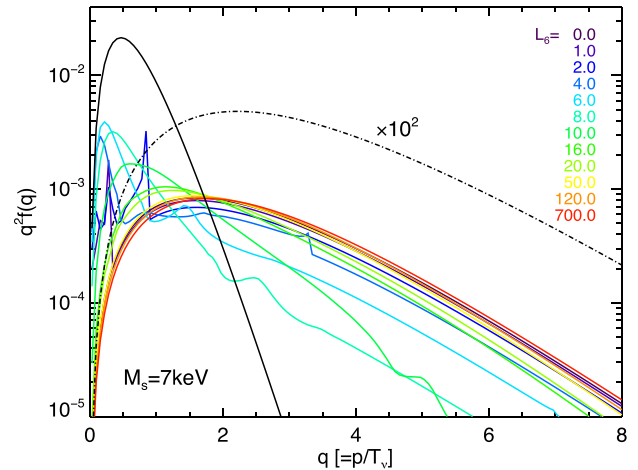
longer in tension with structure formation bounds (Boyarsky et al. 2009b).

The lightest of the three sterile neutrinos in the  $\nu$ MSM is a dark matter candidate whose properties are determined by three parameters: its mass,  $M_s$ ,<sup>1</sup> the mixing angle,  $\theta_1$  – which together with  $M_s$  determines the X-ray decay rate flux,  $F \propto \sin^2(2\theta_1)M_s^5$  (Pal & Wolfenstein 1982; Barger, Phillips & Sarkar 1995) – and the lepton asymmetry, which we denote as  $L_6$ . Here we define  $L_6$  as  $10^6$  times the difference in electron neutrino and anti-electron neutrino abundance divided by the entropy density, i.e.  $L_6 \equiv 10^6 \frac{n_{\nu_e} - n_{\bar{\nu}_e}}{s}$ ; for an alternative parametrization see Abazajian (2014). The requirement that the correct cosmic dark matter density parameter be obtained has the effect that setting the value of two of the parameters determines uniquely the value of the third. For a given mass, as lepton asymmetry increases the mixing angle must decrease. We show the relationship between these two parameters for the 7 keV sterile neutrino in Fig. 1, highlighting the range of  $\theta_1$  – and thus  $L_6$  – that is consistent with the 3.5 keV line. For the remainder of this study we retain  $L_6$  as the free parameter rather than the mixing angle.

## 2.2 Primordial velocities of sterile neutrino dark matter

The lepton asymmetry has an important effect on the shape of the sterile neutrino momentum distribution. It is parametrized in terms of  $L_6$  as defined in the previous subsection;  $L_6 = 0$  thus corresponds to the absence of any lepton asymmetry. As explained in Boyarsky et al. (2009a) the maximal lepton asymmetry attainable in principle within the  $\nu$ MSM is  $L_6^{\max} = 700$  [for comparison the big bang nucleosynthesis (BBN) bound on primordial lepton asymmetry of Serpico & Raffelt (2005) would correspond to  $L_6^{\text{BBN}} \simeq$

<sup>1</sup> In some particle physics studies, this mass is denoted  $M_1$  so as to be distinguished from the two GeV-scale unstable sterile neutrino masses,  $M_2$  and  $M_3$ .



**Figure 2.** Sterile neutrino momentum distributions for different values of  $L_6 = [0, 700]$  as indicated by the legend. Each distribution  $f(q)$  is multiplied by the momentum squared,  $q^2 \times f(q)$ , to reduce the dynamic range. Solid black line – the Fermi–Dirac distribution of a thermal relic with the mass  $M_{\text{th}} = 1.4$  keV (the temperature of this distribution is different from  $T_\nu$ ). Dashed black line – Fermi–Dirac distribution with  $T = T_\nu$ , multiplied by  $10^{-2}$  to fit into the plot. The momenta are plotted for the thermal plasma at a temperature of 1 MeV. The sterile neutrino mass is 7 keV.

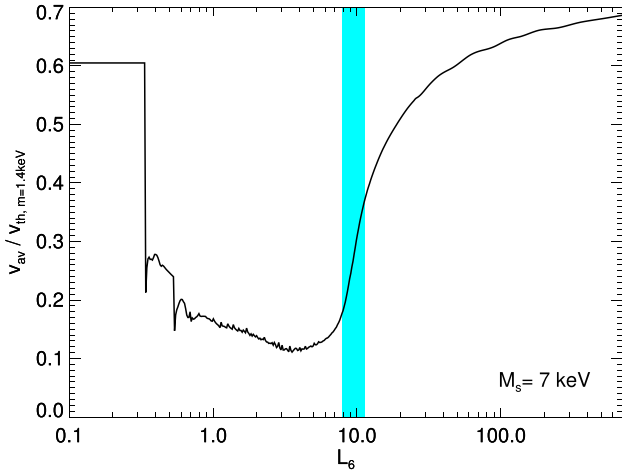
2500] therefore we choose to perform the analysis in the range  $0 \leq L_6 \leq 700$ .<sup>2</sup>

For a given value of  $M_s$  we can therefore vary the value of  $L_6$  and attain a variety of different momentum distributions. As a pertinent example of how the momentum distribution changes for different lepton asymmetry, we generate the  $M_s = 7$  keV sterile neutrino momentum distributions for 12 values of  $L_6$  using the methods and code of Laine & Shaposhnikov (2008) and Ghiglieri & Laine (2015), and plot the results in Fig. 2 (we do not expect the most recent computations Venumadhav et al. 2015 to affect our results).

The behaviour of the momentum distribution is non-monotonic with increasing  $L_6$ . For  $L_6 = 0$  (non-resonant production, NRP) the distribution is well approximated by a rescaled Fermi–Dirac distribution, at least to first order. As  $L_6$  increases, a prominent resonance spike appears at low momentum, along with several additional spikes at higher momenta. The amplitude and position of these resonance peaks increase with lepton asymmetry such that the overall spectrum becomes cooler.<sup>3</sup> Eventually the resonance peak shifts to sufficiently high momentum that the spectrum becomes warmer again, and for  $L_6 \gtrsim 50$  the momentum distribution is very similar to that for non-resonant production. This is because the resonance is enhancing production at all momenta.

<sup>2</sup> The recent work of Canetti et al. (2013a,b) has not revealed any combination of the  $\nu$ MSM parameters that would lead to  $L_6$  in excess of 120. However this is a work in progress and therefore we choose to explore a wider region of the parameters.

<sup>3</sup> The precise shape of the distribution function at low momentum is complicated by the effect of the Pauli exclusion principle. Because of it some low  $q$  sterile neutrinos may be forced to acquire a higher momentum, an effect known as a ‘back reaction’ (Laine & Shaposhnikov 2008). There is still some uncertainty as to which approximations should be used to calculate the contribution of this effect accurately, and this uncertainty translates into a systematic error on the distribution shape. In this study we choose a back-reaction prescription of Laine & Shaposhnikov (2008) that gives the coldest distribution functions for given mass and lepton asymmetry.

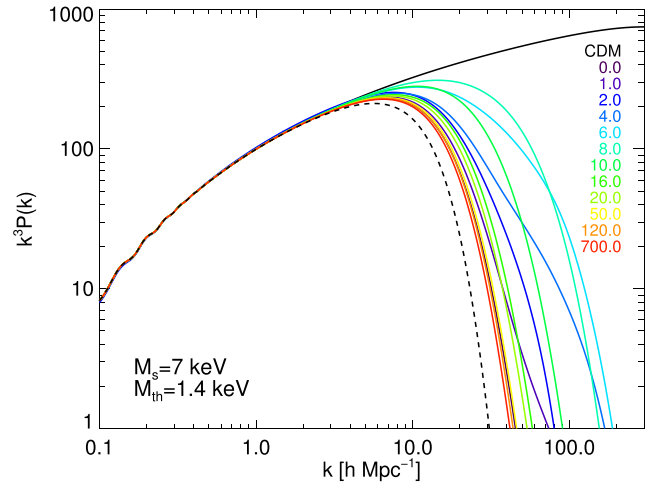


**Figure 3.** The average velocity (a proxy for the free-streaming length), at matter-radiation equality for a series of  $M_s = 7$  keV momentum distributions as a function of lepton asymmetry, normalized to the corresponding average velocity of the thermal relic with  $M_{\text{th}} = 1.4$  keV,  $v_{\text{th}} = 54 \text{ km s}^{-1}$ . The region of  $L_6$  that is consistent with the reported 3.5 keV line (Boyarsky et al. 2014) is given by the cyan region. Small wiggles on the curve correspond to the contributions of sharp resonant peaks in the distribution functions, as seen in Fig. 2.

The shape of these momentum distributions is a key ingredient for calculating the free-streaming velocity, the magnitude of which influences the shape of the matter power spectrum. As a proxy for the free-streaming velocity we calculate the average velocity of the momentum distributions at matter-radiation equality; we denote this average velocity by  $v_{\text{av}}$ . We calculate  $v_{\text{av}}$  for a grid of 500 7 keV momentum distributions, each of which has a value of  $L_6$  in the range [0.1, 700], and plot the results in Fig. 3. We find that for  $L_6 < 0.3$ ,  $v_{\text{av}}$  has a constant value of  $32 \text{ km s}^{-1}$  (which is about 40 per cent lower than the  $v_{\text{av}}$  of Fermi–Dirac distribution with the same mass and  $T = T_\nu$  or, equivalently, of the thermal relic particle with the mass  $M_{\text{th}} = 1.4$  keV). The average velocity then sharply decreases with  $L_6$  as the resonance begins to take effect, and attains a minimum value at  $L_6 \approx 5$  before rising once again to values higher even than that of the non-resonant case. Thus, there exists a ‘sweet spot’ for  $L_6$  for which the spectrum is maximally cool, either side of which the average free-streaming velocity rises rapidly.

### 2.3 Power spectra of sterile neutrino dark matter

The shape of primordial momentum distribution is imprinted in the linear matter power spectrum. We use the distribution functions calculated for Fig. 2 as inputs to a modified version of the Boltzmann solver *CAMB* (Lewis, Challinor & Lasenby 2000) in order to derive the sterile neutrino dimensionless linear matter power spectra –  $\Delta^2(k) = k^3 P(k)$  – at redshift zero; we assume the *Planck* cosmological parameters (quoted in Section 3). We plot the results in Fig. 4. As anticipated from the distribution functions, the wavenumber at which the dimensionless matter power spectrum attains its peak amplitude,  $k_{\text{peak}}$ , increases with  $L_6$  up to some value and then returns to the original, warmer spectrum. These power spectra each have a pronounced cut-off as is the case for fiducial WDM. However, the power spectra close to the turnover have a shallower slope



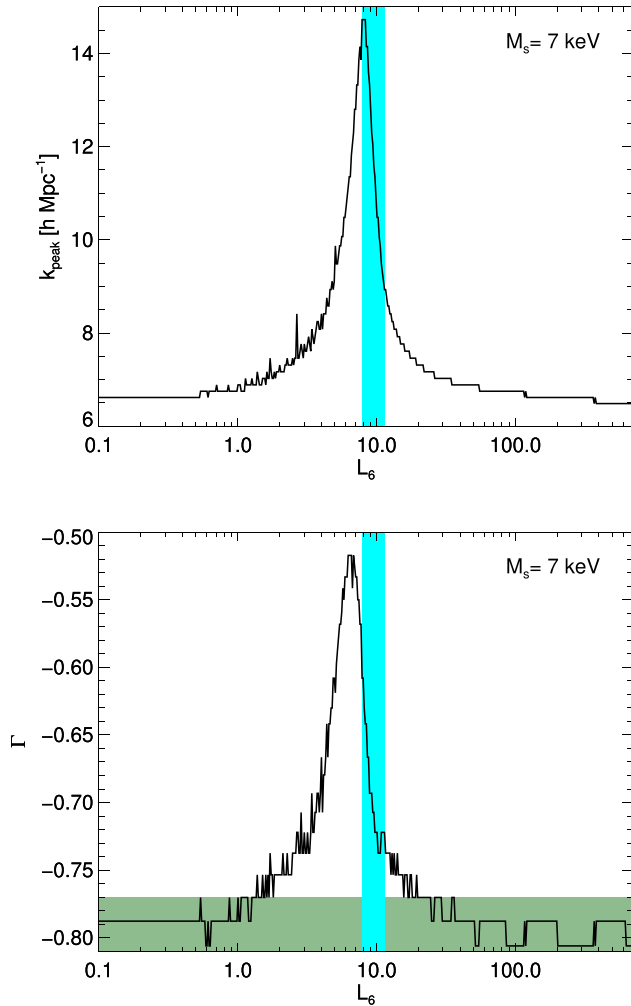
**Figure 4.** Matter power spectra generated from the  $M_s = 7$  keV distribution functions shown in Fig. 2. The CDM power spectrum is shown as a solid black line. The dashed line corresponds to the power spectrum of a thermal relic of mass 1.4 keV, which is the thermal relic counterpart of the NRP 7 keV sterile neutrino, as derived from equations (1) and (2). See the legend for correspondence between colour and lepton asymmetry value.

than for the minimally or maximally resonant sterile neutrino.<sup>4</sup> In order to examine the evolution of the cut-off position and gradient more quantitatively, in Fig. 5 we display both  $k_{\text{peak}}$  and the turnover gradient for a set of 500 7 keV matter power spectra as a function of  $L_6$ ; we define the turnover gradient,  $\Gamma$ , as the logarithmic gradient between  $k_{\text{peak}}$  and  $k_{\text{half-peak}}$ , where the latter is defined as  $\Delta^2(k_{\text{half-peak}} > k_{\text{peak}}) = 0.5 \Delta^2(k_{\text{peak}})$ .

The value of  $k_{\text{peak}}$  increases by over a factor of 2 between the coolest and warmest models, from  $6.6 h \text{ Mpc}^{-1}$  at  $L_6 = 0.1$  to a maximum  $14.7 h \text{ Mpc}^{-1}$  at  $L_6 = 8$ , which is a higher value of the lepton asymmetry than that at which  $v_{\text{av}}$  is minimized. We can therefore conclude that knowledge of the average momentum (and thus free-streaming velocity) is not sufficient to determine the matter power spectrum and that the precise shape of the momentum distribution function therefore plays a key role (see also Maccio et al. 2013 where this has been demonstrated for the cold+warm dark matter models, CWDM). The gradient exhibits similar behaviour: the cut-off is sharp at the largest and smallest values of  $L_6$ , and is comparable to that of the slope of the WDM transfer function developed by Viel et al. (2005, hereafter V05), but becomes much shallower in the middle of the range plotted. The shallowest gradient is attained at  $L_6 \sim 6.3$ , thus at slightly lower  $L_6$  than is the case for  $k_{\text{peak}}$ . We explore the role of these two parameters, plus  $v_{\text{av}}$ , for predicting the Milky Way satellite galaxy abundance in Appendix B.

It is interesting to compare the shapes of sterile neutrino power spectra with the matter power spectra of thermal relic particles. Colombi, Dodelson & Widrow (1996) and Bode et al. (2001) showed that an NRP sterile neutrino matter power spectrum, as derived from Dodelson & Widrow (1994), would have precisely

<sup>4</sup> This shallow slope is similar to that of a cold+warm dark matter mixture (CWDM) for values of  $k$  that are close to the cut-off, and thus CWDM has been used in the past to approximate sterile neutrino matter power spectra for studies of the Lyman  $\alpha$  forest (Boyarsky et al. 2009b,c). However, for high-resolution simulations and Monte Carlo Markov chain methods this approximation is not appropriate as it introduces spurious excess power at small scales.



**Figure 5.** Properties of the  $M_s = 7$  keV matter power spectrum as a function of  $L_6$ . Top:  $k_{\text{peak}}$ ; bottom: logarithmic gradient. The region in  $L_6$  consistent with the 3.5 keV line is shown in cyan. The dark green region marks the range of  $\Gamma$  for V05 thermal relics with the same  $k_{\text{peak}}$  as our 7 keV matter power spectra.

the same shape as a thermally produced particle of some mass. V05 built upon these studies and derived the following relationship between the sterile neutrino and thermal relic masses:

$$M_s = 4.43 \text{ keV} \left( \frac{M_{\text{th}}}{1 \text{ keV}} \right)^{4/3} \left( \frac{0.7^2 \times 0.25}{h^2 \Omega_{\text{DM}}} \right)^{1/3}, \quad (1)$$

where  $M_{\text{th}}$  is the thermal relic mass,  $h$  the Hubble parameter, and  $\Omega_{\text{DM}}$  the dark matter density parameter. Thus, a 7 keV NRP sterile neutrino would lead to the same matter power spectrum as a 1.4 keV thermal relic. V05 then generated a series of thermal relic matter power spectra using Boltzmann codes such as CAMB, and found that their results could be well fit at large  $k$  by the equation  $P_{\text{WDM}}(k) = T^2(k)P_{\text{CDM}}$ , where the transfer function  $T(k)$  has the functional form

$$T(k) = [1 + (\alpha k)^{2\nu}]^{-5/\nu}. \quad (2)$$

Here  $\nu$  is a parameter determined by fitting to the full Boltzmann code transfer function; V05 find a best-fitting value of  $\nu = 1.12$ . The  $\alpha$  parameter is a function that depends on the thermal relic mass (see equation 7 of V05). This fitting function and parametrization provide a good fit for  $k < 5 h \text{ Mpc}^{-1}$ .

We now analyse the correspondence between this fitting function and our matter power spectra. Since the work of Dodelson & Widrow (1994), further developments in the calculation of sterile neutrino properties have broken the precise link between thermal relic mass and sterile neutrino mass given in equation (1) (Abazajian et al. 2001b; Abazajian & Fuller 2002; Dolgov & Hansen 2002; Asaka, Laine & Shaposhnikov 2006; Asaka et al. 2007). To make this point explicit, we plot the V05 curve for a 1.4 keV thermal relic in Fig. 4. We find that the agreement between the ‘true’ NRP sterile neutrino curve and the derived thermal relic curve is still better than 10 per cent at  $k \leq 5 h \text{ Mpc}^{-1}$ . However, the thermal relic has considerably less power at larger  $k$ . The thermal relic curve peaks at a  $k = 5.5 h \text{ Mpc}^{-1}$ , 10 per cent below the sterile neutrino peak. It also exhibits a much more rapid cut-off than the sterile neutrino, such that by  $k \approx 12 h \text{ Mpc}^{-1}$  the amplitude of the thermal relic power spectrum is only half that of the sterile neutrino spectrum.

In order to be check our calculation, we generated thermal relic matter power spectra using our modified version of CAMB. The agreement around the peak in  $\Delta^2$  between the thermal relic Boltzmann calculations and the V05 fit is at the per cent level. We also note that recently Paduroiu, Revaz & Pfenniger (2015) argued that previous studies had underestimated the free-streaming length of thermal relics, which would further increase the tension with sterile neutrino properties.

The scales around the cut-off play an important role in structure formation, and thus this discrepancy between thermal relics and sterile neutrinos is important for this study. Since most simulation-based studies of sterile neutrinos and generic WDM have been performed using the V05 transfer function, care should be taken when comparing our results with previous work. For the remainder of this paper we use the CAMB-derived sterile neutrino transfer functions except where stated otherwise.

### 3 METHODS

In order to calculate the satellite galaxy abundance, and consequently place limits on the sterile neutrino mass, we employ the same methodology as Kennedy et al. (2014), only now applied to sterile neutrinos rather than thermal relics. We use our sterile neutrino power spectra, which are now functions of the sterile neutrino mass and lepton asymmetry as shown in Fig. 4, to generate dark matter halo merger trees for a series of host halo masses. These merger trees are combined with a state-of-the-art semi-analytic galaxy formation model to generate populations of satellite galaxies. The number of satellites is then compared to the measured abundance of Milky Way satellites. The number of dark matter subhaloes above some mass, and thus the number of satellites galaxies, is roughly proportional to the mass of the halo (Wang et al. 2012, and references therein). If the number of satellites resulting from a given combination of sterile neutrino mass, lepton asymmetry, and host halo mass fails to produce enough satellites to meet the number expected for the Milky Way then that combination is ruled out. We can then use estimates on the mass of the Milky Way halo to constrain the sterile neutrino mass and lepton asymmetry.

Our chosen semi-analytic model is the Gonzalez-Perez et al. (2014) version of the GALFORM model of galaxy formation (Cole et al. 2000; Benson et al. 2003; Bower et al. 2006). This model calculates the evolution of galaxies throughout cosmic history, following the formation of dark matter haloes, the accretion and shock-heating of infalling gas that subsequently cools to form stars and the accretion of satellites on to haloes. It accounts for processes such as the photoionization and the chemical enrichment of gas and stars.

Star formation is regulated by feedback from both active galactic nuclei (AGN) accretion and, very importantly on the mass scales of interest here, supernovae. The expulsion of gas from the galaxy due to supernova feedback is modelled assuming that the mass loading is a power law of the galaxy circular velocity; the power-law index, denoted  $\alpha_{\text{hot}}$ , with a fiducial value of 3.2. This value is determined by calibrating to observations of the  $z = 0$  galaxy luminosity function assuming cold dark matter (CDM). It should therefore be recalibrated for sterile neutrino models. Kennedy et al. (2014) found a value of  $\alpha_{\text{hot}} = 3.0$  (with a slight dependence on the warm dark matter particle mass), and we adopt this value throughout this study except where stated otherwise. A discussion of the re-calibration of the model may be found in Appendix A. The fiducial (i.e. CDM) model parameters as a whole are determined by calibrating their values to make reasonable predictions for the evolution of the rest-frame  $K$  band and optical luminosity functions simultaneously: a comprehensive discussion can be found in Gonzalez-Perez et al. (2014).

We apply this model to merger trees of dark matter haloes generated using the extended Press–Schechter (EPS) formalism (Press & Schechter 1974; Bond et al. 1991), and assume the *Planck* cosmological parameters:  $\Omega_0 = 0.307$ ,  $h = 0.678$ ,  $\Omega_\Lambda = 0.693$ ,  $\Omega_b = 0.0483$ ,  $\sigma_8 = 0.823$ , and  $n_s = 0.961$ .

### 3.1 EPS implementation

The rms density fluctuation,  $\sigma(M)$ , can be written as

$$\sigma^2(M) = \frac{1}{2\pi^2} \int_0^\infty k^2 P(k) W^2(k; M) dk, \quad (3)$$

where  $W_k(k; M)$  is a window function which, in the standard EPS method, is chosen to be a top hat in real space. In Fourier space, this window function has the form  $W(k; M) = 3[\sin(kR) - kR\cos(kR)]/(kR)^3$ , where the mass,  $M$ , and filtering scale,  $R$ , are unambiguously related through  $M = \frac{4}{3}\pi\bar{\rho}R^3$ . Decreasing the mass of the window function has the effect of reweighting large  $k$  modes. This means that if the power spectrum has a sharp cut-off,  $\sigma(M)$  will continue to increase with decreasing  $M$ , even though no new modes enter the filter.

An alternative to the real space top hat is a sharp  $k$ -space filter. With this choice, the flattening of  $\sigma(M)$  is set entirely by the sharpness of the power spectrum cut-off. However, this raises the problem that it is no longer clear how to relate the mass to the filtering scale. On dimensional grounds  $M \propto k_{\text{cut}}^{-3}$ , and to maintain the usual relation between mass and radius we can write  $M_{\text{SK}} = \frac{4}{3}\pi\bar{\rho}R_{\text{SK}}^3$ , with  $R_{\text{SK}} = a/k_{\text{cut}}$ , where  $a$  is a constant which needs to be determined. By integrating the mean density under the window function and setting this equal to the required mass, Lacey & Cole (1993) find a value of  $a = (9\pi/2)^{1/3} \approx 2.42$ . Benson et al. (2013) and Schneider, Smith & Reed (2013) match their results to  $N$ -body simulations, and find values of  $a = 2.5$  and  $2.7$ , respectively.

The use of a sharp  $k$ -space filter has been shown to be a suitable approach for the V05 transfer function (Benson et al. 2013), which has a cut-off sharper than many of our models, as shown in Section 2. To check that the method is still valid for our shallower sterile neutrino dark matter cut-offs it is necessary to check the calibration against  $N$ -body simulations.

To this end, we identified which of our set of sterile neutrino matter power spectra has the shallowest cut-off of the whole set –  $M_s = 3$  keV and  $L_6 = 14$ , hereafter M3L14 – and used this as the input transfer function for re-runs of four of the Aquarius Project Milky Way dark matter haloes: Aq-A, Aq-B, Aq-C, and Aq-D (Springel

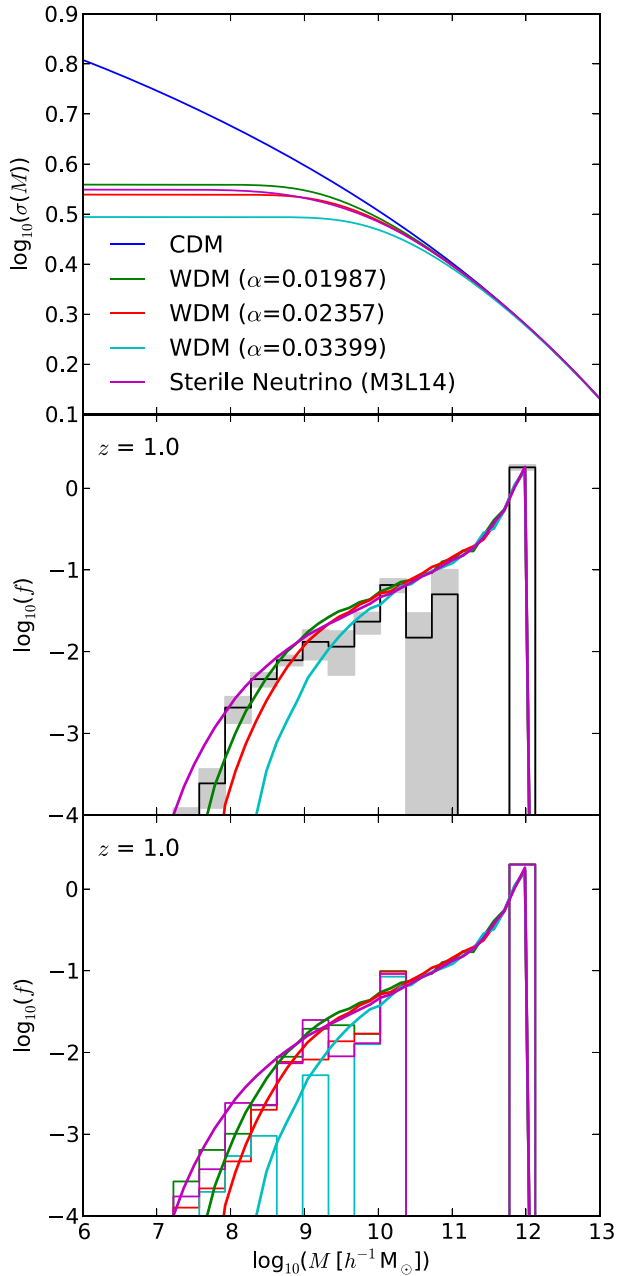
et al. 2008). These were run at Aquarius resolution level 3 (softening length 120.5 pc, particle mass  $5.6 \times 10^4, 2.5 \times 10^4, 5.4 \times 10^4$ , and  $5.4 \times 10^4 M_\odot$ , respectively) with the P-GADGET3 code; the cosmological parameters were 7-year Wilkinson Microwave Anisotropy Probe (WMAP-7; Komatsu et al. 2011). Haloes and subhaloes were identified using the gravitational potential unbinding code, SUBFIND (Springel et al. 2001). Spurious subhaloes – those subhaloes that form by spurious fragmentation of filaments – were identified and removed from the catalogues using the Lagrangian region shape and maximum mass criteria of Lovell et al. (2014). We then compare the conditional mass functions of these simulations with those derived from the EPS method. For a halo of mass  $M_2$  at  $z_2 = 0$ , the conditional mass function gives the fraction of its mass is contained within progenitor haloes of mass  $M_1$  at some earlier redshift  $z_1$ .

We plot the conditional mass functions at  $z_1 = 1$  in Fig. 6, where the haloes have a final mass of  $M_2 \sim 1.5 \times 10^{12} h^{-1} M_\odot$ . In the top panel we compare the rms density fluctuations of the M3L14 matter power spectrum with those of CDM and also three V05 thermal relic power spectra with transfer function parameters  $\alpha = 0.0199, 0.0236$ , and  $0.0340 h^{-1} \text{Mpc}$ , which correspond to thermal relic masses  $M_{\text{th}} = 2.3, 2.0$ , and  $1.5$  keV, respectively (Lovell et al. 2014). These were calculated using a sharp  $k$ -space filter with  $a = 2.7$ . The M3L14 model has a different behaviour than the thermal relic models, in that the curve peels away from CDM at the same mass scale as the  $\alpha = 0.0236$  model but has a slightly shallower slope for large masses. Compared to the  $\alpha = 0.0236$  thermal relic  $\sigma$  has a lower amplitude at intermediate mass scales but a higher amplitude for  $M < 10^9 h^{-1} M_\odot$ . This change is reflected in the  $z_1 = 1$  conditional mass functions:  $M \gtrsim 10^9 h^{-1} M_\odot$ , M3L14 produces a similar number of haloes as the  $\alpha = 0.0236$  thermal relic model, but below this mass the rate of decrease is much shallower such that at  $M \sim 10^8 h^{-1} M_\odot$  M3L14 has a greater abundance of haloes than even the  $\alpha = 0.0199$  thermal relic model. In spite of this change, there is still good agreement between the number of substructures predicted by the EPS method and the number measured in the cleaned simulation halo catalogues. We choose a value of  $a = 2.7$  as this produces the best agreement, but the effect of varying  $a$  is small.

### 3.2 Comparing the number of semi-analytic satellites to observations

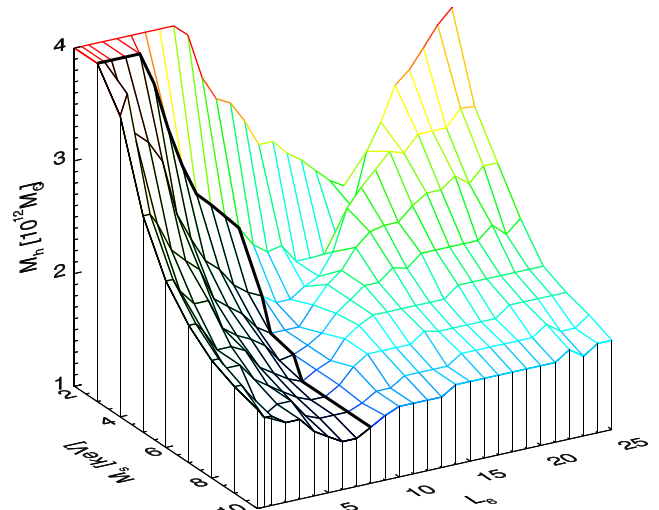
The procedure for determining the number of satellites required for a model to be acceptable is the same as in Kennedy et al. (2014). We retain from that work the conservative assumptions that the census of classical satellites is complete across the entire sky (11 satellites including the Magellanic Clouds), and that the distribution of likely Milky Way satellites from more recent surveys is isotropic.

This last assumption is complicated by the recent discovery of  $\sim 13$  satellites by the Dark Energy Survey (DES; Bechtol et al. 2015; Drlica-Wagner et al. 2015; Koposov et al. 2015), whose identity as satellites rather than globular clusters is established from their half-light radii,  $r_h$ , all of which exceed 30 pc. Up to 11 of those DES satellites with  $M_V < -2$  are likely to have been satellites of the Large Magellanic Cloud (LMC; Jethwa, Erkal & Belokurov 2016). Regardless of their origin, the satellites have been shown in these studies to be anisotropic in their distribution across the DES footprint. In order to incorporate these satellites into our algorithm, we add the 11 likely LMC satellites to the list of classical satellites which we assume is complete across the sky, and add the remaining two DES satellites – along with the corresponding extra sky coverage – to the ‘isotropic’ Data Release 5 (DR5) selection that



**Figure 6.** Top panel:  $\sigma(M)$ , the rms density fluctuation smoothed over mass scale,  $M$ , using a sharp  $k$ -space filter with  $a = 2.7$ , for CDM, WDM and sterile neutrinos where, for WDM,  $\alpha$  determines the position of the cut-off in the power spectrum. Middle panel: mean conditional mass function of four  $N$ -body sterile neutrino haloes, based on the Aquarius Project with *WMAP-7* cosmological parameters (black histogram);  $1\sigma$  errors are shown by the grey shaded area. Colour lines are the mean conditional mass functions of 1000 Monte Carlo simulations, using a sharp  $k$ -space filter, for the different DM cases, with the same colours as in the top panel. Bottom panel:  $N$ -body conditional mass functions from halo A for the different DM cases (colour histograms). Curved lines are the same Monte Carlo conditional mass functions from the middle panel.

also includes the 11 Sloan Digital Sky Survey (SDSS) DR5 satellites. This choice enables us to take account of the LMC–Small Magellanic Cloud (SMC) system without almost certainly overestimating the number of unobserved satellites. In addition, analyses of the VST-Atlas and Pan-STARRS  $3\pi$  surveys have discovered one



**Figure 7.** The surface that shows the values of  $M_h$  as a function of sterile neutrino mass  $M_s$  and lepton asymmetry  $L_6$  that are consistent with the Milky Way satellite data. The plot is cropped such that the maximum permitted value of  $M_h = 4 \times 10^{12} M_\odot$ . The set of models that are excluded at least 95 per cent confidence by the X-ray limits of Watson et al. (2012) and Horiuchi et al. (2014) are shaded in black.

(Torrealba et al. 2016) and three (Laevens et al. 2015a,b) new satellites, respectively. The completeness of these two surveys to date is very uncertain and so to include these satellites in our analysis we make the conservative assumption that they form part of the population assumed to be complete across the sky.

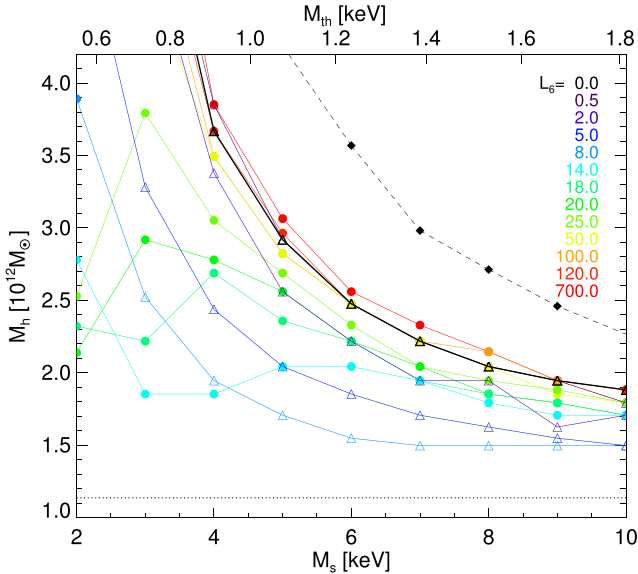
Since SDSS DR5 observed 19 per cent of the sky, and the DES 2-yr study an additional 10 per cent, we are therefore interested in the number of ‘isotropic distribution satellites’ within 30 per cent of the sky. For each galaxy generated by the semi-analytic model we determine the number of satellite galaxies within the halo virial radius having  $M_V < -2$ , and compare this to the number of Milky Way satellites within this same virial radius inferred from the observations. We then iteratively determine the minimum mass<sup>5</sup> of the host halo that would produce the required number of satellites for a given sterile neutrino model, which we define formally to be the smallest halo mass that, for 200 merger tree realizations, produces enough satellites at least 5 per cent of the time. We denote this minimum halo mass as  $M_h$ ; full details of the procedure can be found in Kennedy et al. (2014).

## 4 RESULTS

### 4.1 Constraints on sterile neutrino parameters

We begin the presentation of our results with a 3D plot of  $M_h$  as a function of both sterile neutrino mass and lepton asymmetry in Fig. 7. The range of sterile neutrino masses is 2–10 keV, and of  $L_6$  is 0–25. We also compare the results with limits on  $M_s$ – $L_6$  from

<sup>5</sup> The masses returned by *GALFORM* are defined as ‘Dhalo’ masses, which constitute the gravitationally bound mass of the halo. For a given relaxed halo the Dhalo mass is typically less than 20 per cent larger than the measured virial mass,  $M_{200}$  (Jiang et al. 2014). Therefore when quoting values for  $M_h$  we will assume they are equivalent to  $M_{200}$ .



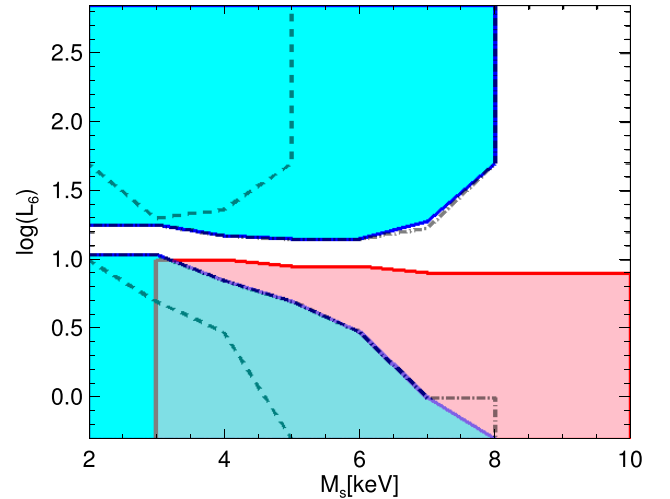
**Figure 8.** The Milky Way halo mass required to account for the observed number of Milky Way satellites, plotted as a function of sterile neutrino mass. Regions above and to the right of a given line are allowed; those below and to the left are disallowed. Colour lines show constraints for different values of the lepton asymmetry. Empty triangles denote  $M_s$ – $L_6$  combinations that are excluded by X-ray non-detections (black region in Fig. 7), as presented in Boyarsky et al. (2014), and filled circles those that are not excluded. The dashed black line is the constraint for trees generated with the V05 thermal relic fitting function discussed in Section 2. The thermal relic masses, calculated from equation (1), are shown on the top axis. The dotted line shows the result obtained for CDM.

X-ray decay non-detections (95 per cent confidence limit; Watson, Li & Polley 2012; Horiuchi et al. 2014).

The allowed values of  $M_h$  decrease as the sterile neutrino mass increases, in the same manner as one would expect for a thermal relic. The non-monotonic behaviour with lepton asymmetry is reflected in the fact that, for a given  $M_s$ ,  $M_h$  attains a minimum value for a specific value of  $L_6$ , which we denote  $L_{6,\min}$ . The value of  $L_{6,\min}$  decreases with sterile neutrino mass, falling from  $L_{6,\min} = 16$  at  $M_s = 3$  keV to  $L_{6,\min} = 6$  at  $M_s = 10$  keV, producing a characteristic winding valley shape in the surface. For  $M_s > 5$  keV the position of the valley floor happens to coincide with the constraints from X-ray observations. Thus, further non-detections in this mass range would force the sterile neutrinos to be ‘warmer’. We also ran the same set of models for the fiducial value of  $\alpha_{\text{hot}} = 3.2$  – and found an increase of no more than 10 per cent in  $M_h$  for any of our  $M_s$ – $L_6$  combinations. Thus, we are confident that the choice of  $\alpha_{\text{hot}}$  calibration makes little difference to the results.

We expand on our results in Fig. 8, in which we plot a separate  $M_h$ – $M_s$  relation for each value of  $L_6$ . We have also generated merger trees for thermal relic power spectra using the V05 transfer function for thermal relic masses in the range [0.79–1.8] keV.

Spectra with  $L_6 = 0$  and 700 result in very similar allowed values of  $M_h$  for a given sterile neutrino mass, as expected from their input matter power spectra. The minimum acceptable value of  $M_h$  drops by over a factor of 2 between the most extreme values of  $L_6$  and the optimal value  $L_6 \sim 10$ , especially at the lowest masses where the results are predominantly determined by the sterile neutrino transfer function rather than by the galaxy formation physics. However, the lowest possible value of  $M_h$  is given by CDM, which occurs at  $M_h = 1.16 \times 10^{12} M_\odot$ : therefore, the sterile neutrino models with still



**Figure 9.** Excluded region in the  $M_s$ – $L_6$  plane. For sterile neutrino parameters in the cyan shaded region the correct number of Milky Way satellite would require the mass of the halo,  $M_h > 2 \times 10^{12} M_\odot$ , which is disfavoured by current astronomical data. The red shaded region is excluded from a non-observation of the X-ray decay line. Even for masses as low as  $M_s = 2$  keV there exist primordial distribution functions ‘cold enough’ to predict the Galactic structures in accordance with observations. The dashed and dashed–dotted lines show how the excluded regions change when one of the GALFORM parameters is varied. The dashed line shows the effect of change of  $v_{\text{cut}}$  from its fiducial value ( $30 \text{ km s}^{-1}$ ) down to  $v_{\text{cut}} = 25 \text{ km s}^{-1}$ . The dashed–dotted line shows the effect of change of  $z_{\text{cut}}$ , from its default value  $z_{\text{cut}} = 10$  to 12; see the text for parameter definitions.

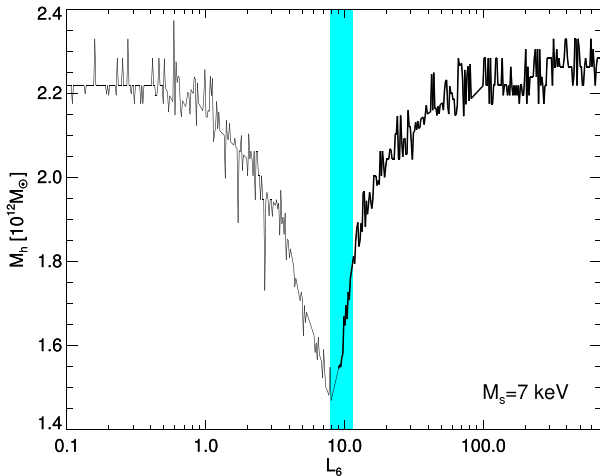
higher masses may return a value of  $M_h$  up to  $\sim 3 \times 10^{11} M_\odot$  lower before hitting the CDM limit.

We can seek to rule out models by making conservative assumptions about the mass of the Milky Way halo. Estimates of the Milky Way halo mass have been made using a variety of methods, including the local Hubble flow (Peñarrubia et al. 2014), dynamical tracers (Deason et al. 2012; Piffl et al. 2014; Wang et al. 2015), the kinematics of bright Milky Way satellites (Sales et al. 2007a,b; Busha et al. 2011; Wang et al. 2012; Boylan-Kolchin et al. 2013; González, Kravtsov & Gnedin 2013; Cautun et al. 2014), and the timing argument (Kahn & Woltjer 1959; Li & White 2008); for a more comprehensive list see Wang et al. (2015). Together these studies allow a wide range of possible halo masses:

$$0.5 \times 10^{12} < M_{200} < 2 \times 10^{12} M_\odot, \quad (4)$$

where  $M_{200}$  is the mass enclosed within the radius of overdensity 200. In order to set a conservative constraint, we take our upper limit to be  $M_h = 2 \times 10^{12} M_\odot$ ; here we have again assumed that the Dhalo definition of mass in our model is approximately equal to  $M_{200}$ . This value rules out a swathe of models with  $M_s < 7$  keV. We find that the non-resonant sterile neutrino ( $L_6 = 0$ ) is ruled out for  $M_s \leq 8$  keV. This bound is weaker, although compatible with the SDSS-based Lyman  $\alpha$  bounds (Seljak et al. 2006; Viel et al. 2006; Boyarsky et al. 2009c); it is comparable with the other structure formation bounds (Maccio & Fontanot 2010; Polisensky & Ricotti 2011; Schneider et al. 2013; Lovell et al. 2014).

However, for the resonantly produced sterile neutrinos there exists a range of  $L_6$  which is compatible with the entire allowed range of halo masses (see Fig. 9). In fact, all sterile neutrino masses  $> 3$  keV are permitted for  $L_6 \sim 14$  if the  $M_h$  constraints alone are considered. When combined with the limits from X-ray non-detections, the approximate constraint on sterile neutrino lepton asymmetry in



**Figure 10.** Minimum Milky Way halo mass,  $M_h$ , as a function of  $L_6$  for  $M_s = 7$  keV. The region in  $L_6$  consistent with the 3.5 keV line is shown in cyan. Data points that are in tension with the X-ray constraints ( $L_6 < 9$ ; Watson et al. 2012; Horiuchi et al. 2014) are connected by thin lines, the remainder by thick lines.

the mass range  $3 \leq M_s/\text{keV} < 6$  is  $10 \lesssim L_6 \lesssim 16$ . The upper limit weakens substantially for 7 keV sterile neutrinos, and disappears for  $M_s > 9$  keV.

We have previously shown that our results are sensitive to the  $\alpha_{\text{hot}}$  feedback parameter at the 10 per cent level, however, Kennedy et al. (2014) showed that there exist other systematic uncertainties within the galaxy formation model that may have a larger effect, and in particular the parameters regulating reionization feedback. GALFORM models reionization such that haloes in the merger tree that have a circular velocity lower than some parameter  $v_{\text{cut}}$  at a redshift of  $z_{\text{cut}}$  do not contain any gas: this reflects the heating of the gas by a background of ionizing photons (Cole et al. 2000; Benson et al. 2006), thus preventing it from ever falling into the halo. In the Gonzalez-Perez et al. (2014) version of GALFORM  $v_{\text{cut}} = 30 \text{ km s}^{-1}$  and  $z_{\text{cut}} = 10$ . In Fig. 9 we also derived limits for  $z_{\text{cut}} = 12$  and  $v_{\text{cut}} = 25 \text{ km s}^{-1}$ . The former has very little effect on our results, however, the lowering of  $v_{\text{cut}}$  introduces many more small galaxies and thus weakens our limits substantially. An increase in  $v_{\text{cut}}$  would have the exact opposite effect.

In order to explore the behaviour of the model in greater detail, and determine precisely the consequences for the 3.5 keV line/7 keV sterile neutrino, we calculate  $M_h$  for the fine grid of  $M_s = 7$  keV models used in Figs 3 and 5. The results are plotted in Fig. 10.

The profile of allowed values of  $M_h$  again has a valley shape, and sharp features are introduced by stochastic scatter in the number of halo satellites. The lowest allowed value of  $M_h$  is  $1.5 \times 10^{12} M_{\odot}$ , which is comfortably within the range estimate for the Milky Way. This occurs at  $L_6 \approx 8$ , and either side of this, the constraint on  $M_h$  rises rapidly to a maximum of  $\approx 2.3 \times 10^{12} M_{\odot}$ . The region consistent with the 3.5 keV line falls near the centre of the trough in  $M_h$ . Thus, the minimum allowed  $M_h$  for the line is  $1.5 \times 10^{12} M_{\odot}$ . As was the case for the full range of  $M_s$ , the X-ray non-detection 95 per cent exclusion range terminates at the bottom of the trough, such that further, more stringent non-detections would force  $M_h$  to increase. It is also the case that if the ‘true’ momentum distribution function exhibits a stronger back reaction than is assumed here,  $M_h$  would increase and the limits become stronger. However, for the present study we are content that values of lepton asymmetry in the

range  $2 \lesssim L_6 \lesssim 20$  are consistent with the current estimate of the Milky Way halo mass.

## 4.2 Comparison to thermal relics

We now compare these results for sterile neutrinos with those for V05 thermal relics as used in (Kennedy et al. 2014). They restricted their analysis to relics of mass 1.5 keV and larger; we extend our analysis to lower masses to show the trend obtained, even though it would be unlikely that we could recalibrate the model to get the correct luminosity functions. We therefore compute nine V05 thermal relic power spectra in the mass range [0.7,1.8] keV and perform the same semi-analytic procedure as used on the sterile neutrino models. These are included in Fig 8, with the equation (1) conversion from sterile neutrino mass to thermal relic mass shown along the top x-axis.

We find that sterile neutrino power spectra with V05 thermal-relic equivalent masses as low as 1.2 keV<sup>6</sup> can generate enough satellites and be compatible with our adopted upper limit of  $M_h < 2 \times 10^{12} M_{\odot}$ , whereas previous studies that used the V05 fit in simulations have shown that the thermal relic mass should be at the very least 1.6 keV (Lovell et al. 2014) and preferably higher still ( $> 2.3$  keV; Polisensky & Ricotti 2011). Kennedy et al. (2014) found that a 1.5 keV thermal relic generated from V05 would require  $M_h \approx 2.2 \times 10^{12} M_{\odot}$ : our V05 relic calculation returns  $M_h \approx 2.3 \times 10^{12} M_{\odot}$ , which is encouraging given that the choice of GALFORM model and cosmology differ between their study and ours. When instead considering our results that include the DES satellites, the  $M_h$  results for the V05 relics are  $\approx 25$  per cent higher than would be obtained for our sterile neutrinos with the corresponding V05 thermal relic mass. Therefore care should be taken when comparing our results to previous studies.

## 5 CONCLUSIONS

Sterile neutrinos are an intriguing dark matter candidate. The underlying model of particle physics can potentially solve many unanswered questions in astronomy and particle physics, and provides a possible explanation for the unidentified 3.5 keV X-ray line recently seen in galaxies and clusters (Boyarsky et al. 2014, 2015; Bulbul et al. 2014). In addition to its role as an X-ray emitter, the sterile neutrino can act like warm dark matter and have properties that are imprinted on the abundance and structure of the Milky Way’s satellite galaxies. We therefore set out to calculate how the parameters of the sterile neutrino model can be constrained by requiring that the expected number of satellite galaxies in the Milky Way for our chosen galaxy formation model should match the observed number of Milky Way satellites.

We reviewed the history of sterile neutrinos as a dark matter candidate, beginning with the initial suggestion of a single, non-resonantly produced sterile neutrino (Dodelson & Widrow 1994). This new particle was motivated by its ability to generate neutrino oscillations and to make up the dark matter. However it was later shown to be incompatible with non-detections of X-ray decay radiation at large masses and with structure formation constraints at lower masses, such that the model was ruled out (Seljak et al. 2006;

<sup>6</sup> This result, along with those in the rest of this subsection, has been derived using the SDSS satellites alone in order to make a fair comparison with previous work. When the DES satellites are included, as shown in Fig. 8, this minimum thermal relic mass rises to  $> 1.8$  keV.

Viel et al. 2006). Later work showed that the presence of a lepton asymmetry could alleviate both of these constraints (Shi & Fuller 1999). It could allow for a smaller neutrino mixing angle, weakening the X-ray bounds, and through resonant production enhance the production of low-momenta sterile neutrinos, thus resulting in better agreement with the observed properties of galaxies. A series of studies then found that the necessary lepton asymmetry could be generated as part of a wider theory that included two further sterile neutrinos at the GeV scale (e.g. Asaka & Shaposhnikov 2005). The theory as a whole could then explain neutrino oscillations, dark matter, and baryogenesis. When coupled to the possible detection of an X-ray decay line (Boyersky et al. 2014, 2015; Bulbul et al. 2014), the keV sterile neutrino had become a competitive and compelling dark matter candidate.

We discussed how the properties of sterile neutrino dark matter are very similar to those of warm dark matter, in that the sterile neutrinos are able to free stream out of small perturbations in the early Universe, thus truncating the matter power spectrum and preventing small galaxies from forming. We showed how the presence of the lepton asymmetry alters the sterile neutrino momentum distribution function, and how the presence of resonances enhances the number of low momentum particles and thus produce a cooler matter power spectrum. The effectiveness of the lepton asymmetry to produce an arbitrarily cold power spectrum was, however, seen to have its limits, in that large lepton asymmetries enhance production at all momenta and result in a very similar power spectrum to that obtained for standard warm dark matter. We also compared the sterile neutrino matter power spectra to those described by the fits used in Lyman  $\alpha$  studies, and found that the latter underestimates the power on comoving scales  $>5 h \text{ Mpc}^{-1}$  due to subsequent developments in the calculation of sterile neutrino momentum distributions.

The sterile neutrino model described above is a two parameter model, with a particle mass,  $M_s$ , and a value of the lepton asymmetry,  $L_6$ . We assembled a grid of  $M_s$  and  $L_6$  pairs, generated their matter power spectra, and used these spectra to build dark matter halo merger trees. We then populated these haloes with galaxies using the GALFORM semi-analytic model of galaxy formation and evolution, and thus calculated their satellite galaxy abundances as a function of the assumed Milky Way halo mass. Thus the number of satellites depends both on the sterile neutrino properties and on the Milky Way halo mass. We found that heavier sterile neutrinos are viable candidates even if the Milky Way halo mass is at the lower end of its observationally allowed range, as is the case for thermal relics. For each particle mass we can associate a characteristic lepton asymmetry associated with it for which the allowed lower limit on the halo mass is minimized. By assuming that the Milky Way halo mass must be no higher than  $2 \times 10^{12} M_\odot$ , we were able to constrain the lepton asymmetry for sterile neutrino masses lower than 9 keV. We showed that the range of 7 keV lepton asymmetries favoured by the 3.5 keV X-ray line requires the Milky Way halo mass to be no less than  $1.5 \times 10^{12} M_\odot$ , well within acceptable bounds. The relationship between minimum allowed halo mass and the wavenumber of the peak of the input matter power spectrum was shown to be tight, and any variation between models with the same peak location could be at least partly explained by differences in the power spectrum slope.

A major uncertainty in our analysis is the total number of satellites that orbit the Milky Way. This is uncertain because current surveys do not cover the whole sky and it is well known that at least the brightest satellites appear in an anisotropic configuration. The number of satellites already known to exist is already approaching the total number of subhaloes predicted to exist in even the coldest

of the sterile neutrino models that are consistent with the 3.5 keV line. A complete census of the satellites population of the Milky Way, which may be obtained with future surveys, may well conclusively rule out the 7 keV resonantly produced sterile neutrino as the dominant component of the dark matter.

Sterile neutrinos are thus a very interesting dark matter candidate, and the 7 keV candidate that could be the source of the 3.5 keV line is in good agreement with current observations of the Milky Way satellites. There remain nevertheless many uncertainties in the argument presented in this paper. The main limitations are uncertainties in the galaxy formation model, particularly the treatment of supernova and photoreionization feedback and how these affect the mass of their host haloes, although the current generation of simulations (Sawala et al. 2016; Fattahi et al. 2016; Oñorbe et al. 2015) are providing valuable insights, at least for CDM. Observationally, the total number and radial distribution of satellites remains poorly constrained. An exciting and powerful development will be X-ray constraints from other observational targets. In particular, observations of dark-matter-dominated satellites have the potential to either rule out much more of the  $M_s$ - $L_6$  parameter space or to obtain further detections of the 3.5 keV line. Such a detection could be used in tandem with dwarf spheroidal mass estimates (Walker et al. 2009, 2010; Wolf et al. 2010) to determine the sterile neutrino mixing angle and therefore the lepton asymmetry. This could lead to an accurate determination of the matter power spectrum, and thus perhaps to a new paradigm in galaxy formation and cosmology.

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## APPENDIX A: FEEDBACK CALIBRATION

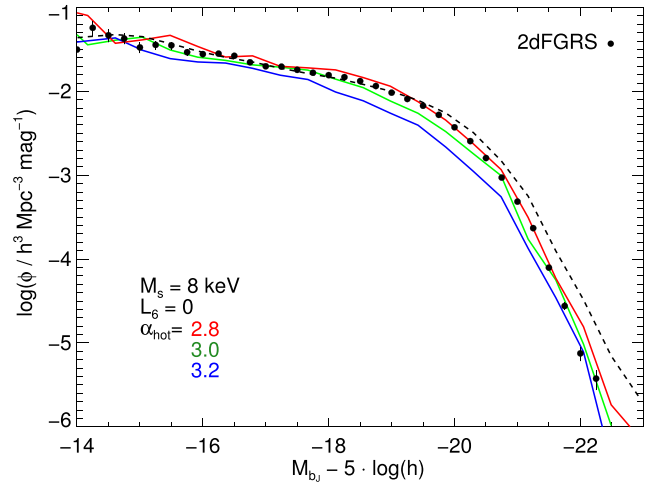
It is a well-known issue in astrophysics that stellar feedback plays a crucial role in regulating the stellar mass of galaxies in general, and thus the number of bright Milky Way satellites in particular. In the model of Gonzalez-Perez et al. (2014) the strength of stellar feedback is parametrized in terms of the mass loading parameter,  $\beta$ , which in this model is defined as the ratio of the gas ejection rate and the star formation rate.  $\beta$  is a function of the circular velocity of the disc and the bulge,  $v_{\text{circ}}$ , and takes the form

$$\beta = \left( \frac{v_{\text{circ}}}{v_{\text{hot}}} \right)^{-\alpha_{\text{hot}}}, \quad (\text{A1})$$

where  $v_{\text{hot}}$  and  $\alpha_{\text{hot}}$  are parameters of the model; their fiducial values are deemed to be those that provide a good fit to the local  $b_J$ - and  $K$ -band luminosity functions, and in this model take the values  $v_{\text{hot}} = 425 \text{ km s}^{-1}$  and  $\alpha_{\text{hot}} = 3.2$ .

Kennedy et al. (2014) showed that the lower concentrations of WDM haloes result in lower values of  $v_{\text{circ}}$  for a halo of a given mass, and that therefore a recalibration is required to still match the observed  $b_J$ - and  $K$ -band luminosity functions at  $z=0$ : they required  $\alpha_{\text{hot}} = 3.0$  for the 1.5 keV thermal relic and proposed a functional form to fit all cooler models up to the limit of  $\alpha_{\text{hot}} = 3.2$  for CDM. We extend this result to one of our sterile neutrino models in Fig. A1, in which we display the  $b_J$  luminosity function for a sterile neutrino with  $M_s = 8 \text{ keV}$  and  $L_6 = 0$  (i.e. NRP) when adopting  $\alpha_{\text{hot}} = 2.8, 3.0,$  and  $3.2$ . We select 8 keV NRP because it is expected to have a power spectrum similar to that of the 1.5 keV thermal relic limit considered by Kennedy et al. (2014); 1.5 keV is also the 99.7 per cent confidence limit lower bound from Lyman  $\alpha$  constraints inferred by Boyarsky et al. (2009b). The fiducial value – i.e. that used for CDM – of  $\alpha_{\text{hot}} = 3.2$  underpredicts the number of galaxies across all magnitudes as expected. The other two values of  $\alpha_{\text{hot}}$  lie much closer to the observations, with  $\alpha_{\text{hot}} = 3.0$  underpredicting the number of galaxies at magnitudes  $\sim -19$  and  $\alpha_{\text{hot}} = 2.8$  slightly overpredicting the number of both very luminous and faint galaxies. It is therefore necessary to make an adjustment to the fiducial model to account for the differences in WDM structure formation.

For the present study one approach would be to recalibrate  $\alpha_{\text{hot}}$  for all of our transfer functions individually. Another option would be instead to adopt the value fitted by Kennedy et al. (2014),  $\alpha_{\text{hot}} = 3.0$ , and apply this to all of our models. In this case the models will overpredict the number of satellites for those combinations of  $L_6$  and



**Figure A1.** The  $b_J$ -band luminosity function at  $z=0$  for an 8 keV sterile neutrino (NRP) with  $\alpha_{\text{hot}} = 2.8, 3.0,$  and  $3.2$  displayed as red, blue, and green lines, respectively. The observational data from the 2dFGRS (Cole et al. 2005) are shown as filled circles. The fiducial CDM model as developed in Gonzalez-Perez et al. (2014) is shown as a dashed black line.

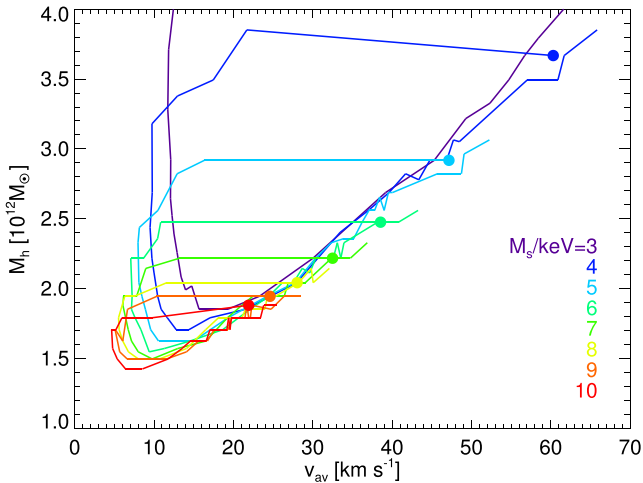
$M_s$  that are not already in severe tension with Lyman  $\alpha$  constraints; any combination that nevertheless fails to produce enough satellites for the expected range of halo masses will be ruled out confidently. We therefore adopt the conservative value  $\alpha_{\text{hot}} = 3.0$  for all the results published here. In several cases we have also performed runs with the fiducial value of  $\alpha_{\text{hot}} = 3.2$ , and compared the two sets of results in the text.

There are other relevant parameters that can have important effects on the satellite galaxy abundance, such as the minimum value of  $v_{\text{circ}}$  required for a galaxy to retain its gas after reionization, and have a brief discussion of this topic in Section 4. However, the primary purpose of this study is to carry out an exploration of the kind of constraints that can be imposed on sterile neutrino models from the observed abundance of Milky Way satellites. We leave more detailed investigation into the effects of galaxy formation to future work. See Kennedy et al. (2014) for a discussion of these parameters.

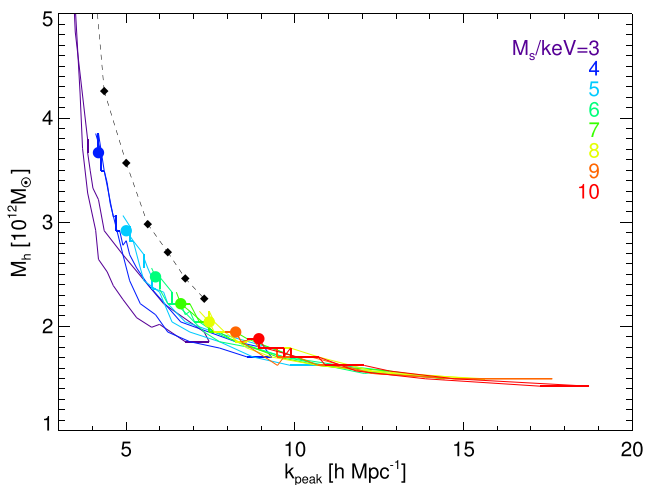
## APPENDIX B: RELATIONSHIP BETWEEN MODEL CHARACTERISTIC SCALES AND MINIMUM HALO MASS

Having established the dependence of the minimum allowed value of  $M_h$  on the particle physics parameters, sterile neutrino mass and lepton asymmetry, we now examine how this relationship is mediated by properties measured from the distribution function and the matter power spectrum. The first variable that we consider is the average velocity at matter-radiation equality,  $v_{\text{av}}$ , which we adopt as a proxy for the free-streaming velocity. Larger free-streaming velocities dampen more small-scale power and thus require a larger  $M_h$ . We show the dependence of  $M_h$  on  $v_{\text{av}}$  for our  $M_s$ - $L_6$  sample in Fig. B1, and highlight NRP models with circles so as to discern the additional features that resonant production entails.

We find that for NRP sterile neutrinos,  $M_h$  increases exponentially with  $v_{\text{av}}$ . The reduction in  $v_{\text{av}}$  that results from the lepton asymmetry causes  $M_h$  to decrease very slowly at first, and then plummets to a minimum before recovering gradually back towards the NRP solution. The lowest value of  $v_{\text{av}}$  does not produce the lowest  $M_h$ , a result that could be inferred by noting that the maximum value of  $k_{\text{peak}}$  and minimum value of  $v_{\text{av}}$  occur at different values of  $L_6$



**Figure B1.** Minimum value of  $M_h$  required to obtain the observed number of Milky Way satellites as a function of the average velocity,  $v_{av}$ , for  $M_s$  in the range 3–10 keV. Each line corresponds to the series of  $L_6$  for a given  $M_s$ ; the correspondence between line colour and  $M_s$  is given in the legend.  $L_6 = 0$  is denoted by a circle. Thick lines show regions that are in agreement with the X-ray non-detection bounds (Watson et al. 2012; Horiuchi et al. 2014).

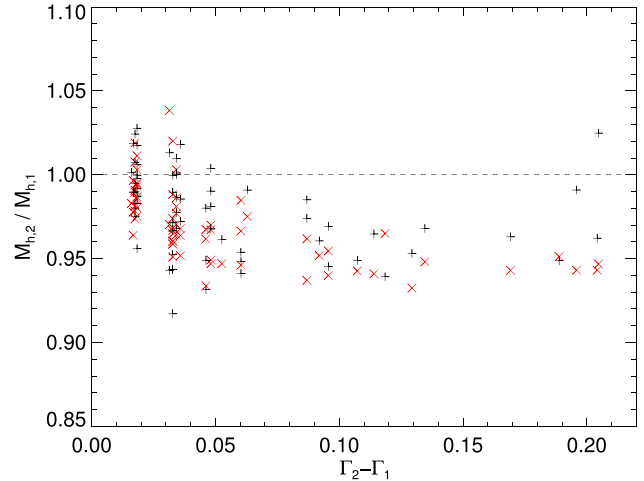


**Figure B2.** The minimum acceptable value of  $M_h$  required to obtain the observed number of Milky Way satellites as a function of the matter power spectrum peak wavenumber,  $k_{peak}$ , for  $M_s$  in the range 3–10 keV. The colours and symbols are the same as in Fig. B1. We also include the results for the V05 thermal relics, shown as diamonds.

(cf. Figs 3 and 5a.) For some  $M_s$ , two values of  $M_h$  at a given  $v_{av}$  can differ by over a factor of 2. We therefore conclude that, in general,  $v_{av}$  is not a good predictor of  $M_h$ . However, if one restricts attention to models with  $L_6 > L_{6, min}$ , we do obtain a clear correlation. Given that for many values of  $M_s$  it is precisely this range of  $L_6$  that is permitted by the X-ray decay constraints, with the help of the latest galaxy formation models it may indeed be possible to predict  $M_h$  from  $v_{av}$  for X-ray-viable models.

An alternative property for determining  $M_h$  is the power spectrum peak wavenumber,  $k_{peak}$ . Larger values of this parameter allow more power on small scales, thus reducing  $M_h$ . We take the values of  $k_{peak}$  computed for each  $M_s$  as a function of  $L_6$  and plot the resulting  $M_h$ – $k_{peak}$  relation in Fig. B2.

The dependence of  $M_h$  on  $k_{peak}$  is much cleaner than that on  $v_{av}$ .  $M_h$  falls rapidly with increasing  $k_{peak}$ , with an apparent asymptote



**Figure B3.** The ratio of  $M_h$  as a function of the difference in  $\Gamma$  for pairs of 7 keV models that share the same  $k_{peak}$ . We plot raw data and smoothed data as black plus signs and red crosses, respectively.

towards  $1.4 \times 10^{12} M_\odot$  for  $k_{peak} \rightarrow \infty$  (i.e. CDM). The scatter in  $M_h$  between all combinations of  $M_s$  and  $L_6$  that correspond to the same  $k_{peak}$  is rarely more than 10 per cent, with the notable exception of the  $k_{peak} < 5 h \text{ Mpc}^{-1}$  regime and the V05 thermal relics. The latter have  $M_h$  higher than sterile neutrinos at a given  $k_{peak}$  by of order tens of per cent. This shows that it is not sufficient to define a generic WDM-like model purely by  $k_{peak}$ ; the shape of the cut-off is also important.

In order to explore the effect of the cut-off shape further, we consider the variation of the post-cut-off slope,  $\Gamma$ , with lepton asymmetry. We showed in Fig. 5 that  $k_{peak}$  and  $\Gamma$  attain their maximum values at slightly different values of  $L_6$ :  $k_{peak}$  is largest at  $L_6 = 8$  whereas the peak value in  $\Gamma$  occurs at  $L_6 \approx 6.5$ . This offset between the two has the consequence that for each value of  $k_{peak}$  there are two possible values of  $\Gamma$ : a higher one for lower  $L_6$  and vice versa. We investigate the effect of this property by finding pairs of  $L_6$  in our sample of five hundred 7 keV models that have the same values of  $k_{peak}$ , and calculate the difference between their two values of  $\Gamma$  in addition to the ratio of their values of  $M_h$ . Where the finite binning of  $k_{peak}$  forces more than two models to take the same  $k_{peak}$ , we consider the pair that have the largest difference in  $\Gamma$ . We display the results in Fig. B3.

There is a trend in the raw data for  $M_h$  to decrease for shallower slopes by, on average, 5 per cent for  $\Gamma_2 - \Gamma_1 > 0.05$ . In order to reduce the noise due to halo-to-halo scatter, we smooth  $M_h(L_6)$  over the lepton asymmetry range  $[\log(L_6) - 0.077, \log(L_6) + 0.077]$ . The trend then exhibits much reduced scatter, such that all of the model pairs around  $\Gamma_2 - \Gamma_1 > 0.17$  exhibit a decrement of over 6 per cent. However, even the maximum decrement is too small to explain fully the tens of per cent discrepancy that is present for the V05 thermal relics, despite the similarity in the values of  $\Gamma$  for V05 relics and NRP sterile neutrinos shown in Fig. 5(b). It may be that further variations in the spectrum shape not captured by our statistic  $\Gamma$  are relevant for the production of satellite galaxies. Nevertheless, we have shown that the shallower slopes of some resonantly produced sterile neutrinos are the reason for the increase in the number of potential satellites, even in comparison to NRP models with the same  $k_{peak}$ .