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Methods to simulate fermions on quantum computers with hardware limitations

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Methods to simulate fermions on quantum computers with hardware limitations

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