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## Exploration on and of networks

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# Exploration on and of Networks

Hakan Güldas

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# Exploration on and of Networks

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