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Tuning Rashba spin-orbit coupling at LaAlO₃/SrTiO₃ interfaces by band filling

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The electric-field tunable Rashba spin-orbit coupling at the LaAlO₃/SrTiO₃ interface shows potential applications in spintronic devices. However, different gate dependence of the coupling strength has been reported in experiments. On the theoretical side, it has been predicted that the largest Rashba effect appears at the crossing point of the d_{xy} and $d_{xz,yz}$ bands. In this work, we study the tunability of the Rashba effect in LaAlO₃/SrTiO₃ by means of backgating. The Lifshitz transition was crossed multiple times by tuning the gate voltage so that the Fermi energy is tuned to approach or depart from the band crossing. By analyzing the weak antilocalization behavior in the magnetoresistance, we find that the maximum spin-orbit coupling effect occurs when the Fermi energy is near the Lifshitz point. Moreover, we find strong evidence for a single spin winding at the Fermi surface.

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Complex oxide heterostructures provide an interesting platform for novel physics since their physical properties are determined by correlated d electrons [1]. The most famous example is the discovery of a high mobility two-dimensional electron system (2DES) at the interface between LaAlO₃ (LAO) and SrTiO₃ (STO) [2]. Intriguing properties, such as superconductivity [3], signatures of magnetism [4,5], and even their coexistence [6,7], have been reported.

At the LAO/STO interface, the 2DES is confined in an asymmetric quantum well (QW) in STO. The intrinsic structure inversion asymmetry introduces an electric field which gives rise to a Rashba spin-orbit (SO) coupling [8]. Additionally, due to the large dielectric constant of the STO substrate at cryogenic temperatures [9], the coupling constant can be tuned with the STO as a backgate [10–12]. This could give rise to applications in spintronics, such as spin field-effect transistors [13]. However, the reported results are inconsistent. Upon increasing the back-gate voltage (V_G), the SO coupling strength was found to decrease [10], increase [11], or show a maximum [12]. A clear understanding of the SO coupling dependence on V_G is necessary for more advanced experiments.

For a free electron gas the Rashba spin splitting is proportional to the symmetry-breaking electric field. However, the Rashba effect in solids like semiconductor and oxide heterostructures has a more complicated origin [14]. Theoretical studies have shown that multiband effects play an essential role in the SO coupling in LAO/STO [15–17]. At the LAO/STO (001) interface, the band structure is formed by the Ti t_{2g} bands. At the Γ point, the d_{xy} band lies below the $d_{xz,yz}$ bands in energy [18]. Applying V_G across the STO substrate changes the carrier density and therefore the Fermi energy (E_F). A Lifshitz transition occurs when E_F is tuned across the bottom of the $d_{xz,yz}$ bands [19]. The largest SO coupling effect was predicted at the crossing point of the d_{xy} and $d_{xz,yz}$ bands [15,17]. The SO coupling theory was

experimentally confirmed later by angle-resolved photoemission spectroscopy measurements [20].

So far, few experiments actually track the evolution of SO coupling when E_F is driven to approach or depart from the Lifshitz point. The tools for this are fully available, since the carrier concentration in the QW can be varied by using STO as a backgate. The effects of backgating have been extensively researched. A particularly relevant phenomenon is that the sheet resistance (R_s) shows irreversible behavior when V_G is swept first forward and then backward [21,22]. Biscaras *et al.* [23] argued that this is caused by the Fermi level lying intrinsically close to the top of the QW, which leads to thermal escape from the injected carriers. Similar experiments recently performed by some of us led to the conclusion that the irreversible behavior in samples with initially a low carrier density is rather caused by trapping by defects [24]. In this work, we use the same tools, analysis framework, and samples to study the Rashba effect in backgated LAO/STO around the Lifshitz point. By carefully monitoring the sign of the magnetoresistance (MR) in high magnetic field and the linearity of the Hall resistance, V_G was tuned back and forth so that the Lifshitz transition was crossed multiple times. The SO coupling characteristic magnetic fields were extracted by fitting the weak antilocalization (WAL) behavior in the MR. We find that the maximum SO coupling effect occurs when E_F is near the Lifshitz point. We also find a single spin winding at the Fermi surface.

We use a Hall bar device with a width of $W = 150 \mu\text{m}$ and length of $L = 1000 \mu\text{m}$, as depicted in the inset of Fig. 1(c). First, a sputtered amorphous AlO_x hard mask in the form of a negative Hall bar geometry (thickness $\sim 15 \text{ nm}$) was fabricated on a TiO₂-terminated STO (001) substrate by photolithography. Then, 15 unit cells of LAO film were deposited at 800 °C in an Ar pressure of 0.04 mbar by 90° off-axis sputtering [25]. Finally, the sample was *in situ*

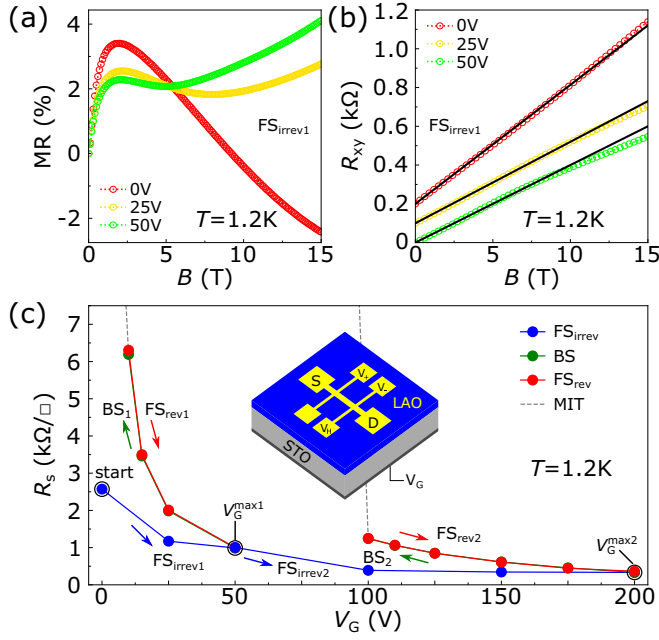


FIG. 1. (a) Magnetoresistance (MR) and (b) Hall resistance (R_{xy}) as a function of magnetic field (B) in the first irreversible forward sweep (FS_{irrev1}) at 1.2 K. $R_{xy}(B)$ curves are separated by an offset and the black lines are linear fits to them. (c) Sheet resistance (R_s) as a function of V_G at 1.2 K. FS_{irrev} , BS, and FS_{rev} stand for irreversible forward sweep, backward sweep, and reversible forward sweep, respectively. Two BSs were performed at 50 V (V_G^{max1}) and 200 V (V_G^{max2}). Note that BS and FS_{rev} overlap perfectly. Inset shows a schematic of the Hall bar device. Source and drain are labeled as S and D. The longitudinal resistance (R_{xx}) is measured between V_+ and V_- and the transverse resistance (R_{xy}) between V_H and V_- . V_G is applied between the back of the STO substrate and the drain.

annealed at 600 °C in 1 mbar of oxygen for 1 h. The backgate electrode was formed by uniformly applying a thin layer of silver paint (Ted Pella, Inc.) on the back of the substrate. The detailed device fabrication procedure is described in Ref. [24]. Magnetotransport measurements were performed in a cryostat with a base temperature of 1.2 K and a magnetic field of 15 T. The longitudinal resistance (R_{xx}) and transverse resistance (R_{xy}) were measured simultaneously using a standard lock-in technique ($f = 13.53$ Hz and $i_{RMS} = 1.0$ μ A). The maximum applied V_G was 200 V and the leakage current was less than 1.0 nA during the measurement.

The device was first cooled down to 1.2 K with V_G grounded. In the original state ($V_G = 0$ V), the observed maximum in MR [Fig. 1(a)] in low magnetic field is a sign of WAL. The negative MR in high magnetic field as well as the approximately linear $R_{xy}(B)$ [Fig. 1(b)] indicate the presence of only one type of carriers. Next, V_G was increased to add electrons to the QW and two characteristic Lifshitz transition features appeared at 25 V. They are the emergence of positive MR in high magnetic field and the change of linearity of $R_{xy}(B)$ [19,26]. V_G was further increased to 50 V (V_G^{max1}) to drive E_F slightly above the Lifshitz point, resulting in larger positive MR and more downward bending of $R_{xy}(B)$ in high magnetic field.

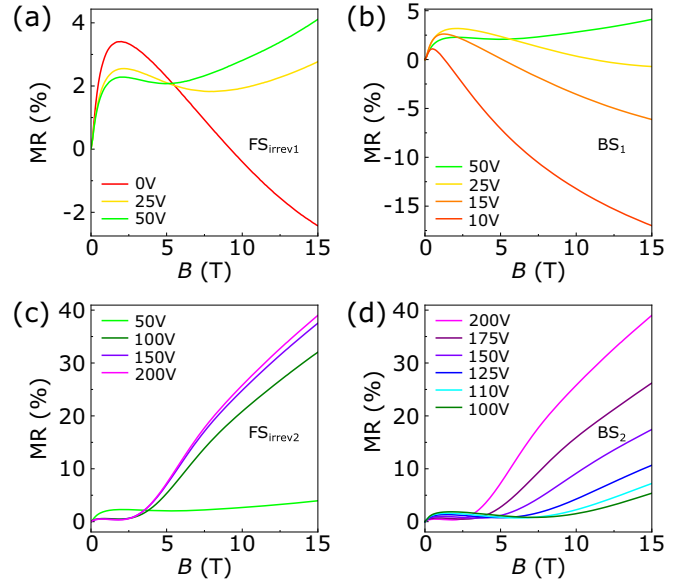


FIG. 2. Backgate tuning of MR in various regimes (a) FS_{irrev1} , (b) BS_1 , (c) FS_{irrev2} , and (d) BS_2 . Data for reversible forward sweeps are omitted since they show similar behaviors as backwards sweeps.

Then V_G was decreased to remove electrons from the QW in order to go back through the Lifshitz transition from the high-density direction. It has been shown that, due to the effect of electron trapping in STO, the R_s always follows an irreversible route when V_G is first swept forward and then backward [22,24,27]. Figure 1(c) shows R_s as a function of V_G . It can be seen that R_s increases above the virgin curve when V_G is swept backward. The backward sweep finally leads to a metal-insulator transition (MIT), whose onset was defined from the phase shift of the lock-in amplifier increasing above 15°. Sweeping V_G forward again results in a reversible decrease of R_s which overlaps with the previous backward sweep and the system is fully recovered when V_G is reapplied to 50 V. We therefore classify V_G sweeps into three regimes, namely, irreversible forward sweep (FS_{irrev}), backward sweep (BS), and reversible forward sweep (FS_{rev}). V_G was then increased to 200 V (V_G^{max2}) to drive E_F well above the Lifshitz point. Similar reversible behavior is observed in BS_2 and FS_{rev2} . Backgate tuning of MR in various regimes is shown in Fig. 2. Note, for instance, now the positive MR at 50 V reverts to the single-band negative MR at 10 V in the backward sweep regime BS_1 .

Figures 3(a)–3(h) show the fits to magnetotransport data with a two-band model [28]:

$$\sigma_{xx} = e \sum_{i=1,2} \frac{n_i \mu_i}{1 + (\mu_i B)^2}; \quad \sigma_{xy} = eB \sum_{i=1,2} \frac{n_i \mu_i^2}{1 + (\mu_i B)^2}, \quad (1)$$

where n_1 and n_2 are the carrier densities of the low mobility carriers and high mobility carriers, respectively, and μ_1 and μ_2 are the corresponding mobilities. For a reliable convergence n_2 and μ_2 are set to 0 in the one-band transport regime. The V_G dependence of the carrier densities and mobilities are presented in Figs. 3(i) and 3(j). The total carrier density (n_{tot}) is the sum of n_1 and n_2 . As shown in Fig. 3(i), the critical carrier density (n_{L-}) corresponding to the Lifshitz transition is 1.51×10^{13} cm^{-2} , which is close to earlier reported results

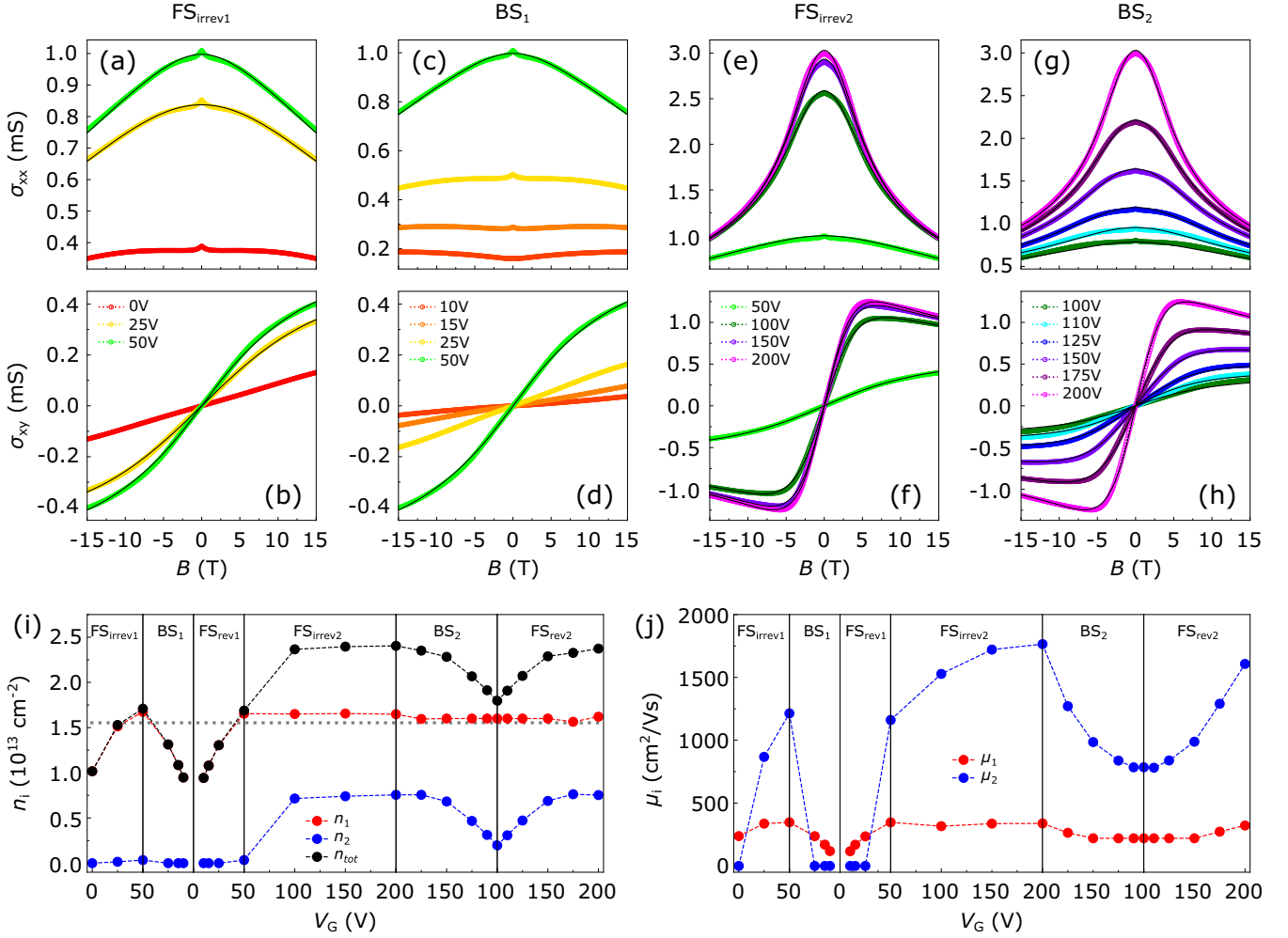


FIG. 3. (a)–(h) Two-band model fits of σ_{xx} and σ_{xy} in regimes FS_{irrev1} [(a) and (b)], BS₁ [(c) and (d)], FS_{irrev2} [(e) and (f)], and BS₂ [(g) and (h)]. The black lines are the fits. (i) V_G dependence of carrier densities. n_1 and n_2 stand for that of the low mobility carriers (LMC) and high mobility carriers (HMC), respectively. The total carrier density (n_{tot}) is the sum of n_1 and n_2 . The gray dashed line represents the critical carrier density ($n_L = 1.51 \times 10^{13} \text{ cm}^{-2}$) for Lifshitz transition. (j) V_G dependence of mobilities; that of the LMCs and HMCs are labeled as μ_1 and μ_2 , respectively.

[19,29]. The evolution of the carrier densities indicates that E_F approaches the Lifshitz point in regimes FS_{irrev1}, FS_{rev1}, and BS₂ and departs from the Lifshitz point in regimes BS₁, FS_{irrev2}, and FS_{rev2}. In Fig. 3(j), it can be seen that μ_1 almost stays unaffected above the Lifshitz transition, whereas μ_2 can be considerably changed by V_G , reaching $\sim 1800 \text{ cm}^2/\text{Vs}$ at 200 V. It should be mentioned that there is a slight curvature in R_{xy} around 5 T [hardly visible in Fig. 1(b)] which cannot be captured by the two-band model. The feature is more visible in the Hall coefficient ($R_H = R_{xy}/B$) plots where it appears as a maximum as shown in Figs. 4(a)–4(d), denoted with an arrow. A similar feature has also been reported by other groups [19,30], but its origin is still under debate. There are attempts to relate it to an unconventional anomalous Hall effect (AHE) [31] or hole transport [30], but we cannot get convincing fits using these models. In any case, we emphasize that the extraction of the parameters is not affected strongly by this feature.

In low-dimensional systems, the conductivity shows signatures of quantum interference between time-reversed

closed-loop electron trajectory pairs. In the presence of SO coupling the pairs interfere destructively, leading to a positive MR in low magnetic field which is known as the WAL [32]. For a system with Rashba-type of SO coupling, the spin relaxation is described by the D'yakonov-Perel' mechanism [33]. The model for analyzing the WAL was established by Iordanskii, Lyanda-Geller, and Pikus (ILP) [34]. In this model, both the single and triple spin winding contributions at the Fermi surface have been taken into account. It should be noted that the ILP model is an effective single-band model, which means that above the Lifshitz point the fitted characteristic magnetic field for SO coupling is an effective field for both the d_{xy} and $d_{xz,yz}$ bands. A model that considers multiband effects is not available yet. The WAL correction to the magnetoconductivity is given by [30,34]

$$\Delta\sigma(B) = -\frac{e^2}{2\pi h} \left[\mathcal{L}(B) - \mathcal{L}(0) + \psi\left(\frac{1}{2} + \frac{B_i}{B}\right) - \ln\left(\frac{B_i}{B}\right) \right], \quad (2)$$

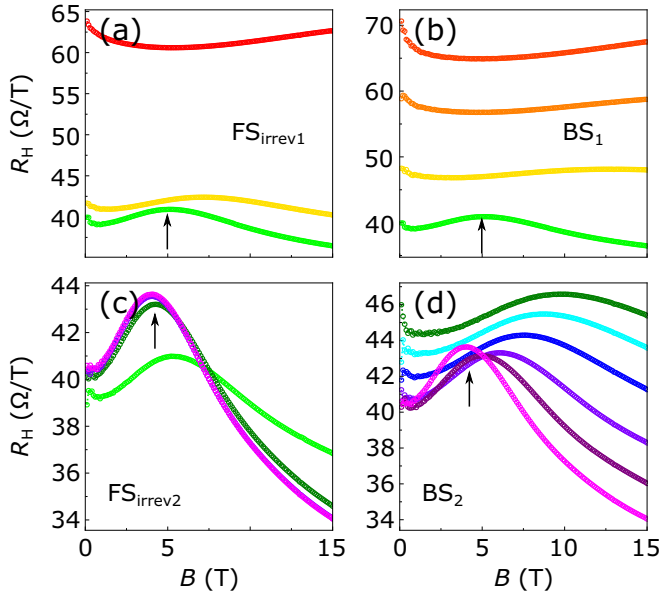


FIG. 4. Hall coefficient ($R_H = R_{xy}/B$) in regimes (a) FS_{irrev1} , (b) BS_1 , (c) FS_{irrev2} , and (d) BS_2 . The color scheme is the same as in Fig. 3. The arrows indicate the upturn in R_{xy} . Note the truncated scale for R_H .

$$\mathcal{L}(B) = \frac{1}{a_0} + \frac{2a_0 + 1 + \frac{B_{SO1} + B_{SO3}}{B}}{a_1 \left(a_0 + \frac{B_{SO1} + B_{SO3}}{B} \right) - 2 \frac{B_{SO1}}{B}} + \sum_{n=1}^{\infty} \frac{3a_n^2 + 2a_n \frac{B_{SO1} + B_{SO3}}{B} - 1 - 2(2n+1) \frac{B_{SO1}}{B}}{\left(a_n + \frac{B_{SO1} + B_{SO3}}{B} \right) a_{n-1} a_{n+1} - 2 \frac{B_{SO1}}{B} [(2n+1) a_n - 1]}, \quad (3)$$

where ψ is the digamma function, $a_n = n + 1/2 + (B_i + B_{SO1} + B_{SO3})/B$. The fitting parameters are the characteristic magnetic fields for the inelastic scattering $B_i = \hbar/4eD\tau_i$, and for the spin-orbit coupling $B_{SO_n} = (\hbar/4eD)2\Omega_n^2\tau_n$ ($n = 1$ or 3 for single or triple spin winding), where D is the diffusion constant, τ_i and τ_n are relaxation times, and Ω_n is the spin splitting coefficient.

Figures 5(a) and 5(b) depict WAL fits in the two FS_{irrev} and BS regimes. The solid black circles represent the local maxima of the MR curves. In principle, the SO coupling strength can be roughly estimated by the magnetic field (B_{max}) where the local maximum appears [12]. It can be clearly seen that B_{max} increases as E_F approaches the Lifshitz point (regimes FS_{irrev1} and BS_2), while B_{max} decreases as E_F departs from the Lifshitz point (regimes BS_1 and FS_{irrev2}). This already shows qualitatively that maximum spin-orbit coupling occurs when the Fermi energy is near the Lifshitz point. The fitted values for the characteristic magnetic fields are plotted in Fig. 5(c), where B_{SO} is the sum of B_{SO1} and B_{SO3} . In most cases B_{SO3} is much smaller than B_{SO1} , indicating a single spin winding at the Fermi surface. The maximum SO coupling strength occurs near the Lifshitz point, agreeing with the evolution of B_{max} . Driving E_F either above or below the Lifshitz point would lead to a decrease of the SO coupling strength. B_i increases when the carrier density is lowered, which is due to more accessible phonons contributing to the scattering process, and vice versa.

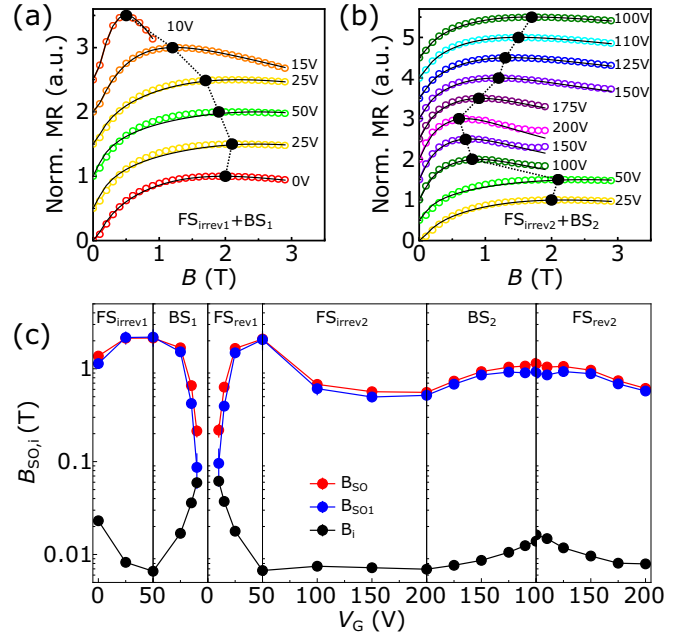


FIG. 5. (a), (b) Weak antilocalization (WAL) analysis in regimes (a) FS_{irrev1} and BS_1 and (b) FS_{irrev2} and BS_2 . The solid circles correspond to experimental data and the black lines to fits using the ILP model. The local maximum of each MR curve is plotted black. The MR curves are normalized to the local maxima and separated by an offset of 0.5. The black dashed line is a guide to the eye for the evolution of the local maxima. (c) Fitted characteristic magnetic fields as a function of V_G . SO field B_{SO} is the sum of B_{SO1} (single spin winding) and B_{SO3} (triple spin winding). B_i is the inelastic scattering field.

If B_{SO1} is 0 and only B_{SO3} is present, the ILP formula could be reduced to a simpler model developed by Hikami, Larkin, and Nagaoka (HLN) [35], in which the spin relaxation is described by the Elliot-Yafet mechanism [36,37]. However, the HLN model yields inaccurate fits to our data, which is different from earlier reported results [12,38], where a triple spin winding has been found.

Our results manifest the nontrivial SO coupling mechanism at the LAO/STO interface predicted by theoretical works [15,17]. Applying an external electric field can tune the SO coupling, but its direct contribution is rather small. According to the Rashba theory for a free electron system, a typical electric field in experiments, e.g., 100 V, only yields a spin splitting of $\sim 10^{-8}$ meV [15], which is much smaller than the measured values that are of the order of meV [11]. Instead the electric-field effect is indirect. It is the tuning of carrier densities and therefore band filling that significantly influence the SO coupling. Our results, therefore, help to clarify the conflicting results reported in Refs. [10,11]. The reason is that the experiments were carried out in different transport regimes, namely, Ref. [10] in the two-band regime (i.e., above the Lifshitz point) and Ref. [11] in the one-band regime (i.e., below the Lifshitz point). It is also worth mentioning that the mobile electrons usually are distributed over a range of ~ 10 nm from the interface [24,28,39]. Therefore the local electric field experienced by electrons at different depths varies considerably. However, also this variation has a minor effect on the SO coupling compared with the substantial contribution from the coupling of the d_{xy} and $d_{xz,yz}$ orbitals.

In summary, we have performed magnetotransport experiments to study the Rashba SO coupling effect in backgated LAO/STO. By tuning the gate voltage, the Fermi energy has been driven to approach or depart from the Lifshitz point multiple times. We have done WAL analysis using the ILP model, which reveals a single spin winding at the Fermi surface. We have found that the maximum SO coupling occurs when the Fermi energy is near the Lifshitz point. Driving the Fermi energy above or below the Lifshitz point would result in a decrease of the coupling strength. Our findings provide valuable insights to the investigation and design of oxide-based spintronic devices.

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