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## Optimally weighted ensembles of surrogate models for sequential parameter optimization

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# Optimally weighted ensembles of surrogate models for sequential parameter optimization

Martina Echtenbruck



# Optimally weighted ensembles of surrogate models for sequential parameter optimization

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