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## Algebraic filters for filtered backprojection

Plantagie, L.

### Citation

Plantagie, L. (2017, April 13). *Algebraic filters for filtered backprojection*. Retrieved from <https://hdl.handle.net/1887/48289>

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**Author:** Plantagie, L.

**Title:** Algebraic filters for filtered backprojection

**Issue Date:** 2017-04-13

# **ALGEBRAIC FILTERS FOR FILTERED BACKPROJECTION**

Proefschrift

ter verkrijging van  
de graad van Doctor aan de Universiteit Leiden,  
op gezag van Rector Magnificus prof.mr. C.J.J.M. Stolker,  
volgens besluit van het College voor Promoties  
te verdedigen op donderdag 13 april 2017  
klokke 13:45 uur

door

Linda Plantagie

geboren te Nieuwegein  
in 1986

Promotor: Prof. dr. Kees Joost Batenburg

Samenstelling van de promotiecommissie:

Voorzitter: Prof. dr. A. W. van der Vaart

Secretaris: Prof. dr. B. de Smit

Overige leden: Prof. dr. R. H. Bisseling (Universiteit Utrecht)  
Prof. dr. J. Sijbers (Universiteit Antwerpen)  
Dr. E. Van de Castele (AZ Monica, Antwerpen)

## **ALGEBRAIC FILTERS FOR FILTERED BACKPROJECTION**

ISBN: 978-94-6299-548-2

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Cover design by Ridderprint BV, Ridderkerk  
Printed by Ridderprint BV, Ridderkerk

The research in this thesis has been financially supported by the  
Netherlands Organisation for Scientific Research (NWO), project  
639.072.005.

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