



Universiteit  
Leiden  
The Netherlands

## Non-decoupling of heavy scalars in cosmology

Hardeman, A.R.

### Citation

Hardeman, A. R. (2012, June 8). *Non-decoupling of heavy scalars in cosmology*. Casimir PhD Series. Retrieved from <https://hdl.handle.net/1887/19062>

Version: Corrected Publisher's Version

License: [Licence agreement concerning inclusion of doctoral thesis in the Institutional Repository of the University of Leiden](#)

Downloaded from: <https://hdl.handle.net/1887/19062>

**Note:** To cite this publication please use the final published version (if applicable).

Cover Page



Universiteit Leiden



The handle <http://hdl.handle.net/1887/19062> holds various files of this Leiden University dissertation.

**Author:** Hardeman, Sjoerd Reimer

**Title:** Non-decoupling of heavy scalars in cosmology

Date: 2012-06-08

# **Non-decoupling of heavy scalars in cosmology**

## **P R O E F S C H R I F T**

ter verkrijging van  
de graad van Doctor aan de Universiteit Leiden,  
op gezag van Rector Magnificus prof. mr P. F. van der Heijden,  
volgens besluit van het College voor Promoties  
te verdedigen op vrijdag 8 juni 2012  
klokke 12:00

door

**Sjoerd Reimer Hardeman**

geboren te Hengelo (Overijssel), Nederland in 1982

## **Promotiecommissie**

Promotor: prof. dr. A. Achúcarro  
Co-Promotor: dr. K. E. Schalm  
Overige leden: prof. dr. J. W. van Holten  
dr. D. Roest  
prof. dr. J. M. van Ruitenbeek  
dr. B. J. W. van Tent

Casimir PhD Series, Delft-Leiden, 2011-3  
ISBN 978-90-8593-092-1

The background image is the Hubble ultra deep field, an image of an estimated 10,000 galaxies in the constellation Fornax. These galaxies were formed from the density perturbations that were created during inflation and are best studied from the cosmic microwave background radiation. The image of this radiation is used as a background for the letters on the cover. Finally, a curved inflaton trajectory is depicted, which will make features in the power spectrum that might be possible to study using late time cosmology.

‘Lieve hart mijn boek is af, mijn boek is af!’ - Multatuli



---

# Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	The standard model of cosmology . . . . .	1
1.2	The inflationary paradigm . . . . .	5
1.2.1	Slow-roll inflation . . . . .	7
1.2.2	The power spectrum . . . . .	9
1.2.3	Nongaussianities . . . . .	13
1.3	Heavy physics and inflation . . . . .	14
1.3.1	String theory and inflation . . . . .	14
1.3.2	Supergravity and effective field theory . . . . .	16
<b>2</b>	<b>Consistent decoupling of heavy scalars and <math>\mathcal{N}=1</math> supergravity</b>	<b>23</b>
2.1	Consistent decoupling of scalar fields in $\mathcal{N}=1$ supergravity . . . . .	24
2.2	Analysis of the consistency conditions . . . . .	26
2.3	Consistent decoupling compared to gravitational coupling in rigid supersymmetry . . . . .	28
2.4	Discussion . . . . .	29
<b>3</b>	<b><math>F</math>-term uplifting and the supersymmetric integration of heavy scalars</b>	<b>33</b>
3.1	Introduction . . . . .	33
3.2	$F$ -term uplifting and integrating out heavy scalars . . . . .	37
3.3	Stability of supersymmetric critical points . . . . .	40
3.3.1	Analysis of the Kähler function . . . . .	40
3.3.2	Analysis of the scalar potential with vanishing $D$ -terms . . . . .	42
3.3.3	Analysis of the scalar potential with non-vanishing $D$ -terms . . . . .	44
3.4	Stability of uplifted vacua . . . . .	47
3.4.1	Stability of uplifted vacua with zero $D$ -term potential . . . . .	47

## CONTENTS

---

3.4.2	Stability of uplifted vacua with a non-zero $D$ -term potential . . . . .	50
3.5	More general couplings . . . . .	51
3.6	Summary and Conclusions . . . . .	54
<b>4</b>	<b>Heavy physics in the Cosmic Microwave Background</b>	<b>57</b>
4.1	Introduction . . . . .	57
4.2	Basic considerations . . . . .	61
4.2.1	Background solution . . . . .	62
4.3	Perturbation theory . . . . .	67
4.3.1	Canonical frame . . . . .	70
4.3.2	Quantisation and initial conditions . . . . .	71
4.3.3	Two-point correlation function . . . . .	74
4.4	Applications in Minkowski space . . . . .	75
4.4.1	Dynamics in the presence of mass hierarchies . . . . .	75
4.4.2	Two-field models . . . . .	77
4.4.3	Constant radius of curvature . . . . .	79
4.4.4	Low energy effective theory . . . . .	81
4.5	Discussion . . . . .	82
4.5.1	Inflation . . . . .	83
4.5.2	Decoupling of light and heavy modes in supergravity . . . . .	84
4.5.3	Consistent decoupling and autoparallel trajectories . . . . .	86
<b>5</b>	<b>Two-field models of inflation</b>	<b>87</b>
5.1	Introduction . . . . .	87
5.2	Inflationary models with two scalar fields . . . . .	88
5.2.1	Power spectrum . . . . .	91
5.2.2	Effective Theory . . . . .	92
5.3	Slow-roll inflation in two-field models . . . . .	94
5.3.1	Slow-roll parameters . . . . .	94
5.3.2	Perpendicular dynamics . . . . .	96
5.3.3	Equations of motion in the slow-roll regime . . . . .	97
5.3.4	Effective theory for the adiabatic mode . . . . .	97
5.4	Features in the power spectrum . . . . .	99
5.4.1	Constant radius of curvature . . . . .	100
5.4.2	Single turn in the trajectory . . . . .	101
5.4.3	A specific example . . . . .	104
5.4.4	Enhancement of nongaussianity . . . . .	106
5.5	Conclusions . . . . .	108

<b>6 Conclusions</b>	<b>111</b>
<b>A Commutation relations for quantum multi-fields</b>	<b>115</b>
<b>B Zeroth-order theory of the background fields</b>	<b>119</b>
<b>Samenvatting</b>	<b>141</b>
<b>Summary</b>	<b>151</b>
<b>Dankwoord</b>	<b>161</b>
<b>List of publications</b>	<b>163</b>
<b>Curriculum Vitae</b>	<b>165</b>

