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Prediction accuracy and stability of regression with optimal scaling transformations

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Citation

Kooij, A. J. van der. (2007, June 27). *Prediction accuracy and stability of regression with optimal scaling transformations*. Leiden. Retrieved from <https://hdl.handle.net/1887/12096>

Version: Corrected Publisher's Version

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Note: To cite this publication please use the final published version (if applicable).

Prediction Accuracy and Stability
of Regression with
Optimal Scaling Transformations

Van der Kooij, Anita Jolande,
Prediction Accuracy and Stability of Regression with Optimal Scaling
Transformations.
Dissertation Leiden University — With ref. — With Summary in Dutch.
Subject headings: nonlinear regression; CATREG; optimal scaling;
transformations; local minima; prediction accuracy; regularization;
.632 Bootstrap; Ridge regression; Lasso; Elastic Net

ISBN 978-90-9021936-3

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Printed by Mostert en van Onderen, Leiden

Prediction Accuracy and Stability of
Regression with Optimal Scaling
Transformations

Proefschrift
ter verkrijging van
de graad van Doctor aan de Universiteit Leiden,
op gezag van de Rector Magnificus prof.mr. P.F. van der Heijden,
volgens besluit van het College voor Promoties
te verdedigen op woensdag 27 juni 2007
klokke 16.15 uur
door
Anita J. van der Kooij
geboren te Boskoop
in 1961

PROMOTIECOMMISSIE

Promotor	Prof. dr. J.J. Meulman
Referent	Prof. J.H. Friedman, Ph.D., Stanford University, USA
Overige Leden	Prof. dr. W.J. Heiser Prof. dr. M.H. van IJzendoorn Dr. ing. P.H.C. Eilers Prof. dr. R.D. Gill

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