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# **Efficient Multiple Testing for Large Structured Problems**

Rosa Janna Meijer

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# Efficient Multiple Testing for Large Structured Problems

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# Table of Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
1.1	Introduction . . . . .	1
1.2	Hypothesis Testing . . . . .	2
1.2.1	Type of test . . . . .	2
1.2.2	Multiple Testing . . . . .	4
1.3	Prediction modeling . . . . .	5
1.3.1	Type of model . . . . .	6
1.3.2	Predictive performance . . . . .	7
1.4	Computational feasibility . . . . .	8
1.5	Outline of the thesis . . . . .	9
<b>2</b>	<b>Extending Hommel's procedure</b>	<b>13</b>
2.1	Introduction . . . . .	14
2.2	Hommel's procedure . . . . .	15
2.3	More efficient implementation of Hommel's procedure . . . . .	18
2.4	Confidence Sets . . . . .	20
2.4.1	Determining whether an hypothesis can be rejected by the closed testing procedure in an efficient way . . . . .	22
2.4.2	Algorithm . . . . .	26
2.5	Application . . . . .	28
2.6	Discussion . . . . .	33
<b>3</b>	<b>A region-based multiple testing method</b>	<b>35</b>
3.1	Introduction . . . . .	36
3.2	Region hypotheses . . . . .	37
3.2.1	A FWER controlling multiple testing procedure, based on the sequential rejection principle . . . . .	39
3.2.2	Confidence sets for the number of true rejections in regions chosen post-hoc . . . . .	44
3.2.3	A weighted-version of the region-method . . . . .	45
3.3	Algorithms . . . . .	46
3.3.1	Dynamic programming algorithm to calculate ratios . . . . .	47
3.3.2	Complexity . . . . .	48

3.3.3	Confidence statements . . . . .	51
3.4	Applications . . . . .	51
3.5	Discussion . . . . .	57
3.6	Appendix . . . . .	58
<b>4</b>	<b>A multiple testing method for DAGs</b>	<b>61</b>
4.1	Introduction . . . . .	62
4.2	The method . . . . .	63
4.2.1	Sequential rejection principle . . . . .	65
4.2.2	Testing procedure for DAGs with one-way logical relationships . . . . .	67
4.2.3	Using two-way logical relationships: a more powerful procedure . . . . .	70
4.2.4	Confidence sets for the number of true findings in sets chosen post-hoc . . . . .	73
4.3	Algorithms . . . . .	74
4.3.1	Maximizing the denominator . . . . .	75
4.3.2	Constructing confidence sets . . . . .	77
4.4	Applications . . . . .	77
4.4.1	Comparison of the approaches that can be used when two-way logical relationships are present . . . . .	78
4.4.2	Comparing the any-parent and all-parents rule to existing FWER controlling methods . . . . .	80
4.4.3	A simulation study to further explore the method's behavior . . . . .	82
4.5	Discussion . . . . .	85
<b>5</b>	<b>Multiple testing of gene sets from GO</b>	<b>89</b>
5.1	Introduction . . . . .	90
5.2	Structure of gene sets . . . . .	91
5.3	Appropriate multiple testing procedures . . . . .	94
5.4	More powerful FWER controlling methods . . . . .	98
5.5	Discussion . . . . .	103
<b>6</b>	<b>Finding important variables in high-dimensional data</b>	<b>107</b>
6.1	Introduction . . . . .	107
6.2	Selecting variables by fitting a prediction model . . . . .	108
6.2.1	Screening by penalized methods . . . . .	109
6.2.2	Screening by univariate selection . . . . .	113
6.2.3	Practical usefulness of methods possessing screening properties . . . . .	114
6.2.4	The Van de Vijver data set . . . . .	116
6.3	Selecting variables by testing individual covariates . . . . .	118
6.3.1	Methods for FWER control . . . . .	121
6.3.2	Methods for FDR control . . . . .	124
6.3.3	Confidence intervals for the number of true discoveries . . . . .	126

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6.4	Reducing the number of variables beforehand and incorporating back-ground knowledge . . . . .	128
6.5	Discussion . . . . .	129
<b>7</b>	<b>Efficient approximate cross-validation</b>	<b>131</b>
7.1	Introduction . . . . .	132
7.2	Approximation procedure . . . . .	133
7.2.1	Generalized linear models . . . . .	134
7.2.2	Cox' proportional hazards model . . . . .	138
7.3	Results . . . . .	140
7.3.1	Measure of predictive performance: the cross-validated log-likelihood . . . . .	141
7.3.2	Data sets . . . . .	141
7.3.3	Ridge regression . . . . .	141
7.3.4	Influence of $n$ , $k$ and $\lambda$ on the accuracy of the approximations . . . . .	144
7.3.5	Computation Time . . . . .	145
7.4	Discussion . . . . .	147
	<b>Bibliography</b>	<b>149</b>
	<b>List of Publications</b>	<b>157</b>
	<b>Samenvatting</b>	<b>159</b>
	<b>Dankwoord</b>	<b>165</b>
	<b>Curriculum Vitae</b>	<b>167</b>



