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**Proximity effects in superconducting spin-valve structures**  
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## Chapter 4

### Superconducting spin-valve: weak ferromagnetic case

## 4.1 Introduction

A superconductor (S) and a ferromagnet (F) both show a mean-field order for the electron spin. In the ferromagnet the ordering is in real-space and the exchange field ( $H_{\text{ex}}$ ) (or exchange energy  $E_{\text{ex}}$ ) favors one spin direction, while in the superconductor the ordering is in k-space and the order parameter ( $\Delta$ ) is built up from Cooper pairs consisting of electrons with opposite spins. Bringing these antagonistic types of order into close proximity leads to a complex interplay with new possible ground states, and possible consequences for the superconductivity as well as for the magnetism [41, 42, 31]. The foremost characteristics of the S/F proximity effect in the case of homogeneous  $H_{\text{ex}}$  are the oscillatory decay of the induced order parameter in the F metal and the emergence of spin triplet correlations. In special cases this could enable the formation of the spin equal (long range) components of the triplet, in particular for inhomogeneous exchange fields [39] or halfmetallic ferromagnets [43]. The oscillatory order parameter brings about an oscillation of the superconducting transition temperature  $T_c$  as function of the F layer thickness, which has been observed in various experiments [44, 45]. This phenomenon is reasonably well understood and described by theoretical models. As for the existence of long range triplet components, two experiments has been reported thus far [29, 30], but their existence is not yet fully accepted.

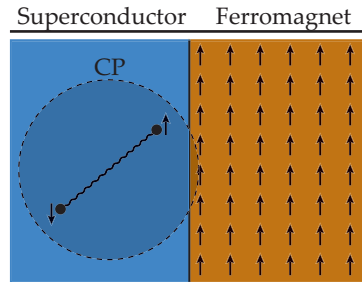


Figure 4.1: Spin ordering of the two electrons of a Cooper pair (CP) in the superconductor, and of the lattice points in the ferromagnet.

Two main consequences of the interplay between magnetism and superconductivity are the S/F/S  $\pi$ -junction, and the F/S/F superconducting spin-valve. In the  $\pi$ -junction the order parameter oscillation in the F metal yields a phase change of  $\pi$  between the superconducting banks, which was demonstrated to exist both by transport experiments [46] and in measurements of the density of states on the F-side of and S/F sandwich [47]. The spin-valve exhibits (in theory) re-entrant superconductivity by switching the magnetization of the F banks from parallel (P) to anti-parallel (AP), which would lead to a controllable supercurrent through a small field manipulation [9, 10]. Theory describing both phenomena is well developed for the case of weak ferromagnetism with homogeneous exchange fields, as then the quasiclassical

Green functions adequately describe the transport probability of electrons and Cooper pairs. However, inhomogeneities in  $H_{\text{ex}}$ , in particular from domains or domain walls, still pose difficulties for both experiment and theory. Moreover, for ferromagnets with strong exchange fields, where  $E_{\text{ex}}$  is no longer much smaller than the Fermi energy  $E_F$ , or with non-zero polarization of the electronic spin bands, the current framework is not suitable as it does not incorporate these effects. For the case of the spin-valve effect, which is strongest close to  $T_c$  where superconductivity is still weakly developed, magnetic domains could also have a significant effect on the superconducting gap and thus on the working of the superconducting spin-valve. This is the issue we address in this and the following chapter, where here we deal with weak ferromagnetism and in the next chapter with strong ferromagnetism.

## 4.2 The superconducting spin-valve

The conventional superconducting spin-valve structure is a system where two ferromagnetic layers are separated by a superconducting spacer. It was first proposed by Tagirov [9] (and similarly by Buzdin and co-workers [10]) who calculated, using linearized Usadel equations, the superconducting transition temperature of the S-layer as function of F-layer thickness, for both the parallel (P) and antiparallel (AP) direction of exchange fields. It was shown that for weak ferromagnets,  $T_c$  for the anti-parallel configuration is always higher than for the parallel case, where a weak ferromagnet really means a ferromagnet with  $E_{\text{ex}} \ll E_F$  and a polarization close to zero. This change in  $T_c$  becomes more interesting when the thickness of the F layers becomes of the order of the coherence length in F, since there exist a (small) thickness range of the F layers where it should be possible to fully suppress superconductivity in the parallel configuration, while having a finite  $T_c$  in the anti-parallel configuration. It should thus be possible to switch between the normal and superconducting state, and hence "valving" a supercurrent, if the direction of the exchange fields can be controlled. The spin-valve can only work if there is a coupling between the two F layers which additionally couples to the order parameter, since it is the order parameter which should differentiate between a parallel or anti-parallel alignment. This coupling is provided by Cooper pairs and therefore the thickness of the S layer should be limited to several times the superconducting coherence length. When this condition is met, Cooper pairs in the superconductor can touch both the F layers (i.e. one of the electrons is "close" to one of the F layers, and the other electron is "close" to the other F layer). Due to the non-local nature of the Cooper pairs (and the Andreev reflection process), the Cooper pair can leave the superconductor such that

the two electrons enter a different F layer. In the anti-parallel alignment of the direction of exchange fields, the two electrons enter identical spin bands. However, this is not true for the parallel alignment. In that case, there is a potential difference between the electrons which is balanced by a difference in kinetic energy (just as for the standard S/F proximity). This kinetic momentum difference leads to additional dephasing of the induced "pair", which in turn results into a lowering of the Cooper pair density. The final result is thus an additional lowering of  $T_c$  in case of parallel alignment. This mechanism of the (weak-limit) spin-valve is illustrated in Fig. 4.2. Dipolar fields were not taken into account in theoretical model, and thus an argument of the kind "In an anti-parallel alignment the dipolar fields create a more natural environment compared to the parallel alignment" to explain the  $T_c$  difference is, although correct, not what the weak-limit models are about. When the thickness of

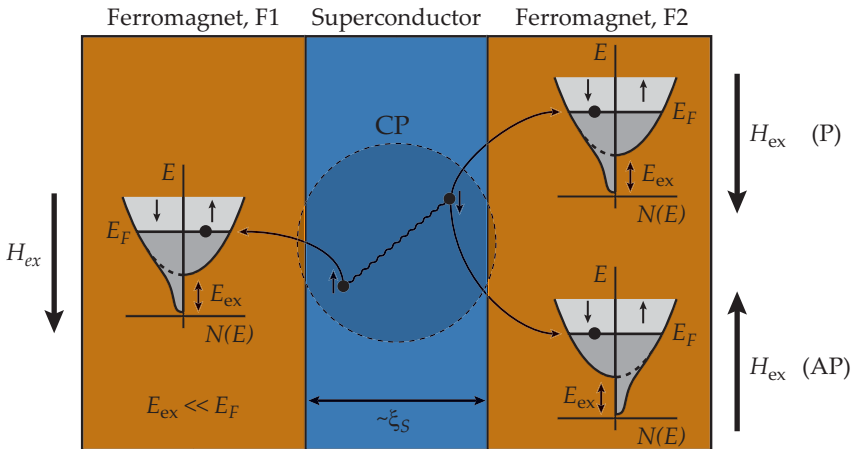


Figure 4.2: Comparing the parallel (P) and anti-parallel (AP) configuration of the ferromagnetic exchange fields  $H_{ex}$  in a superconducting spin-valve. Here, a Cooper pair (CP) couples the two ferromagnetic layers F1 and F2, with  $\xi_S$  the superconducting coherence length. In F1 the orientation of  $H_{ex}$  is "down" while in F2 the orientation is either "up" (AP configuration) or "down" (P configuration). The presented electron band structures are impressions of how a weak ferromagnet is treated in the theoretical framework: as a normal metal with identical spin bands near the Fermi energy  $E_F$  (and thus no spin polarization) and a weak exchange field  $E_{ex} \ll E_F$ , making the distortion to the spin bands very small

the F layer becomes of the order of the coherence length in the ferromagnet ( $\xi_F$ ), the induced oscillating order parameter in F reaches its outer boundary. This results in a back-reflection of the oscillation and causes self-interference. This is the origin of the minimum in Fig. 1.4, and thus of the re-entrance effect.

By now, various spin-valve systems has been measured. A number of them have Nb as superconductor in combination with weakly magnetic CuNi [48, 49] or stronger magnets such as Ni [50], Ni<sub>80</sub>Fe<sub>20</sub> (Permalloy, Py) [51, 52, 53], Co and Fe combined [54] or Co [55]. Moreover, the systems do not only differ in type of magnet, also the method to obtain switching is different. Some use a spin-valve stack with antiferromagnetic Fe<sub>50</sub>Mn<sub>50</sub> adjacent to one of the F layers in order to pin its magnetization, while the magnetization of the other layer can rotate freely. This is the case in the reports on Nb/CuNi [48, 49], Nb/Ni [50], Nb/Py [52]. The other experiments rely on the difference in thickness of the F layers in order to obtain different coercive fields, as in the reports on Nb/Py [51, 53], Nb/(Co,Fe) [54] and Nb/Co [55]. The experiments using a pinning layer confirm the general prediction for the superconducting spin-valve: in the P alignment of the two F layers, the transition temperature  $T_c^P$  is slightly lower than  $T_c^{AP}$  in the AP alignment. The experiments without pinning layer report the reverse behavior, with strong indications that now stray fields and magnetic coupling of the F layers play a role. Taken together, the literature data seem to suggest that the presence of the pinning layer makes a distinction in the outcome of the experiments by suppressing secondary stray field effects originating from local inhomogeneities (like domain walls). We are not aware that this observation has been made before, but it makes it possible to understand all the different reports in a unified way. There is, however, another issue which has not been fully resolved: the size of the apparent spin-valve effects are small compared to theoretical predictions. Changes in  $T_c$  are mostly less than 10 mK, and in bilayer experiments involving Py it was demonstrated that the relative enhancement of superconductivity over domains walls resulted in a similar-sized increase in  $T_c$  [56]. For the weak ferromagnets such as Cu<sub>1-x</sub>Ni<sub>x</sub> (with x in the range 0.5 - 0.6), which played such an important role both in demonstrating  $\pi$ -junctions and (apparent) spin switching, it was not yet investigated whether domains in the F layer can enhance superconductivity in a similar way. In this chapter, we report on a study of Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayers and trilayers where we compare anisotropic magnetoresistance (AMR) effects in the normal state with the magnetoresistance in the superconducting transition and measurements of the depairing (critical) current  $I_{dp}$  below  $T_c$ , both for microstructured and large-scale samples. We show that in bilayers enhanced superconductivity is indeed found when the F-layer is in a domain state. In the transition this is seen as a decrease in resistance in the field range where domains occur according to AMR. Below the transition it is seen as a maximum in  $I_{dp}$  as function of the in-plane magnetic field. Interestingly, the maximum occurs at significantly higher field values than where the domain

state occurs above or in the transition, suggesting that the well-developed superconductivity now influences the mechanism of magnetization rotation in the F layer. Finally, in trilayers we basically make the same observations. A domain-state dominated mechanism for spin-valve effects therefore cannot be ruled out.

### 4.3 Sample details

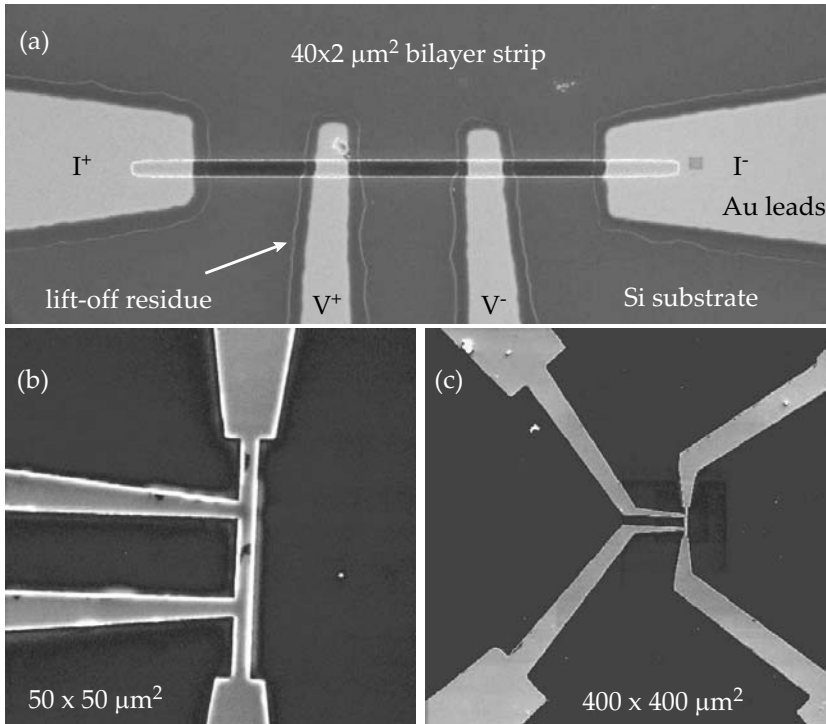


Figure 4.3: SEM images of  $40 \times 2 \mu\text{m}^2$  bilayer devices (a) standard 4-probe device, (b) contact included device and (c) bonding pads and leads. In (a), the bright colored Au leads were deposited using a lift-off mask technique, leaving typical Au residues. The geometry of (c) is used for all devices.

Nb/Cu<sub>43</sub>Ni<sub>57</sub> layers were grown onto Si(100) substrates by DC magnetron sputtering in a ultra high vacuum chamber with a background pressure of  $10^{-9}$  mbar and an Ar pressure of  $4 \mu\text{bar}$  with Nb as bottom layer (see Ch. 3.1 for additional details). The Cu<sub>43</sub>Ni<sub>57</sub> thickness was kept at 10 nm for all samples, while the Nb layers are 20 nm for the bilayers, and 25 nm for the trilayers.

Also all devices have an additional Nb capping layer (of 1-2 nm thick) on top of the  $\text{Cu}_{43}\text{Ni}_{57}$  top layer. The ratio Cu/Ni in the target is 50/50 (atomic percentage), which results in an approximate 43/57 ratio at the sample. The Curie temperature of the  $\text{Cu}_{43}\text{Ni}_{57}$  is around 150 K, and it has a degree of polarization close to zero (making it a model weak ferromagnet). The purity of the Nb target is 99.95% which yields a  $T_c$  of 9.1-9.2 K. Different samples were used for different bridge widths, although sometimes two bridges were patterned and measured on the same sample. Standard electron beam lithography was used to pattern micro-sized strips with a length of 40  $\mu\text{m}$  and a width ranging from 1 to 4  $\mu\text{m}$ . These strips were etched with Ar ion-etching (at 2.5  $\mu\text{bar}$  Ar pressure) in a background pressure of  $10^{-6}$  mbar. Au contacts were sputtered in a second deposition step using a lift-off resist-mask technique, with a few monolayers of Ti used as an adhesion layer for the Au. The contact geometry is 4-probe with 10  $\mu\text{m}$  spacing between the voltage probes. Fig. 4.3a shows SEM (scanning electron microscope) images of  $40 \times 2 \mu\text{m}^2$  bilayer strips. The contour lines surrounding the high contrast Au leads are Au lift-off residues. Trilayers and macroscopic sized samples were made using the same recipe, where for the latter the strip dimensions are  $2000 \times 200 \mu\text{m}^2$  with 1000  $\mu\text{m}$  spacing between the voltage probes. The superconducting transition temperature for the bilayer samples, measured after structuring was 6.5 K, except for the  $40 \times 1$  sample where it was 7.5 K, probably due to a slightly thicker Nb layer. For the trilayers it was 5.9 K. The thickness dependence of  $T_c$  for plain Nb films and for Nb/F and F/Nb/F are presented in earlier works [57, 58]. The two-step process in order to make separate electrical Au contacts to the strips, rather than etch out a full geometry including contacts, is crucial for the experiments, since otherwise the influence of the (magnetic) contact areas can be significant as we show in Ch. 4.5. For those devices with 'contacts included', strips including leads to the bonding pads are all etched down during one step of Ar ion-etching.

The micron sized lateral dimensions bring along two main advantages: it promotes probing states with only few domains, avoiding a large spaghetti of domain states, and the resistance c.q. the cross-section is sufficiently high for anisotropic magnetoresistance (AMR) measurements and critical current ( $I_c$ ) measurements. The AMR measurements play a key role in our experiments since they allow to determine if and when domains appear in the ferromagnet just above  $T_c$ . This can then be compared to the response of the superconductor to an applied field in and below the transition. Resistance measurements were done in a standard  $^4\text{He}$  cryostat with magnetic shielding to provide a low-noise environment, and a superconducting coil to provide the magnetic field



(ranging up to 1 T). All field measurements are performed with the externally applied field directed along the strips, which implies the current is parallel to field. For CuNi this should result in a resistance *decrease* when domains are being formed in a initially homogeneous state, similar to the behavior of the elemental transition metals Fe, Co and Ni. At temperatures well below  $T_c$  we performed  $I_c$  measurements, which probe the gap amplitude in the superconductor. The method for such measurements makes use of pulsed currents, and was described in Ref. [59].

## 4.4 Results

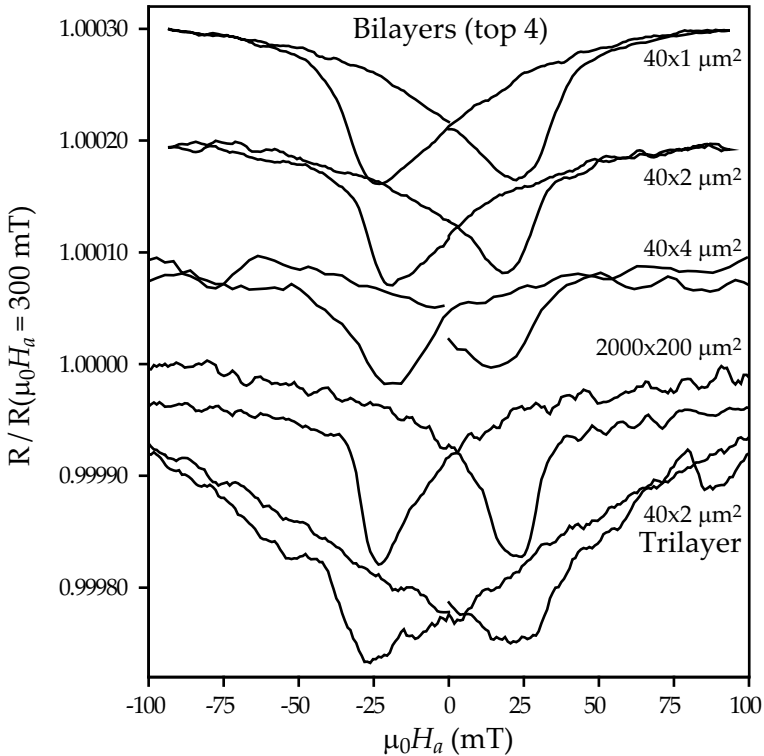


Figure 4.4: Resistance normalized to the value at 300 mT as function of an in-plane applied field  $H_a$  on Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strips of  $40 \times 1$ ,  $40 \times 2$ ,  $40 \times 4$  and  $2000 \times 200 \mu\text{m}^2$ . Temperatures were in a range between 7.5 K and 9 K for the different datasets. The curves are shifted for clarity, each with a value of  $1 \times 10^{-4}$  with respect to the one below. Also shown are data on a  $40 \times 2 \mu\text{m}^2$  Cu<sub>43</sub>Ni<sub>57</sub>/Nb/Cu<sub>43</sub>Ni<sub>57</sub> trilayer strip (all with Nb in normal state); these data are not shifted.

Data were obtained for samples with different bridge widths, as well for temperatures above and below  $T_c$ , and we present them in the following way. We first give a brief overview of the behavior of the different samples. We then concentrate on the  $40 \times 2 \mu\text{m}^2$  bilayer strip, which best illustrates most of the physics, before coming back to the samples with different bridge widths. The results of the field-dependent resistance measurements  $R(H)$  at a temperature just above  $T_c$  are presented in Fig. 4.4 for bilayer strips with a width of  $1 \mu\text{m}$ ,  $2 \mu\text{m}$  and  $4 \mu\text{m}$ , as well as for the large bilayer structure ( $2000 \times 200 \mu\text{m}^2$ ), and for a  $40 \times 2 \mu\text{m}^2$  trilayer strip. The resistance values are normalized to the value measured at 300 mT. The data clearly show hysteresis and resistance dips. The relative resistance change is of order  $10^{-4}$  and the minimum of the dips is close to a field of  $\pm 22$  mT. This field we call the dip-field  $H_{\text{dip},n}$  (n meaning the normal state) and is generally taken as the coercive field of the ferromagnetic layers. The width of the hysteretic parts is about 50 mT. All bridges show similar values for  $H_{\text{dip},n}$  and the hysteretic width, and they lead to the conclusion that domains are forming in all our ferromagnetic layers, despite the parallel field alignment and narrow strips with high aspect ratio.

#### 4.4.1 Results on the $2 \mu\text{m}$ bridge

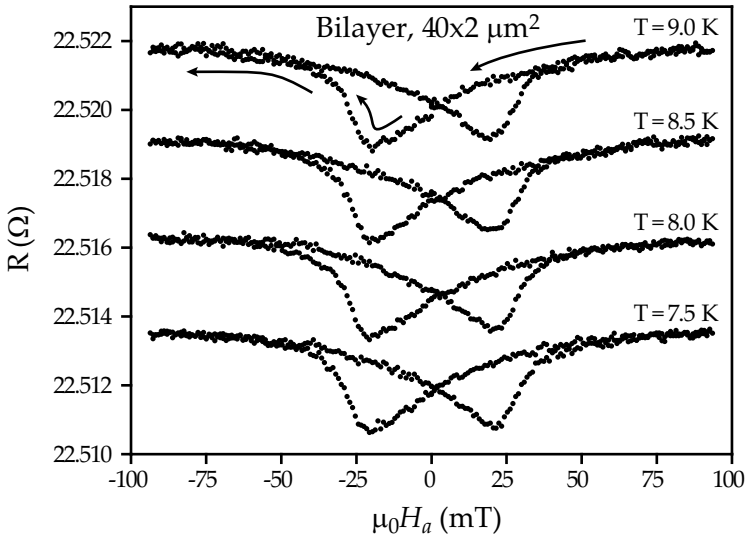


Figure 4.5: Resistance  $R$  versus in-plane applied field  $H_a$  on a  $40 \times 2 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strip at several temperatures above the superconducting transition. Arrows in the top curve show the direction of the field sweep starting from high fields.

Results of  $R(H)$  on a  $40 \times 2 \mu\text{m}^2$  bilayer strip for several temperatures  $T > T_c$  are presented in Fig. 4.5 and illustrate that the values  $H_{\text{dip},n}$  are independent of temperature in the range of a few Kelvin above  $T_c$ . The same measurements are repeated for  $T < T_c$  and shown in Fig. 4.6, where the resistance is normalized to the value at zero field. The measured signal now comes predominantly from the superconducting layer, which is shorting the ferromagnetic layer by percolation paths. The  $R(H)$  are measured at var-

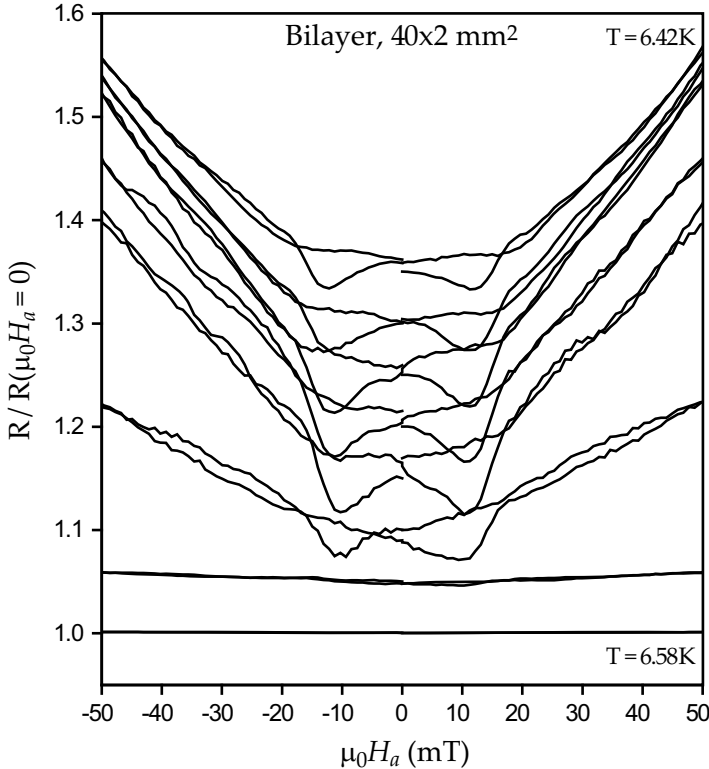


Figure 4.6: Resistance normalized to the value at zero field on a  $40 \times 2 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strip at several temperatures in the transition curve (Nb in superconducting state). The bottom curve is for  $T = 6.58$  K. Each subsequent curve is shifted by  $+0.05$  with respect to the previous one, with corresponding temperatures 6.55, 6.52, 6.50, 6.48, 6.46, 6.44 and 6.42 K (top curve).

ious temperatures along the transition curve shown in Fig. 4.7, which has an approximate width of 100 mK. The 100 mK width makes that a relative resistance change of  $10^{-4}$  (our typical result in the AMR measurements) corresponds to a temperature change of 0.01 mK. This is below our measurement

accuracy, so we lose track of any AMR features while in the transition area. Again there are two clear dips visible as well as a parabolic shaped response at higher fields, for all measurements except for the one very near the top of the transition curve at 6.58 K. That one gives a straight line; apparently the superconductor is driven into the normal state by the measurement current which in all measurements was of the order  $2.5 \times 10^8$  A/m<sup>2</sup>. The relative resistance change  $(\delta R)/R$  in the dips is now of order of percents, much larger than the observed AMR effect. Moreover, the size of the dip, meaning the maximum value of the resistance difference  $\delta R$  between forward and backward sweeps, goes through a maximum. Fig. 4.7 shows  $\delta R$  taken from the unnormalized data as function of temperature. It peaks at 6.52 K, which is about halfway in the transition in the steepest part. We can relate this to a shift in  $T_c$  according to  $\delta R = \delta T_c (\partial R / \partial T)$  which comes to a few mK. Looking more carefully

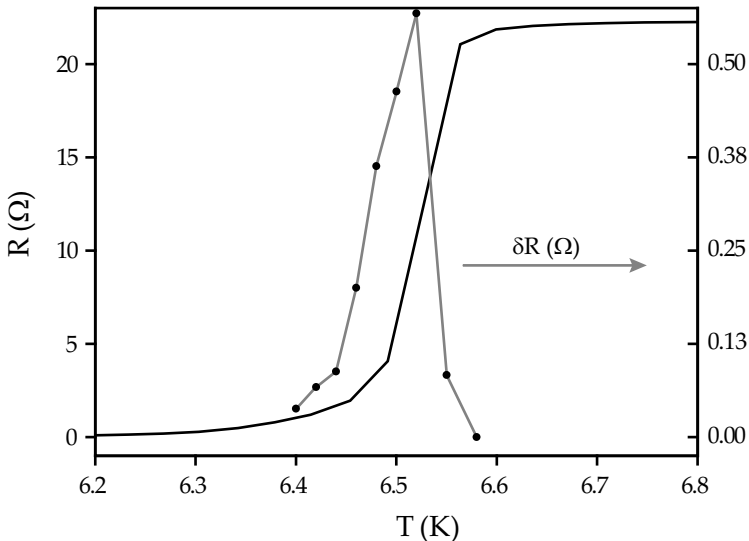


Figure 4.7: Temperature variation of the resistance of the device from Fig. 4.6 in the transition (left-hand scale), which is a typical result for all our devices. It also shows the temperature variation of the magnitude of the resistance dip  $\delta R$  (right-hand scale).

at the  $R(H)$  curve we notice that (coming from positive fields) the parabolic shaped curve, which reflects the standard response of the superconductor on a magnetic field, first makes an upward oriented kink around  $H = 18$  mT before it arrives at the dip, with  $H_{\text{dip,s}} = -12$  mT (s denoting the superconducting state). The location of the dips and their normalized sizes do not show a

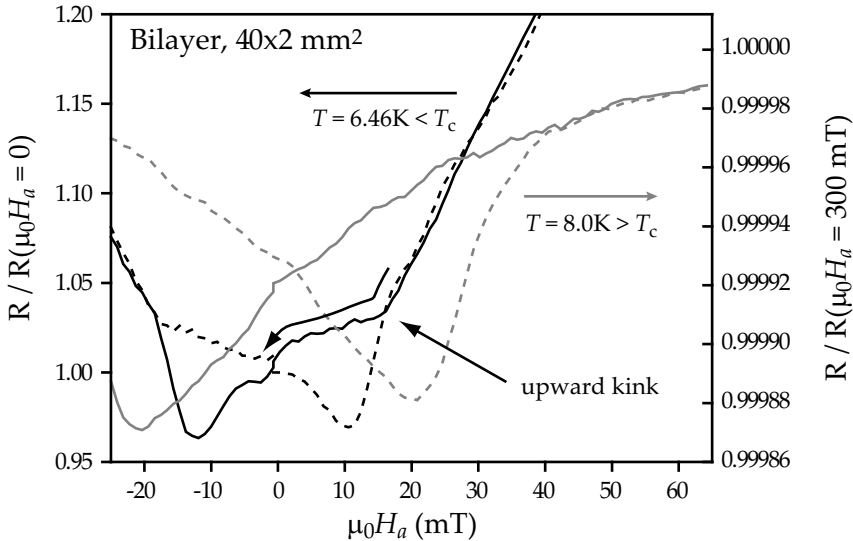


Figure 4.8: Comparison of the field dependence of the resistance  $R$  for a  $40 \times 2 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strip, with  $T$  above  $T_c$  (right-hand scale) and below  $T_c$  (left hand scale). The solid lines are data taken with *decreasing* field starting from +300 mT, as shown by the arrows; The dashed lines are data taken with *increasing* field starting from -300 mT. The upward kink in the decreasing-field data below  $T_c$  is also indicated.

strong temperature effect, which is a clear sign that the development of the superconducting gap is not significantly changing the ferromagnetic domain structure. Important to remark, however, is that the dip fields  $H_{\text{dip},s}$  are almost a factor two smaller than the dip fields  $H_{\text{dip},n}$ . We come back to this below, but for the moment we assume that they are still due to the domain state occurring in the Cu<sub>43</sub>Ni<sub>57</sub> layer. The dips reflect an enhancement of the (emerging) superconducting state, and therefore indicate that  $T_c$  is shifting towards higher values in the domain state, just as seen in previous work on Nb/Py bilayers. In Fig. 4.8 we show a comparison of the  $R(H)$  measurements (on our  $40 \times 2 \mu\text{m}^2$  bilayer) above and below  $T_c$ . It illustrates the difference in dip fields, but more important is to establish that the upward kink seen below  $T_c$  in the decreasing field data is still at positive fields in a regime, according to the AMR data, where domains are growing. On the other hand, no similar feature is detected in the AMR data.

We now want to discuss the observations with respect to the dip fields and the upward kink. Firstly, it is important to realize that the resistance dip occurring in the AMR effect is due to the fact that the resistance in the

ferromagnet depends on the angle between the local magnetization  $M$  and the current  $I$  with, for the case of CuNi, the lowest resistance when  $M \perp I$  [34]. The resistance minimum found when changing the direction of the magnetization then signifies the maximum amount of domains with a direction perpendicular to the current and the bridge. In the superconducting state, however, the resistance minimum comes about by a different mechanism, since it is determined by the average exchange field sampled by a Cooper pair of characteristic length  $\xi_S$ , which can be quite large close to  $T_c$ . There is no reason why the two types of averaging over a domain configuration would yield the same resistance minimum; for instance, a configuration where all of the magnetization is perpendicular to the current would give a strong minimum in AMR, but no resistance lowering in the superconducting state, since the exchange field in that case is homogeneous. It is interesting to remark that this difference would not be observable in Nb/Py, since in that case the switching was in such a small field range (order  $10^{-4}$  T) that a possible averaging difference would go unnoticed [56].

That leaves an explanation for the kink feature in  $R_s(H)$ . Looking again at Fig. 4.8, it does not seem a coincidence that the kink in the decreasing field data occurs around the coercive field in the increasing field part of the loop. In very similar measurements ( $R(H)$  in the resistive transition) on Nb/Py [56] a small increase in  $R$  was found at this field point in the hysteresis loop, although it was not visible in the magnetization that domains started to form. Apparently, domain formation starts when the field value comes inside the hysteresis loop even for quite square loops. Here we believe that the domain formation accelerates and starts to produce stray fields (either perpendicular, or in-plane), resulting in the kink because they act as Cooper pair breakers.

#### 4.4.2 Other bilayers and trilayers

The 2  $\mu\text{m}$  wide bilayer strips clearly show a decrease in resistance of the superconductor in the domain area of the ferromagnet. The results for other strip widths, specifically for 1  $\mu\text{m}$  and 'large' (200  $\mu\text{m}$  wide, 2 mm long) are given in Fig. 4.9, together with the result on a  $40 \times 2 \mu\text{m}^2$  trilayer. These presented curves are all below the steep part of the transition curve. They basically confirm the 2  $\mu\text{m}$  data, but there are some differences. First of all, in the narrower 1  $\mu\text{m}$  strip the resistance dips have completely disappeared, while the AMR data of Fig. 4.4 definitely indicate the presence of domains. Instead, only the parabolic feature remains here. On the other hand, for the larger widths the resistance dips are present at the same field value or a bit lower but now a new sharp dip appears, precisely coincident with the upward

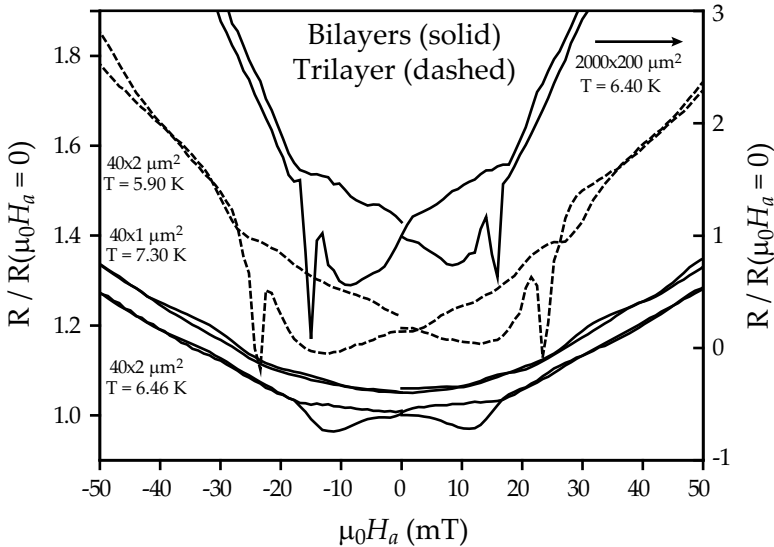


Figure 4.9: Normalized resistance measurements on a  $40 \times 1$ ,  $40 \times 2$  and  $2000 \times 200 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer (first one shifted by +0.05) and a  $40 \times 2 \mu\text{m}^2$  Cu<sub>43</sub>Ni<sub>57</sub>/Nb/Cu<sub>43</sub>Ni<sub>57</sub> trilayer strip (shifted by +0.2). Temperatures are all below the steep part of the corresponding transition curves.

kink discussed in the previous paragraph. Important of course is that also the new dip signifies lowering of resistance and is therefore not due to stray field enhancement. Without more precise knowledge of the size and shape of the domains and their evolution, it is difficult to give a solid explanation for these observations. What is known from decoration experiments with magnetic particles is that the typical domain size on large samples is of the order of  $0.5 \mu\text{m}$  [60]. Still, we perceive a hierarchy of events. For the smallest strip AMR detects the occurrence of domains with a component of their magnetization perpendicular to the current, but with a magnetization spread that is not large enough to significantly change the average field that Cooper pairs experience. For the  $2 \mu\text{m}$  strip the domain configuration in the switching is apparently different, and leads to a smaller averaged exchange field. For wider strips the domain state passes through even more configurations. In particular around the coercive field there probably is a large number of small domains, which leads to a sharp resistance dip.

Fig. 4.9 also shows a measurement on the trilayer structured as a  $40 \times 2 \mu\text{m}^2$  strip. The data show both the shallow dips and the sharp dips, similar to the

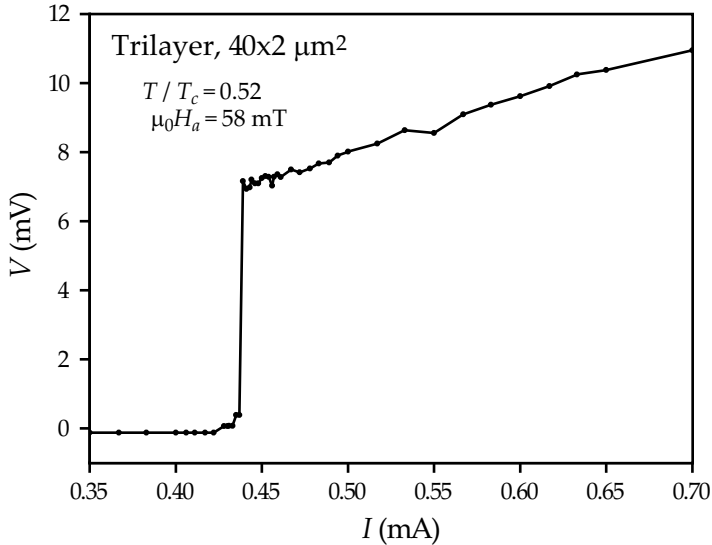


Figure 4.10: Voltage  $V$  versus current  $I$  measured on a  $40 \times 2 \mu\text{m}^2$   $\text{Cu}_{43}\text{Ni}_{57}/\text{Nb}/\text{Cu}_{43}\text{Ni}_{57}$  trilayer strip at 4.3 K and 58 mT. The sharp jump at 0.44 mA is taken as a measure for the critical (depairing) current.

bilayers with wider bridge widths. The bilayer results exclude that the two dips are due to different switching fields for the two layers, but in the spirit of the hierarchy sketched above, the domain state in the trilayer seems to resemble those of wider bilayers, which suggest a form of coupling between the two layers. From the size of the dip in  $R_s(H)$ , and the steepness of the transition curves at that temperature, we can estimate the corresponding  $T_c$  shift. For all our devices this results in an approximate shift of few mK. We also measured the transition curve at  $H_{\text{dip}}$  for the cases that the field was set from high positive fields (corresponds to the parabola) and from high negative fields (corresponds to the dip). In this way we found a shift in  $T_c$  of about 1.5 mK, which is hardly different from the values reported for the CuNi-based spin-valve in Ref. [49].

#### 4.4.3 $I_c(H)$ well below $T_c$

So far we focussed on transport measurements around the transition, which consistently show an enhancement of  $T_c$  in the domain state of the F layers. To see what happens below  $T_c$  we conducted a series of critical current measurements as function of applied field,  $I_c(H_a)$  by measuring the current  $I$  -



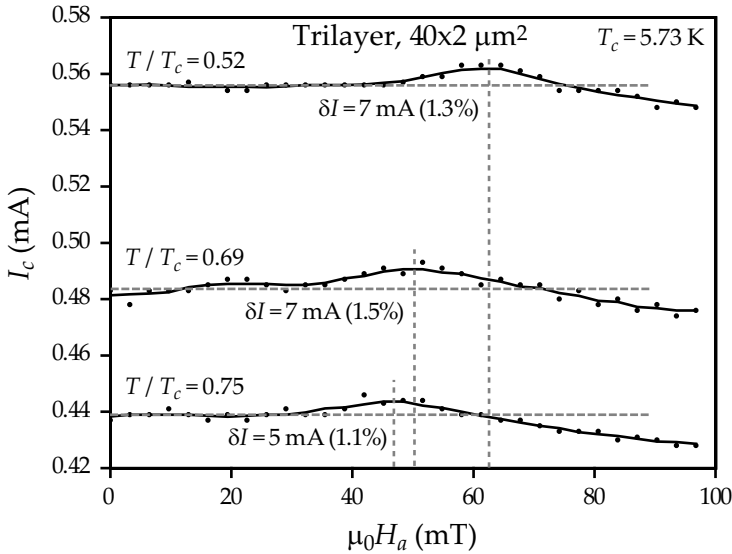


Figure 4.11: Critical current measurements  $I_c$  as function of applied magnetic field  $H_a$  on a  $40 \times 2 \mu\text{m}^2$   $\text{Cu}_{43}\text{Ni}_{57}/\text{Nb}/\text{Cu}_{43}\text{Ni}_{57}$  trilayer strip for different reduced temperature  $T/T_c$  as indicated. The value of  $T_c$  is 5.73 K. Dotted vertical lines indicated the positions of the maxima in  $I_c$ ; dotted horizontal lines show the average value of  $I_c$  around zero field as reference for the indicated values of increase in  $I_c$  at the maximum.

voltage  $V$  characteristic. We used 3 ms current pulses, with an interval of several seconds and increasing in amplitude until the critical current is reached and the superconductor is driven in the normal state. The sample is initially cooled down in zero field condition and the first measurement at a fixed temperature always starts in zero applied field. The  $I$ - $V$  curves all showed a sharp jump from almost zero voltage to the normal state, as we found before on S-films and S/F bilayers [59, 57]. An example is given in Fig. 4.10. The jump indicates that we are measuring a depairing current rather than the onset to vortex flow, which means that the measurement is directly sensitive to the superconducting gap. Also, the value of  $I_c$  is well defined due to the sharp transition. The results for the  $40 \times 2 \mu\text{m}^2$   $\text{Cu}_{43}\text{Ni}_{57}/\text{Nb}/\text{Cu}_{43}\text{Ni}_{57}$  trilayer are shown in Fig. 4.11, for three temperatures well below  $T_c$ , in terms of the reduced temperature  $t = T/T_c$  down to  $t = 0.5$ . All data show the same behavior, with initial constant  $I_c$  for increasing  $H_a$ , followed by a small maximum of the order of 1 %, before a decrease sets in. The field values where the maximum occurs,  $H_{\text{max}}$ , are in the range 50 mT - 60 mT and increase with decreasing temperature. The uncertainty in the determination of

$I_c$  is basically the step size for the increase in current ( $1.8 \mu\text{A}$ ) and therefore significantly below the enhancement of  $I_c$  we find around  $H_{\text{max}}$ . We interpret the enhanced  $I_c$  as an enhancement of the superconducting gap, and note that the percentage change is similar to the observed shifts in  $T_c$ . The peaks, however, do appear at fields higher than the observed dip fields in our  $R(H)$  measurements. In Fig. 4.12 we combine the values for  $H_{\text{dip}}$  and  $H_{\text{max}}$  for the  $40 \times 2 \mu\text{m}^2$   $\text{Cu}_{43}\text{Ni}_{57}/\text{Nb}/\text{Cu}_{43}\text{Ni}_{57}$  trilayer. It shows the constant value for  $H_{\text{dip,n}}$ , the jump to a lower value in the transition, and then the significant increase well below  $T_c$ .

We interpret the maximum in  $I_c$  as still caused by the domain state of the F layers. We do not know of similar data in the regime below  $T = 0.9$ , except for a report on Nb/Co bilayers where an increase in  $I_c$  of almost 50 % was found at around  $t = 0.5$  [61]. Such a large value may well be an artefact caused by the sample geometry. As mentioned in Ch. 4.3, the geometry used here consists of simple bars with Au contacts. When the contact pads are included in the etching, all observations can change significantly, and in particular for the  $I_c$  enhancement we also find an increase of over 60 % as will be shown in Ch. 4.5. The smaller value (of order 1 %) also seems intuitively reasonable, since the superconducting order parameter is now well developed and the superconducting coherence length is small, making the sampling of the domain state by the Cooper pair less efficient. That leaves the question of the increase in coercive fields to values above 60 mT. In order to set these in perspective, we can estimate the maximum coercive field  $H_{c,m}$  as expected for coherent rotation of the magnetization in the framework of the Stoner-Wohlfart model [34, 62]. For the field along the easy axis of magnetization,  $H_{c,m}$  equals the anisotropy field  $H_{an} = 2K_a/(\mu_0 M_s)$ , with  $K_a$  the anisotropy constant and  $M_s$  the saturation magnetization. Taking a value of  $6 \times 10^3 \text{ J/m}^3$  for  $K_a$  [63] and a value of 0.1 T for  $\mu_0 M_s$  [58] leads to roughly  $\mu_0 H_{an} = 0.1 \text{ T}$ , still above the value we find for the coercive fields. This indicates that the superconducting state has a significant effect on the domain structure during the rotation of the magnetization, going in the direction of coherent rotation. As that would mean that the amount of domain walls becomes less, it would be another ground for the small effects observed in the superconductor far below  $T_c$ . Incidentally, similar effects of the superconductor on the magnetic state have been reported before. Magnetization measurements using a microfabricated Hall probe on Al/Ni submicron samples showed that shielding currents can reshuffle magnetic domains [64]. Similarly, magnetization measurements by SQUID magnetometry on S/F multilayers demonstrated changes in the magnetic state of the F layers in response to the onset of superconductivity

[65, 66].

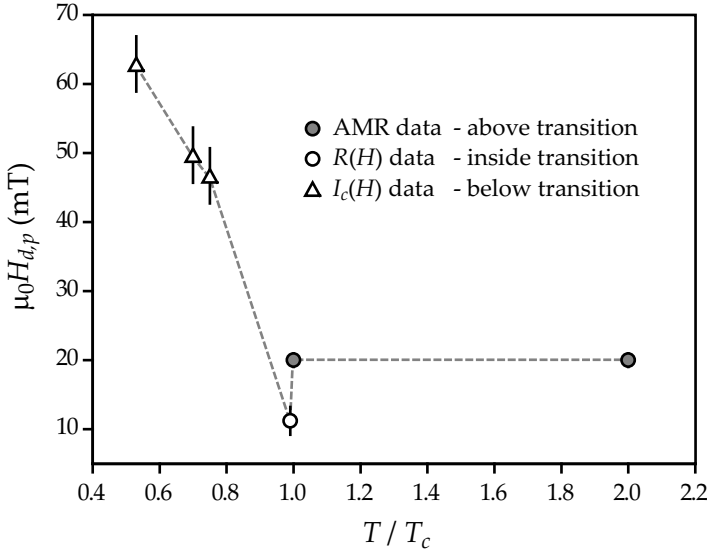


Figure 4.12: Collection of the measured dip and peak fields  $H_{d,p}$  in our devices as function of temperature.

## 4.5 The influence of magnetic contacts

In measurements on the effects of stray fields and the spin-valve mechanism in F/S/F trilayers different sample geometries are used. In particular for lithographically structured samples it is tempting to include contact pads in the layout, since then only a single etch step is needed to fabricate the full device. Here we show that such a 'contact-included' geometry behaves very differently from a simple strip which has been contacted with Au leads. A SEM image of a contact included strip is shown in Fig. 4.3b, and Fig. 4.3c shows the geometry of the bonding pads and leads to the strip. Field-dependent resistance measurements on a contact-included  $40 \times 2 \mu\text{m}^2$  bilayer for  $T > T_c$  and  $T < T_c$  are shown in Fig. 4.13 and Fig. 4.14 respectively, where they are compared

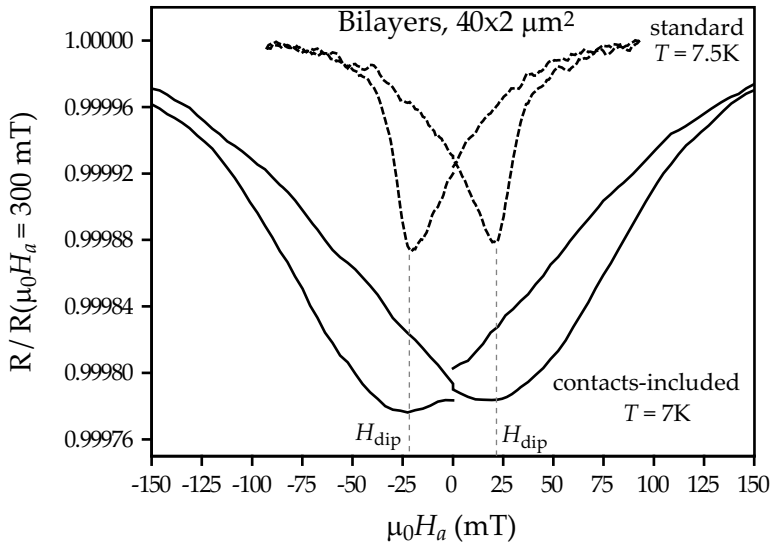


Figure 4.13: Resistance measurements on a contact-included  $40 \times 2 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strip, compared to a strip-like standard device of similar size (Nb in the normal state). The temperatures of the measurements (7.5 K and 7 K) are just above  $T_c$  for both devices. The values of the dip field are indicated with the dotted lines.

to the results obtained on our standard bilayer strip. Above  $T_c$  the AMR dip shows a large broadening of about a factor 4, while the coercive field value is about the same with a value close to  $\pm 22$  mT. Below  $T_c$  the results are not very different, except that the location of the dip has shifted to a higher value coinciding with the observed coercive field. From these resistance measurements the "malfunctioning" of the device is not clear, but it does point towards a coercive-field dominated working of the device, from which we have shown is not the underlying mechanism in our strips. In Fig. 4.15 we show critical current measurements on a contact-included  $40 \times 2 \mu\text{m}^2$  trilayer and compare them to the results obtained on the standard trilayer strip. The obvious difference is the size of the peak, which now shows an increase of nearly 60 percent! The location of the peak compares very well to the ones found on the standard device. Most likely, the T-shaped contact areas create a bottleneck for the supercurrent. Due to that shape, the magnetic anisotropy energies are likely to dominate the formation process and induce a very inhomogeneous magnetic profile localized near the contacts. This explains the large broadening of the AMR curve. Furthermore, this complex domain structure (or rather the stray fields produced by it) strongly suppresses the gap, an effect which apparently

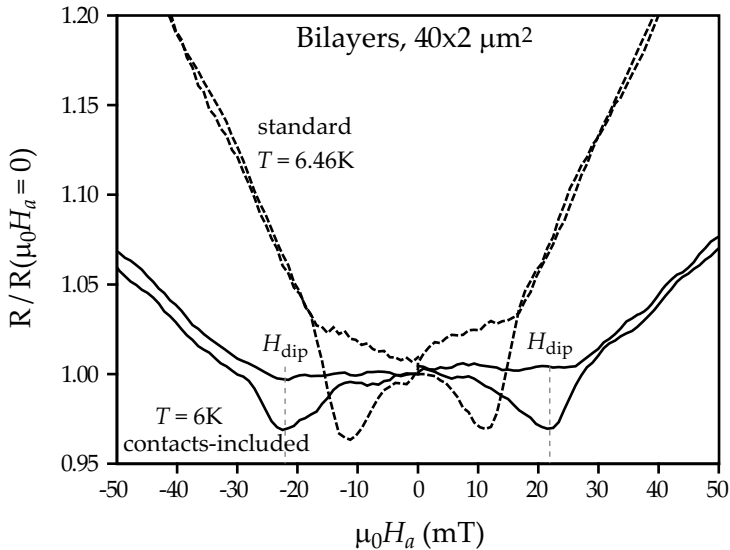


Figure 4.14: Resistance measurements on a contact-include  $40 \times 2 \mu\text{m}^2$  Nb/Cu<sub>43</sub>Ni<sub>57</sub> bilayer strip, compared to a strip-like standard device of similar size (Nb in the superconducting state). The temperatures of the measurements (6.46 K and 6 K) are in the resistive transition for both devices. The values of the dip field are indicated with the dotted lines.

disappears at higher fields, resulting in a large increase in critical current.

## 4.6 Conclusions

In conclusion, we investigated the effect of magnetic domains on a superconductor for the case of weakly ferromagnetic Cu<sub>43</sub>Ni<sub>57</sub> by comparing magnetotransport measurements above and below the superconducting transition, both for bilayers and for trilayers resembling a spin-valve geometry, and for small structures as well as for large samples. We generally find that above the transition the resistance change is dominated by the AMR effect of the ferromagnetic layer (with a relative change of order  $10^{-4}$ ), while in the transition it is dominated by changes in the superconducting gap (with a relative change of order  $10^{-1}$ ). The AMR measurements show that domains are appearing in all our devices even down to the smallest bridges of  $1 \mu\text{m}$  wide, with nearly identical hysteretic behavior and a coercive field value of 22 mT. In the samples with a  $2 \mu\text{m}$  bridge a small but clear enhancement of  $T_c$  is found inside the transition which we claim to be due to the presence of mag-

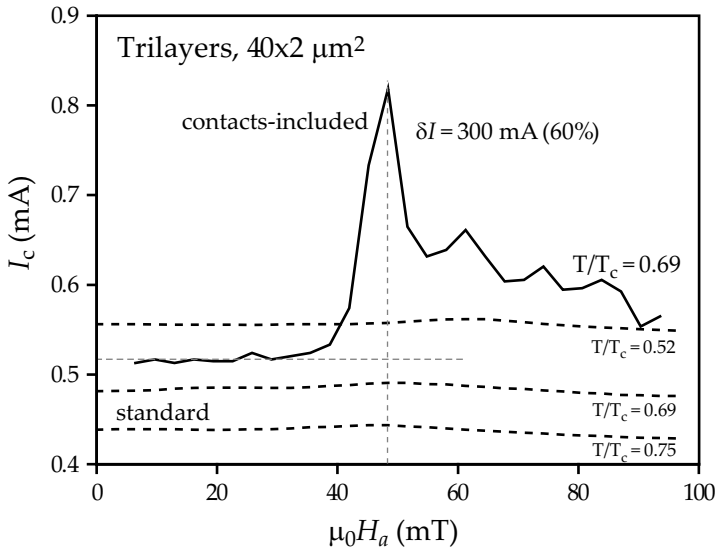


Figure 4.15: Critical current measurements  $I_c$  as function of applied magnetic field  $H_a$  on a contact-included  $40 \times 2 \mu\text{m}^2$   $\text{Cu}_{43}\text{Ni}_{57}/\text{Nb}/\text{Cu}_{43}\text{Ni}_{57}$  trilayer strip, for a reduced temperature  $T/T_c = 0.69$ . The dashed lines show the data from the standard devices displayed in Fig. 4.11. Also indicated is the critical current increase in the peak as compared to the zero-field value.

netic domains. This enhancement is present in a limited field range, somewhat smaller than the range over which domains are present in the ferromagnetic layers. Still in the transition, the largest effect on the resistance is at a different field than the largest dip in the AMR. We believe that this reflects the difference in mechanisms giving rise to the two effects; on the one hand magnetization perpendicular to the current, on the other optimal sampling when the superconducting coherence length and the ferromagnetic domain sizes are of similar order. In samples with wider bridges even two dips are found in the transition, which is qualitatively ascribed to the evolution of domain states which appears to be possible in these wider samples. By going to lower temperatures and measuring the critical current (as a measure of the strength of the superconducting gap) we see that this enhancement is still present but the field at which it appears is shifting towards significantly higher values. This we attribute to the increasing strength of the superconductor which is forcing the ferromagnet to switch in a more single domain type of manner. The results on our micro-structured bilayers are very similar to the ones on our large-scale bilayer and micro-structured trilayers. All different measurement

show enhancement of the superconducting gap with a relative size of a few percent. This is very similar to all previous works on spin-valves involving weakly ferromagnetic CuNi, where the mechanism was believed to be the parallel vs anti-parallel orientation of the exchange fields. In view of our results, domain formation in the individual F-layers should be considered at least as an effect of similar importance.