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## Simulating Cosmic Reionisation

Pawlak, A.H.

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# SIMULATING COSMIC REIONISATION



# SIMULATING COSMIC REIONISATION

Proefschrift

ter verkrijging van  
de graad van Doctor aan de Universiteit Leiden,  
op gezag van de Rector Magnificus prof. mr. P. F. van der Heijden,  
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door

Andreas Heinz Pawlik

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in 1978

Promotiecommissie

Promotor: Prof. Dr. H. Röttgering

Co-promotor: Dr. J. Schaye

Overige leden: Prof. Dr. V. Icke  
Prof. Dr. K. Kuijken  
Dr. V. Springel (MPA Garching)  
Prof. Dr. S. Zaroubi (Universiteit Groningen)

*Because something is happening here.*

*But you don't know what it is.*

*Do you, Mr Jones?*

BALLAD OF A THIN MAN

**Section of the East Side Gallery, Berlin, December 2007.** The East Side Gallery is a memorial for freedom that consists of about 100 paintings by international artists on part of the Berlin wall between Ostbahnhof and Oberbaumbrücke along the river Spree. Photo taken by the author. Digitalization: Machteld Dekens. Cover design: Thomas Wilhelmi.

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