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Quantum entanglement in polarization and space

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Quantum entanglement in polarization and space

PROEFSCHRIFT

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