

BREAKING THE CURVE WITH CANDELS: A BAYESIAN APPROACH TO REVEAL THE NON-UNIVERSALITY OF THE DUST-ATTENUATION LAW AT HIGH REDSHIFT

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ABSTRACT

Dust attenuation affects nearly all observational aspects of galaxy evolution, yet very little is known about the functional form of the dust-attenuation law in the distant Universe. In this work, we fit to the spectral energy distributions (SEDs) of galaxies under different assumptions about the wavelength-dependent dust-attenuation curve, and compare the inferred attenuation with the observed infrared (IR) luminosities. This is applied to a sample of IR-luminous galaxies at $z \sim 1.5 - 3$ where the multi-wavelength CANDELS photometry cover rest-frame ultraviolet (UV, down to Lyman- α) to near-IR (NIR) wavelengths, with supporting 24 μm imaging from *Spitzer*. We fit the UV-to-NIR galaxy SEDs with multiple dust laws, and use Bayes factors to select galaxies with strong preference between laws. Importantly, we find that for individual galaxies with strong Bayes-factor evidence, their observed location on the plane of the infrared excess (IRX , $L_{\text{TIR}}/L_{\text{UV}}$) and UV slope (β) agrees with the predicted value for the favored dust law. Furthermore, a parameterization of the dust law reveals a relationship between its UV-to-optical slope (δ) and the color excess: $\delta = (0.62 \pm 0.05) \log(E(B - V)) + 0.26 \pm 0.02$. Galaxies with high color excess have a shallower, starburst-like attenuation, and those with low color excess have a steeper, SMC-like attenuation. Surprisingly, the shape of the dust law does not depend on stellar mass, star-formation rate, or β , at least for galaxies down to the stellar mass range of this work ($\log M_{\star}/M_{\odot} > 9$). The strong correlation between the tilt of the attenuation law, and color excess is consistent with expected effects from an attenuation driven by scattering, a mixed star-dust geometry, and/or trends with stellar population age, metallicity, and dust grain composition. We extend these results to a larger sample with photometric redshifts at $1.5 < z < 3$, which gives us confidence that this method can provide quantitative constraints on the dust-attenuation law at even higher ($z > 3$) redshifts.

1. INTRODUCTION

Our knowledge of star-formation rates (SFRs) among the majority of the highest redshift galaxies $z > 4$ is (except in rare cases) limited to observations in the rest-frame UV, where the effects of the dust attenuation are most severe and leads to large systematics. High-redshift surveys are predominantly limited to studying the rest-frame ultraviolet (UV)-to-near infrared (NIR) spectral energy distribution (SED). The dust attenuation at this critical portion of the SED cannot be dismissed even at $z = 7 - 8$, considering the mounting observations of high-redshift dusty star-forming galaxies, sub-millimeter galaxies, and quasars (Wang et al. 2008; Finkelstein et al. 2012; Casey et al. 2014a). In addition, while there is no

shortage of observations/simulations that offer potential mechanisms for dust production in the early universe (Todini & Ferrara 2001; Gall et al. 2011a,b,c; Ventura et al. 2014), it is still uncertain how, and to what degree, these mechanisms influence the wavelength-dependence of attenuation at high redshift.

The nuances of dust geometry, extinction, and scattering from the interstellar medium (ISM) and star-forming regions are often conveniently packaged into a “recipe” of reddening (Calzetti 1997), parameterized by a wavelength-dependent curve of the total-to-selective extinction (Witt & Gordon 2000, and references therein),

$$k_{\lambda} = A_{\lambda}/E(B - V) \text{ and } R_V = A_V/E(B - V), \quad (1)$$

where A_{λ} is the total extinction in magnitudes at wavelength λ and $E(B - V)$ is the color excess of selective

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extinction. We emphasize the distinction that dust “extinction” accounts for the absorption and scattering of light out of the line of sight, whereas “attenuation” also accounts for the spatial scattering of light into the line of sight for extended sources such as galaxies. We refer to both extinction and attenuation models as “dust laws” for brevity. Successful empirical and analytic dust laws have been used for decades as a necessary *a priori* assumption when inferring fundamental physical properties of galaxies (Papovich et al. 2001).

Dust laws are already known to be non-universal across all galaxy types from derivations of the Small and Large Magellanic Cloud (SMC and LMC) and Milky Way dust laws, as well as dust attenuation in $z < 1$ galaxies (Conroy & Gunn 2010). For example, Kriek & Conroy (2013) have shown that the form of the dust law can vary significantly at $z < 2$ as a function of galaxy type and in some cases it differs strongly from the conventionally assumed Calzetti et al. (2000) prescription, derived from local UV-luminous starbursts. The conditions that produce these unique dust laws are complex. They depend on the covering factor of the dust grain size, line-of-sight geometry, and composition (which depends on metallicity), and can therefore change when galaxies are viewed at different orientations (Witt & Gordon 2000; Chevillard et al. 2013) or stellar population ages (Charlot & Fall 2000). The differences in dust grain properties stem from the dust production sources, such as supernovae (SNe) and asymptotic giant branch (AGB) stars, which may change relative strength over cosmic timescales (Morgan & Edmunds 2003).

Changes in the observed star-dust geometry, the relative geometry between stars and dust grains, produce different attenuation scenarios even for galaxies of a similar type. For example, observations of the infrared excess ($IRX \equiv L_{TIR}/L_{UV}$) and the UV slope, (β , $f_\lambda \propto \lambda^\beta$), have shown that star-forming galaxies bracket a range of attenuation types from starburst to SMC-like attenuations (Buat et al. 2011, 2012; Muñoz-Mateos et al. 2009; Overzier et al. 2011). The position of galaxies on the $IRX - \beta$ plane suggests that a single dust-attenuation prescription is incapable of explaining all observations (Burgarella et al. 2005; Seibert et al. 2005; Papovich et al. 2006; Boquien et al. 2009; Casey et al. 2014b).

Although star-forming galaxies likely have a variety of attenuation scenarios, it is possible to infer their dust geometries by correlating them with physical properties. For example, Reddy et al. (2015) studied a sample of $z \sim 2$ galaxies and found that the differences in attenuation between gas and stars is correlated with the galaxy’s observed specific SFR ($sSFR = SFR/M_*$), potentially a byproduct of the visibility of star-forming birth clouds. If the dust law is dependent on star-formation activity, then it may be different at earlier epochs ($z > 2$). It is now understood that the intensity of star-formation and ionization conditions, which directly influence the attenuation conditions, have evolved with redshift (Madau & Dickinson 2014; Steidel et al. 2014; Casey et al. 2014b; Shimakawa et al. 2015; Shapley et al. 2015; Sanders et al. 2015). These conditions are regulated by the formation, destruction, and spatial distribution of dust grains, and this cycle is one of the most poorly quantified processes in galaxies. One reason to seek evidence for the dust law is to place constraints on dust grain

size/composition and their production mechanisms, such as SNe and AGB stars. A better understanding of these mechanisms would help to constrain metal buildup and galactic feedback (Gall et al. 2011a; Davé et al. 2011).

Both the scale and the shape of the dust affect the interpretation of galaxy SFRs, the evolution of the SFR density, and the evolution of the intergalactic medium (IGM) opacity. For example, Smit et al. (2014) show their measurement of the $z \sim 7$ specific SFR (SFR/Mass) changes by nearly an order of magnitude depending on the assumed prescription of dust attenuation. It is clear that new methods must be developed to determine the shape of the dust law in the distant universe.

Our goal in this work is to provide evidence for the dust law at high redshifts using the information from galaxies’ rest-frame UV-to-NIR SEDs. We use a Bayesian formalism that marginalizes over stellar population parameters from models of the galaxy SEDs (Salmon et al. 2015). This allows us to measure evidence in favor of one dust law over another for individual galaxies. We show that the favored dust laws are consistent with the galaxies’ locations on the $IRX - \beta$ diagram for a sample of galaxies at $1.5 < z < 3.0$ with mid-IR imaging, where we can verify that the predicted attenuation agrees with the IRX .

This work is organized as follows. §2 outlines our photometric and IR data, redshifts, and sample selection, as well as our calculations of IR luminosities and β . §3 describes the framework of our SED-fitting procedure, including the stellar population models and dust laws. §4 defines the use of Bayes factors as our selection method, and §5 defines our parameterization of the dust law. §6 shows the main results of the paper, where we use our Bayesian technique to quantify the evidence that star-forming galaxies at $z \sim 1-2$ have a given dust law, using CANDELS *Hubble Space Telescope* (*HST*) and *Spitzer* data spanning the rest-frame UV-to-NIR SED. We then show that the UV color and thermal IR emission (measured from mid-IR data) of these galaxies match the properties of their predicted dust law. §7 discusses the implications and physical origins of our results, as well as comparisons to previous work and dust theory. Finally, §8 summarizes our main conclusions. We assume concordance cosmology such that $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{M,0} = 0.3$ and $\Omega_{\Lambda,0} = 0.7$.

2. DATA, REDSHIFTS, AND SAMPLE SELECTION

2.1. Photometry: CANDELS GOODS Multi-wavelength Data

This work takes advantage of the multi-wavelength photometry from the GOODS North and South Fields (Giavalisco et al. 2004), the CANDELS survey (Grogin et al. 2011; Koekemoer et al. 2011), the WFC3 Early Release Science program (ERS Windhorst et al. 2011), and the Hubble Ultra Deep Field (HUDF Beckwith et al. 2006; Ellis et al. 2013; Koekemoer et al. 2013; Illingworth et al. 2013). We define magnitudes measured by *HST* passbands with the ACS F435W, F606W, F775W, F814W and F850LP as B_{435} , V_{606} , i_{775} , I_{814} , and z_{850} , and with the WFC3 F098M, F105W, F125W, F140W, and F160W, as Y_{098} , Y_{105} , J_{125} , JH_{140} , and H_{160} , respectively. Similarly, bandpasses acquired from ground-based observations include the VLT/ISAAC K_s ; and

VLT/HAWK-I K_s bands. We refer to Guo et al. (2013) for more details on the GOODS-S dataset, and Barro et al. (in prep.) for the GOODS-N dataset.

As applied by Salmon et al. (2015), we include an additional flux uncertainty, defined to be 10% of the flux density per passband of each object. This accounts for any systematic uncertainty such as flat-field variations, PSF and aperture mismatching, and local background subtraction. The exact value was chosen from series of recovery tests to semi-analytic models applied by Salmon et al. (2015). Including this additional uncertainty also helps to avoid situations where a given model SED band serendipitously finds a perfect match to an observed low-uncertainty band, creating a biased posterior around local maxima. The additional uncertainty is added in quadrature to the measured uncertainties.

2.2. IR Photometry: Spitzer and Herschel

We utilize imaging in the IRAC 3.6 and 4.5 μm bands from the *Spitzer* Extended Deep Survey (Ashby et al. 2013) to measure the rest-frame NIR of the galaxy SED. As described by Guo et al. (2011), photometry was measured for sources in versions of the *HST* images that was convolved to match their point-spread functions. The IRAC catalog uses the *HST* WFC3 high-resolution imaging as a template and matches to the lower-resolution images using TFIT (Laidler et al. 2007) to measure the photometry.

In order to verify the dust-attenuation law derived from the rest UV-to-NIR data, we require a measure of the rest UV-to-optical light reprocessed by dust and reemitted in the far-IR. Conventionally, the important quantities are the ratio of the observed IR-to-UV luminosities, $L(IR)/L(UV)$, which measures the amount of reprocessed light, and the UV-spectral slope, β , which measures the shape of the dust-attenuation curve (e.g., Meurer et al. 1999; Charlot & Fall 2000; Gordon et al. 2000; Noll et al. 2009; Reddy et al. 2010). We use MIPS 24 μm measurements from the GOODS-*Herschel* program (Elbaz et al. 2011), where the GOODS IRAC 3.6 μm data was used as prior positions to determine the MIPS 24 μm source positions. Then, PSF-fitting source extraction was performed to obtain 24 μm fluxes, which we require to be $> 3\sigma$ detections for our sample. While we also examined galaxies with *Herschel* PACS and SPIRE 100 to 250 μm photometry, these data were ultimately not included in the results for reasons discussed in §2.5.

2.3. Redshifts

To minimize uncertainties in SED-fitting owing to redshift errors, we selected objects that have the highest quality spectroscopic redshifts. The spectroscopic redshifts are a compilation (Nimish Hathi & Mark Dickinson, private communication) from several published and unpublished studies of galaxies in GOODS-S (Mignoli et al. 2005; Vanzella et al. 2008; Balestra et al. 2010; Popesso et al. 2009; Doherty et al. 2005; Kriek et al. 2008; Fadda et al. 2010, Weiner et al. (unpublished)) and GOODS-N (Reddy et al. 2006; Daddi et al. 2009). We define the sample of galaxies with high-quality redshifts as the “spec- z ” sample, but later we consider the full sample with photometric redshifts, which we call the “phot- z ” sample.

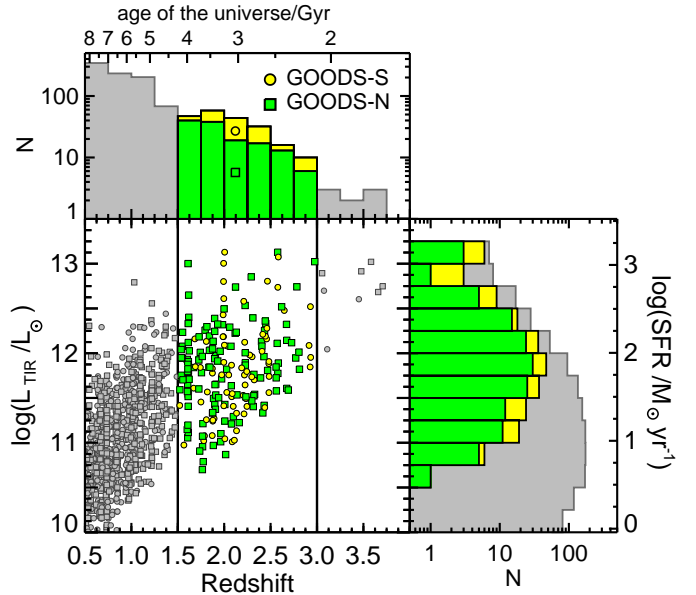


Figure 1. The log of total IR Luminosity (L_{TIR}), which was determined using a redshift dependent conversion from $L_{24 \mu\text{m}}$, as a function of redshift. Galaxies in our sample lie in GOODS-N (yellow) and GOODS-S (green) and were restricted to $\log L_{\text{TIR}} < 12.5$ and $z_{\text{spec}} > 1.5$. The adjacent histograms compare the logarithmic distributions of our sample to the parent sample. For reference, the top and right axes show the age of the universe and the SFR respectively.

The primary goal of this work is to determine the ubiquity of the dust-attenuation law at the peak of the SFR density. When deriving properties of distant galaxies we must naturally consider how our results are dependent on the assumed redshift of each galaxy. This can be done in two ways. First, we explore how our results depend on redshift accuracy by testing how our results vary if we use photometric redshifts for galaxies rather than their spectroscopic redshifts. Second, we determine how the results of the spec- z sample differ from a larger sample of galaxies with photometric redshifts. The former test addresses how photometric redshift accuracy in general affects the methods and results, while the latter test addresses if the photometric redshift accuracy within a larger sample is sufficient to reproduce the spectroscopic-redshift results. In addition, a photometric-redshift sample can reveal biases in the spec- z sample because the latter is likely biased towards the brighter, bluer galaxies.

We use photometric redshifts that were derived following the methods by Dahlen et al. (2013), who developed a hierarchical Bayesian technique to convolve the efforts of eleven photometric redshift investigators in the CANDELS team. The photometric-redshift estimates of GOODS-S are taken from Santini et al. (2015) and those of GOODS-N are taken from Dahlen et al. (2015 in prep.). The GOODS-N photometric-redshift estimates also take advantage of SHARDS-grism narrow-band data. We take the photometric redshift as the median from the combined full $P(z)$ distributions of nine GOODS-N and six GOODS-S photometric-redshift investigators. We estimate the photometric-redshift accuracy from the normalized median absolute deviation, which gives a 68% confidence range, of $\sigma_{\text{NMAD}}/(1+z) = 0.040$ (Brammer et al. 2008).

2.4. Sample Selection

We limited the sample to $z > 1.5$, such that the ACS B_{435} band still samples the rest-frame far-UV (FUV, ~ 1500 Å), which is a crucial portion of the SED when distinguishing between dust laws. §6.1 discusses the consequences of a galaxy not having a band close to the FUV, due to the redshift or available photometry. We also required a $z < 3$ limit because the IR-selection of sources at higher redshift correspond to objects with very bright IR luminosities ($\log L_{\text{TIR}}/L_{\odot} > 12.5$), where the frequency of objects dominated by AGN emission increases to $\sim 60\%$ (Nardini et al. 2010). In addition, the upper redshift limit was chosen to avoid significant redshift evolution within the sample.

The redshift range of $1.5 < z < 3.0$ and $24 \mu\text{m}$ detections ($f_{24 \mu\text{m}} S/N > 4$) produces an initial sample of 65 (554) GOODS-N and 123 (552) GOODS-S spec- z (phot- z) selected galaxies. A small number ($< 5\%$ of the spec- z sample and $< 2\%$ of the phot- z) of objects were identified on or near bright stars and diffraction spikes, as well as at the edges of the image (Guo et al. 2013) and were removed from all samples.

We further identified galaxies that imply the presence of an active galactic nucleus (AGN) from their IR or radio data (Padovani et al. 2011; Donley et al. 2012) or if they have known X-ray detections (Xue et al. 2011). This selection removes 6 (52) GOODS-N and 31 (108) GOODS-S sources in the spectroscopic (phot- z) spec- z sample. Our final sample contains 56 (485) GOODS-N and 88 (432) GOODS-S galaxies in the fiducial spec- z (phot- z) sample.

2.5. Calculation of Total Infrared Luminosities

One method to calculate the total infrared luminosity (L_{TIR}) involves fitting broadband flux densities to a suite of look-up tables that were derived from templates of local IR luminous galaxies (Elbaz et al. 2011; Dale et al. 2001; Dale & Helou 2002; Rieke et al. 2009). However, recent work has shown that template-fitting can overestimate L_{TIR} especially when the observed bands do not well sample the dusty SED (see Papovich et al. 2007; Overzier et al. 2011). At the redshifts of our sample, 46% of our galaxies lack detections redward of $24 \mu\text{m}$ (i.e., *Herschel* PACS or SPIRE). Detailed studies have calibrated the $24 \mu\text{m}$ luminosity to an approximation of L_{TIR} for both local and high-redshift ($z < 2.8$) galaxies (Wuyts et al. 2008; Rujopakarn et al. 2013). Here, we adopt the relation between $24 \mu\text{m}$ flux density and total IR luminosity from Rujopakarn et al. (2013) (see their equation 3 and Fig. 2). We then convert the total IR luminosities to SFRs following Rujopakarn et al. (their equation 8, which is similar to the Kennicutt (1998) conversion, with factors applied appropriate for a Salpeter-like IMF). This $24 \mu\text{m}$ conversion was developed under several relevant assumptions: that it applies to $z \sim 2$ galaxies that lie on the SFR-stellar mass main sequence, the galaxies are not hyperluminous ($L_{\text{TIR}} < 10^{13} L_{\odot}$), and that IR surface density scales linearly with IR luminosity. These assumptions become important for compact starburst galaxies and ULIRGs ($L_{\text{TIR}}/L_{\odot} > 10^{12}$). Nevertheless, these objects are rare and less than 8% of galaxies have $L_{\text{TIR}}/L_{\odot} > 10^{12}$ in both the phot- and spec- z samples. This small fraction of the sample are not the

galaxies that drive the results of this work. In addition, we take advantage of $\sim 54\%$ of the galaxies in our spec- z sample that have *Herschel* PACS and/or SPIRE data in order to justify our conversion of $24 \mu\text{m}$ luminosity to L_{TIR} . The details of this comparison can be found in Appendix A, but in short, the results of this work are unaffected by using fits to *Herschel* data instead of the $24 \mu\text{m}$ conversion to calculate L_{TIR} .

The distribution of L_{TIR} is shown in Figure 1 as a function of redshift for all $24 \mu\text{m}$ -detected sources with spectroscopic redshifts, including those within our redshift range. For reference, we also show the SFRs corresponding to a given L_{TIR} following conversions by Rujopakarn et al. (2013). This figure shows that galaxies in our sample have IR luminosities ranging from 5×10^{10} to $10^{13} L_{\odot}$, consistent with luminosities of LIRGs and ULIRGs.

2.6. Calculation of UV Slope β

The rest-frame UV slope is an important observational tool due to its relative ease of measurement for the highest redshift galaxies (even to $z \sim 10$, see Wilkins et al. 2015) and its sensitivity to stellar population age, metallicity, and attenuation by dust. Moreover, β has often been used to estimate the dust attenuation by extrapolating its well-known local correlation with infrared excess (Meurer et al. 1995, 1999). Studies of the origins of the scatter in the $IRX - \beta$ relation show that it depends on metallicity, stellar population age, star-formation history, spatial disassociation of UV and IR components, and the shape of the underlying dust-attenuation curve, including the presence of the 2175 Å absorption feature (Gordon et al. 2000; Buat et al. 2005, 2010; Reddy et al. 2006; Muñoz-Mateos et al. 2009; Boquien et al. 2012). This raises concerns about generalizing the $IRX - \beta$ relation to higher redshifts (e.g., see the discussion by Casey et al. 2014b).

Historically, the methods used to calculate β have been entirely dependent on the available dataset. In the absence of UV continuum spectroscopy (the original method to determine β , Calzetti et al. 1994), we must calculate β from the UV colors provided by broadband photometry. Specifically, we calculated β from the best-fit SED following the methods of Finkelstein et al. (2012). We favor this method over a power-law fit to the observed photometric bands for the following reasons.

First, we ran simple tests to recover the true β from using a power-law fit to the bands with central wavelengths between rest-frame $1200 < \lambda < 3000$ Å. The true β is determined from stellar population models by Kinney et al. (1996), using the spectral windows defined by Calzetti et al. (1994) after applying a range of $E(B - V)$. This method produces a systematic offset at all redshifts such that $\beta_{\text{true}} = \beta_{\text{phot}} - 0.1$, and at some redshifts the recovery is off as much as $\Delta\beta = -0.5$.

Second, Finkelstein et al. (2012) saw a similar offset and scatter in recovering β from a single color or power-law fit. They promoted calculating β by using UV-to-optical photometry to find the best-fit SED and using the UV spectral windows of Calzetti et al. (1994) to determine β . Their simulations report a better recovery of β_{true} with no clear systematics and a scatter of $\Delta\beta = \pm 0.1$ for galaxies at $z = 4$. We therefore used the best-fit model to calculate β , assuming a constant SFH

Table 1
SED Fitting Parameters

Parameter	Quantity	Prior	Relevant Sections
Redshift	fixed	spectroscopic redshifts, $1.5 \leq z_{\text{spec}} \leq 3.0$	§ 2.3 § 6.2
	fixed	photometric redshifts, $1.5 \leq z_{\text{phot}} \leq 3.0$	§ 2.3 § 6.3
Age	100	10 Myr to t_{max} ^a	–
Metallicity	5	$0.02 Z_{\odot} \leq Z \leq 2.5 Z_{\odot}$	–
$E(B - V)$ ^b	85	Linear, -0.6 to 1.5	§ 3.3
Attenuation prescription	fixed	starburst (Calzetti et al. 2000) or SMC92 (Pei 1992)	§ 3.3 § 6.2.2
	varied	δ power-law deviation from starburst (Noll et al. 2009)	§ 5 § 6.3.2
f_{esc}	fixed	0	–
Star formation history ^c	fixed	100 Gyr (constant)	§ 3.2
	varied	$\pm\tau = 0.1, 0.3, 1, 3, 10$ Gyr	§ 3.2

^aThe lower end of this range represents the minimum dynamical time of galaxies in our redshift range up to t_{max} , which is the age of the Universe for the redshift of each object, which is up to 4.2 Gyr at $z \sim 1.5$.

^bWe fit to a range of color excess values, $E(B - V)$. This scales the dust-attenuation curve to achieve a wavelength-dependent attenuation, $A(\lambda) = k(\lambda)E(B - V)$.

^cThe star formation history is defined as $\Psi(t) = \Psi_0 \exp(t/\tau)$ such that a SFR that increases with cosmic time has a positive e -folding time, τ . When the SFH is allowed to vary as a fitted parameter, we consider rising and declining histories (positive and negative τ) separately. When the star formation history is fixed to constant, we assume a very long e -folding time, $\tau \sim 100$ Gyr.

and a starburst (Calzetti et al. 2000) dust law. One may be concerned that the choice of dust law may influence the calculation of β . However, the best-fit SED will always provide a close match to the UV colors so long as the assumed dust law does not have any extreme features such as the excess of absorption at 2175 Å or the almost broken power-law rise in the far UV of the Pei (1992) extinction curve. For example, we found similar results when calculating β from the best-fit SED when we allow the shape of the dust law to vary as a new parameter in §5.

3. MODELING STELLAR POPULATIONS

The bulk of the methods and procedures of the SED fitting are described by Salmon et al. (2015), which we summarize here including recent changes. The SED fitting is Bayesian in nature, offering a mechanism to determine the conditional probability for each desired physical property of the galaxy.

3.1. Bayesian Methods

Using Bayes’ theorem,

$$P(\Theta'|D) = P(D|\Theta') P(\Theta')/P(D), \quad (2)$$

we determine the posterior, $P(\Theta'|D)$, with parameters $\Theta' = (\Theta\{t_{\text{age}}, E(B - V), Z\}, M_{\star})$ and data, D , under the *a priori* probability of the parameters or simply the “prior”, $P(\Theta')$. The likelihood, $P(D|\Theta')$, is determined in the usual way using χ^2 statistics (i.e., equation 2 of Salmon et al. 2015). The unconditional marginal likelihood of the data, $P(D)$, often referred to as the Bayesian evidence², normalizes the posterior such that the integrated posterior across all parameters is equal to unity (Jeffreys 1961; Heckerman 1995; Newton et al. 1996):

$$\text{Bayesian evidence} \equiv P(D) = \int_{\Theta} P(D|\Theta) P(\Theta) d\Theta. \quad (3)$$

² The Bayesian evidence is occasionally denoted by Z . We adopt the formal definition, $P(D)$, to avoid confusion with the conventional astronomical symbol of metallicity.

Calculating the unconditional marginal likelihood is a way to eliminate the parameters Θ from the posterior (in Equation 2) through integration, leaving us with the probability of seeing the data D given all possible Θ (Kass & Raftery 1995). The importance of the marginal likelihood will be discussed further in §4.

Posteriors on individual parameters can be determined by marginalizing over nuisance parameters. The strength of this Bayesian approach is that the marginal probability of a given parameter is conditional to the probability from the nuisance parameters. For example, the posterior on $E(B - V)$ is conditional to the probability contribution from all stellar population ages, metallicities, and star-formation histories. This approach is an alternative to using parameter results taken from the best-fit (minimum χ^2) model SED because it relies on posterior integration instead of likelihood maximization. The disadvantage of the latter is that small differences in χ^2 or an underrepresentation of measurement uncertainties can result in best-fit models that are sporadic across the parameter space, making results highly dependent on the SED template assumptions (see Figures 20 and 21 of Salmon et al. 2015). We therefore favor using the median of each parameter’s marginalized posterior over results determined from the best-fit model, as supported by recent literature (Song et al. 2015; Tanaka 2015; Smith & Hayward 2015).

3.2. Stellar Population Models

Table 1 shows the ranges, quantities, and priors of the SED fitting parameters. Each combination of age, metallicity, and $E(B - V)$ produces an SED shape and associated χ^2 . The parameter space is constructed following the listed priors on each parameter. We used Bruzual & Charlot (2003) stellar population synthesis models with the addition of nebular emission lines assuming an ionizing continuum escape fraction of $f_{\text{esc}}=0$ (Salmon et al. 2015). We assumed a Salpeter (1955) initial mass function and H I absorption from line-of-sight IGM clouds according to Meiksin (2006). The Meiksin (2006) IGM attenuation model includes higher order Ly-

man transitions. Nevertheless, the assumption of IGM attenuation has minimal effect on the results because few galaxies have photometry covering wavelengths blueward of 1216 Å.

The range of $E(B - V)$ extends below zero for two reasons. First, consider the example where a Gaussian-shaped posterior for parameter x peaks at $x = 0$, but all probability at $x < 0$ is set to zero. The x corresponding to the median probability of such a posterior would be biased to $x > 0$, an artifact of the choice of parameter space. This was pointed out by Noll et al. (2009), who showed a bias to Bayesian estimates of certain parameters, especially parameters such as $E(B - V)$ whose posterior often peaks at the edge of the parameter space. Second, negative values of $E(B - V)$ are not necessarily unphysical. There are some, albeit rare, situations where isotropic scattering by dust in face-on galaxies can produce an enhancement of optical light (i.e., $A_V < 0$ Chevallard et al. 2013).

We also considered how our results are dependent on the assumed shape of the star-formation history. The star-formation history is known to be a poorly constrained parameter in the fitting process (e.g., Papovich et al. 2001; Noll et al. 2009; Reddy et al. 2012; Buat et al. 2012; Mitchell et al. 2013). While it is not the motivation of this work to accurately fit the star-formation history for individual galaxies, assuming a fixed history may reduce flexibility in the parameter space and overstate the perceived evidence between different dust laws. We therefore considered three scenarios of the star-formation history (SFH): constant, rising, and declining exponentially with cosmic time, with ranges for the latter two cases described in Table 1. We take the assumption of a constant history as our fiducial model, and we show in Appendix B that our main results are unchanged if we instead adopt rising or declining star-formation histories.

The stellar mass is treated differently than the individual parameters Θ . It is effectively a normalization of the SED, given the mass-to-light ratio associated with the SED shape, hence the distinction in §3.1 between Θ , which represents the parameters that actually drive the goodness of fit, and Θ' , which is those parameters and their associated stellar mass. In this manner, the posterior in stellar mass was determined by integrating the posterior rank-ordered by stellar mass to achieve a cumulative probability distribution in stellar mass such that the median is defined where the cumulative probability is equal to 50%.

3.3. Known Dust Attenuation Curves

The dust law was fixed during the fitting process (along with the redshift, escape fraction, and star-formation history), although we individually considered a variety of commonly used dust laws. The curves of these dust laws are shown in Figure 2 and include those of the empirically derived attenuation for local starburst galaxies (Calzetti et al. 2000), the Milky Way extinction (which showcases the strong 2175 Å dust absorption feature, Gordon et al. 2003), an empirically derived attenuation for $z \sim 2$ star-forming galaxies (“MOSDEF”, Reddy et al. 2015), and two interpretations of the SMC extinction: SMC92 (Pei 1992) and SMC03 (Gordon et al. 2003), hereafter.

In Figure 3, several dust attenuation and extinction

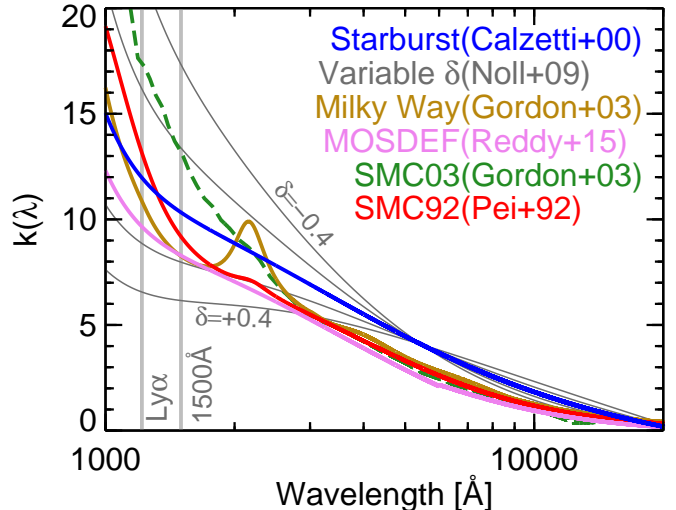


Figure 2. A variety of common dust laws shown by their total-to-selective extinction or attenuation as a function of wavelength. The Pei (1992) derivation of the SMC extinction (red, SMC92) will be used in this work to compare to the starburst prescription derived by Calzetti et al. (2000) (blue). Other dust laws are also shown including the MOSDEF (pink) attenuation curve derived from $z \sim 2$ galaxies (Reddy et al. 2015), and the Milky Way (green) and SMC (SM03, black dashed) extinction curves derived by Gordon et al. (2003). In addition, we consider a power-law deviation to the starburst curve by Equation 7 to be more (+ δ) or less ($-\delta$) grey. The wavelengths of 1500 Å and the Lyman α emission line are shown for reference.

laws from Figure 2 are shown on the plane of infrared excess, IRX , and UV slope, β . Each dust law’s $IRX - \beta$ relation represents the predicted location of a variety of stellar populations that have been reddened according to their given dust-attenuation or dust-extinction curve. Creating these relations requires several assumptions about the intrinsic stellar populations, which manifest as an increase in the relation’s width. First, we obtained a library of BC03 stellar populations with a range of ages (50 Myr to 1 Gyr), star-formation histories ($SFR \sim e^{t/\tau}$, where $1 \text{ Gyr} < \tau < 100 \text{ Gyr}$), and metallicities ($0.02 Z_{\odot} < Z < 2.5 Z_{\odot}$). Then, we subtracted the dust attenuated SED from the intrinsic SED and integrated the residual across all wavelengths to obtain an estimate of the bolometric IR luminosity for these models. We made the approximation that the calculated IR luminosity of each model is representative of L_{TIR} , under the assumption that all attenuated UV-to-NIR light is completely reprocessed to produce the total IR luminosity. L_{UV} was calculated as the average luminosity in a 100 Å box filter centered at 1500 Å. Finally, β was calculated for these models from a power-law fit to the spectral windows defined by Calzetti et al. (1994).

From this framework, each dust model in Figure 3 has a width in the $IRX - \beta$ plane which is a product of the range in the stellar population parameters (age, metallicity, star-formation history), which affects both IRX and β and produce the scatter illustrated by the colored swath. The left edge represents younger, low-metallicity, and maximally blue stellar populations, while the right edge extends towards older, metal-rich, and intrinsically red stellar populations. With increasing steps of $E(B - V)$ (moving up each $IRX - \beta$ relation), a steeper dust law will redden the SED faster and there-

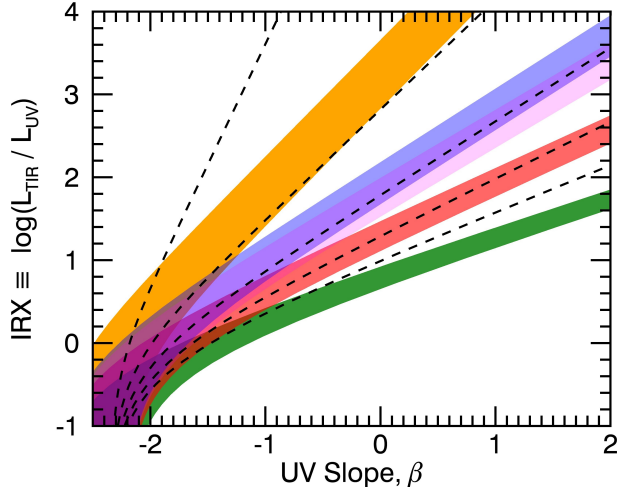


Figure 3. The predicted locations of galaxies with different dust laws on the plane of the UV slope β and infrared excess ($L_{\text{TIR}}/L_{\text{UV}}$). The colored swaths correspond to the same dust laws as in Figure 2, clockwise from top left: Milky Way, starburst, MOSDEF, SMC92, and SMC03. The width of each $IRX - \beta$ relation accounts for the scatter in the intrinsic β from the effects of stellar population age (50 Myr to 1 Gyr), SFH ($\text{SFR} \sim e^{-t/\tau}$, with 1 Gyr $< \tau < 100$ Gyr), and metallicity ($0.02 Z_{\odot} < Z < 2.5 Z_{\odot}$). The dashed lines show the relations according to the parameterized dust law (see §5) with (clockwise from left) $\delta = +0.4, +0.2, 0.0, -0.2, \text{ and } -0.4$.

fore produce less IRX at a given β when compared to greyer, starburst-like dust laws (Siana et al. 2009). In addition, the presence of a 2175 Å dust absorption feature, such as is found in the Milky Way dust law, will produce a significant excess of IR emission without significantly contributing to the reddening (although this depends on the manner in which β is determined, see Kriek & Conroy 2013). These $IRX - \beta$ relations provide an observational basis with which to distinguish between dust-attenuation curves.

4. DISTINGUISHING BETWEEN DUST LAWS WITH BAYES FACTORS

Determining the shape of the dust-attenuation curve from broadband data is nontrivial. Broadband SED fitting is fraught with parameter degeneracies, a product of several physical mechanisms that conspire to produce similar SED shapes (e.g., stellar population age, metallicity, star-formation history, and dust attenuation; e.g., Papovich et al. 2001, 2011; Lee et al. 2010, 2011; Walcher et al. 2011; Pacifici et al. 2012; Pforr et al. 2012, 2013; Mitchell et al. 2013). As mentioned in §3, these degeneracies spawn biases in simple χ^2 likelihood-ratio tests because best-fit models are more sensitive to SED template assumptions such as the inclusion of nebular emission lines, changing the assumed dust curve, and/or the degeneracies within the parameters themselves (Tilvi et al. 2013; Salmon et al. 2015).

To distinguish between dust laws, we should consider all parameters, Θ , as nuisance parameters, such that the fully marginalized parameter space contains probability contribution from all Θ . We are then left to quantify the difference between the fully marginalized posteriors under their respective assumptions of non-parametric dust laws. In order to achieve this, we consider the posterior in Bayes theorem (Equation 2) as being further conditional

to a model assumption exterior to the fitting process (in this case, the assumed dust-attenuation curve, k_{λ}). Then we may determine the odds that the hypothesis of one dust-attenuation curve is correct over another. The ratio of a posterior assuming dust-attenuation curve k_{λ}^1 and a posterior assuming dust-attenuation curve k_{λ}^2 is therefore given by,

$$\frac{P(\Theta', k_{\lambda}^1 | D)}{P(\Theta', k_{\lambda}^2 | D)} = \frac{P(D | \Theta', k_{\lambda}^1)}{P(D | \Theta', k_{\lambda}^2)} \times \frac{P(\Theta' | k_{\lambda}^1)}{P(\Theta' | k_{\lambda}^2)}, \quad (4)$$

or posterior odds = Bayes factor \times prior odds.

The term in the middle is referred to as the Bayes factor (Jeffreys 1935, 1961; Kass & Raftery 1995). In practice, we may write the Bayes factor as a ratio of the marginal likelihood (see Sutton & Abrams (2001) for a similar definition). Combining the definition in Equation 3 with the conditions in Equation 4, we obtain the plausibility that one dust-attenuation curve is more likely given another, marginalized over all parameters:

$$\text{Bayes factor} \equiv B_{12} = \frac{P(D | k_{\lambda}^1)}{P(D | k_{\lambda}^2)} \quad (5)$$

Kass & Raftery (1995) offered descriptive statements for Bayes factors in order to denominate several standard tiers of scientific evidence. These were defined using twice the natural logarithm of the Bayes factor, which we will call the Bayes-factor evidence, ζ :

$$\begin{aligned} \text{Bayes-factor evidence} &\equiv \zeta = 2 \cdot \ln B_{12} \\ \zeta &= 2 \cdot \ln \frac{\int_{\Theta} P(D | \Theta', k_{\lambda}^1) P(\Theta' | k_{\lambda}^1) d\Theta}{\int_{\Theta} P(D | \Theta', k_{\lambda}^2) P(\Theta' | k_{\lambda}^2) d\Theta}. \end{aligned} \quad (6)$$

We adopt the significance criteria of Kass & Raftery (1995), who define the evidence to be “very strong” ($\zeta > 10$), “strong” ($6 < \zeta < 10$), or “positive” ($2 < \zeta < 6$) towards k_{λ}^1 (and equivalent negative values for evidence towards k_{λ}^2). Intuitively, because the Bayesian evidence, $P(D)$, is proportional to the integral over the likelihood (Equation 3), a model that produces a better fit to the data (low χ^2) will yield a higher $P(D)$, making $|\zeta|$ larger in the case that one dust law is more likely than another.

Throughout this paper, we refer to galaxies with high $|\zeta|$ as having strong Bayes-factor evidence towards a given dust law. However, we caution that Bayes factors do not necessarily mandate which of two models is correct but instead describe the evidence against the opposing model. For example, a galaxy with very strong evidence towards model 2 (e.g., $\zeta \approx -20$ according to equation Equation 6), promotes the *null hypothesis* that model 1 is correct. Formally, it does not say the model 2 is the correct model (and vice versa). In the next section, we address this subtlety with a direct parameterization of the dust-attenuation curve in order to confirm if the Bayes-factor evidence is indeed pointing towards the appropriate dust prescription.

5. PARAMETERIZING THE DUST LAW

While it is instructive to search for the evidence that galaxies have one of the empirically or physically motivated dust laws from §3.3, there is no guarantee that

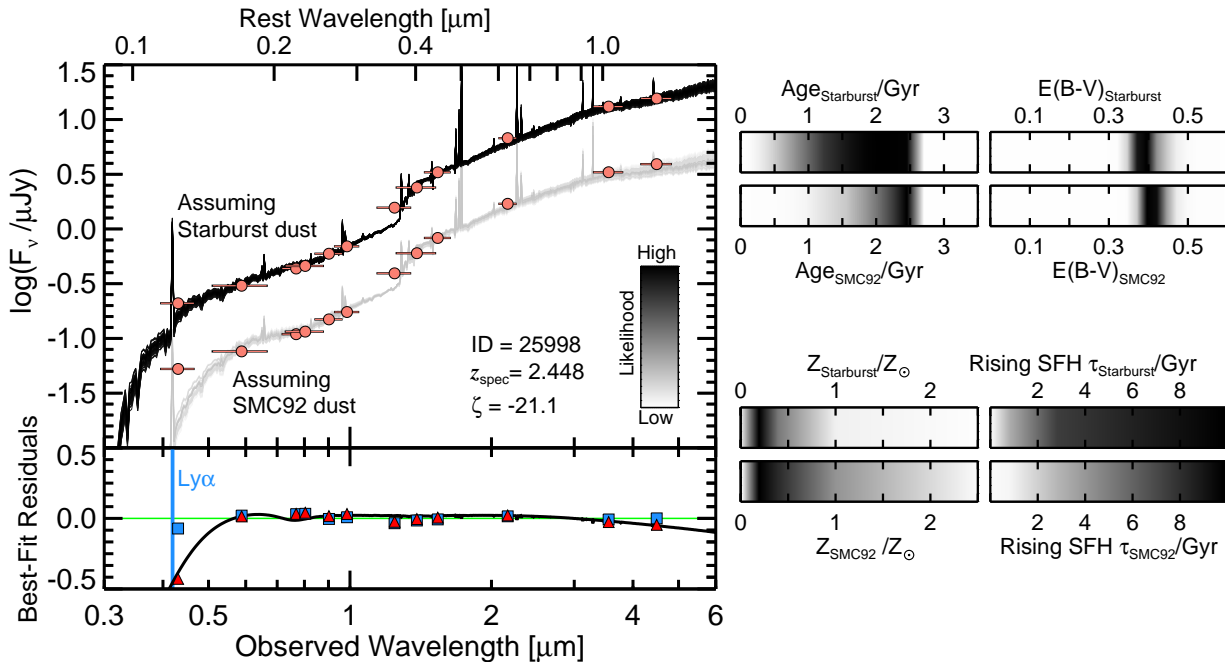


Figure 4. The SED of a galaxy in our spec- z sample with strong Bayes-factor evidence ($\zeta = -21$) towards a starburst-like attenuation. The salmon-colored photometric data points are shown twice, with the second set offset by 0.6 dex for clarity. The 50 most likely SEDs are shown, scaled in opacity such that darker curves represent higher likelihood up to the best-fit model, under an assumed starburst (upper) or SMC92 (lower) dust law. The black curve in the lower panel shows the log-difference residual of the best-fit SED under each dust assumption, and the average residual of the data and the 50 best-fit starburst (SMC92) model fluxes in blue squares (red triangles). The residual of the best-fit SEDs are shown in the lower panel. The bars to the right show the marginalized posteriors of individual parameters, with darker regions denoting higher likelihood. For galaxies with very red SEDs across rest-frame $\lambda = 0.2 - 2 \mu\text{m}$ (the inferred $E(B - V)$ is high) the UV-steep SMC92 dust law is incapable of producing high-likelihood models that match both the $B_{435} - V_{606}$ color and the red rest-frame NIR color. This leads to the large difference in Bayesian evidence and the low Bayes-factor evidence, ζ .

these dust laws apply to all galaxies, particularly at high-redshifts. We therefore adopted an alternative model for the dust attenuation, where we parameterize the dust law in the SED-fitting process. The parameterization allows a smooth transition between the different dust laws. Following Kriek & Conroy (2013), we allow the dust-attenuation curve to vary as a deviation in slope from the starburst curve of Calzetti et al. (2000), following the parameterization provided by Noll et al. (2009). The change in slope, which is a purely analytical interpretation of how the dust-attenuation curve may be adjusted, is applied by multiplying the starburst curve by a power law:

$$A_{\lambda, \delta} = k_{\lambda}^{\text{SB}} (\lambda/\lambda_{\text{V}})^{\delta} \quad (7)$$

This definition returns the starburst attenuation curve, k_{λ}^{SB} , when $\delta = 0$, a steeper, stronger attenuation in the FUV when $\delta < 0$, or a flatter, greyer attenuation across UV-to-NIR wavelengths when $\delta > 0$. Examples of these dust laws are shown in Figure 2. In comparison, SMC92 is slightly steeper than the starburst curve across UV-to-NIR wavelengths, similar to $\delta \approx -0.1$, but is much steeper at FUV ($\lambda \lesssim 1500 \text{ \AA}$) wavelengths, similar to $\delta \approx -0.5$.

Given the set of dust laws, we can marginalize over all other parameters Θ , to obtain the posterior on δ for each galaxy. This process is the same as the marginalization in Equation 3, where we marginalize over all Θ to obtain the full marginal likelihood, except that we have added an additional parameter δ . In some cases δ may be poorly constrained, and the posterior will be very broad. This is to be expected, as there is similarly a population

of galaxies for which the Bayes factor is unable to return significant evidence. The results of fitting to δ are described in §6.2.2 and 6.3.2.

Equation 7 assumes there is no additional contribution from the 2175 Å absorption feature, which is a hallmark of the Milky Way dust-attenuation curve (Gordon et al. 2003) and is likely caused by absorption from polycyclic aromatic hydrocarbons. Although there is evidence of the 2175 Å feature in high-redshift quasars (Notaerdame et al. 2009), gamma ray burst host galaxies (Elíasdóttir et al. 2009), and star-forming galaxies (Noll et al. 2007; Buat et al. 2011), its strength and prevalence in distant galaxy populations remains uncertain (Buat et al. 2012). The photometric data used in this work lacks the wavelength resolution to confirm the presence of the dust bump in our sample.

6. THE NON-UNIVERSALITY OF DUST LAWS AT $z \sim 2$

6.1. Relevant Spectral Features

Figure 4 shows the SED of a single galaxy in the spec- z sample that has strong Bayes-factor evidence promoting a starburst dust-attenuation law. The SED features that drive the differences in likelihood between the two dust assumptions are subtle. In general, the rest-frame UV flux ($1200 \text{ \AA} \lesssim \lambda \lesssim 1400 \text{ \AA}$), which at the redshift range of this work is either the B_{435} or V_{606} filter, catches the wavelength where the dust laws differ the most. For galaxies like the example in Figure 4, the rest-frame optical-to-NIR SED suggests a highly attenuated stellar population (high $E(B - V)$), yet the flux from the rest-frame FUV band is brighter than the pre-

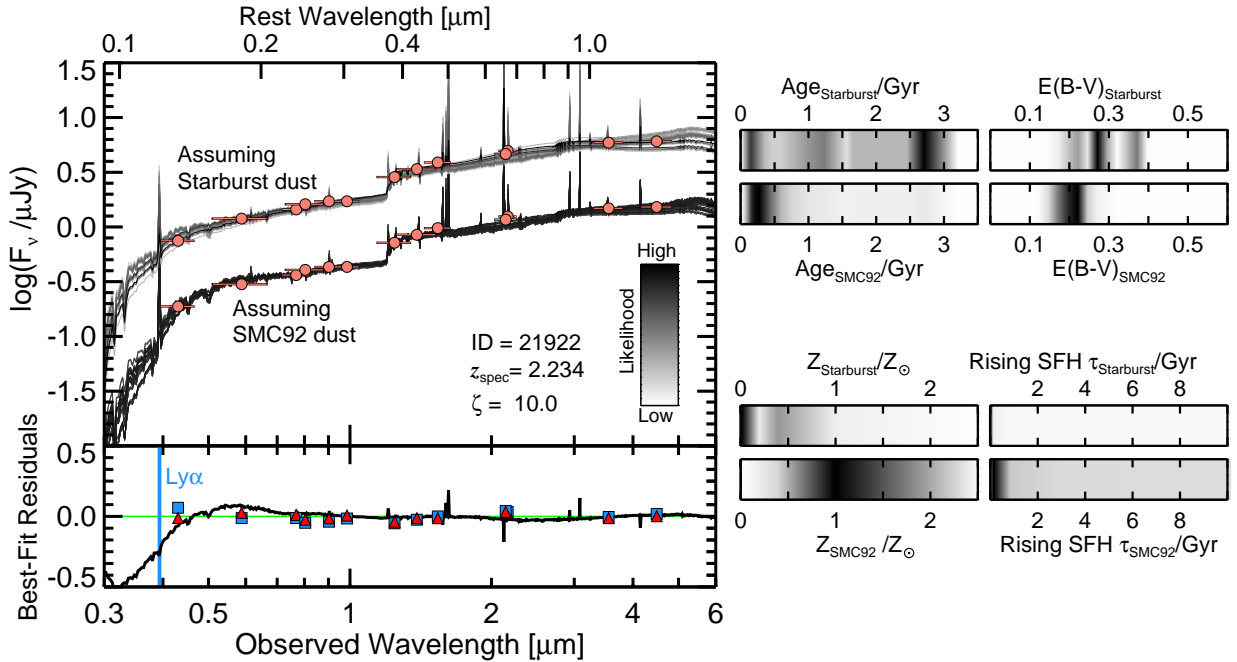


Figure 5. Same as Fig. 4 but for a galaxy that has strong Bayes-factor evidence ($\zeta = 10$) towards an SMC92-like dust-attenuation law. The data is shown twice for fits under each dust assumption, offset by 0.6 dex for clarity. The results between assuming starburst and SMC92 attenuations are subtle; when most of the SED (rest-frame $\lambda = 0.2 - 2 \mu\text{m}$) suggests relatively low values of $E(B - V)$, the assumption of a starburst law does not produce as many models with significant likelihood as the SMC92 law capable of reproducing both the red $B_{435} - V_{606}$ color and the rest-frame NIR color. The resulting difference in likelihood is reflected in the Bayes-factor evidence, ζ .

diction when assuming SMC92 dust. This results in a lower likelihood for SMC92 models compared to models that assume starburst dust. This is true even when accounting for the contribution from $\text{Ly}\alpha$ emission in the models or variations to the assumed star-formation history. The likelihood difference, when marginalized over all parameters, is reflected in the Bayes-factor evidence.

Figure 5 shows the SED of a single galaxy in the spec- z sample that has strong Bayes-factor evidence promoting an SMC92 dust-extinction law. For this galaxy, the rest-frame optical-to-NIR SED suggests a stellar population with relatively low levels of attenuation (low $E(B - V)$). However, there is a subtle decrease in the rest-frame FUV emission, which the starburst attenuation has difficulty matching simultaneously with the rest of the SED, resulting in less overall likelihood as compared to the SMC92 assumption. Again, this likelihood difference is reflected in the Bayes-factor evidence.

One potential alternative explanation for the shape of these SEDs is a two-component stellar population: a young burst of star formation producing O- and B-type stars that dominate the rest-frame UV and an already present intermediate-age population that dominates the rest-frame optical-to-NIR SED. As shown in the single-parameter likelihood distributions of Figures 4 and 5, the exponential star-formation history is a poorly constrained parameter with this dataset. Folding in additional SFH parameters will require a data with a higher wavelength resolution of the SED in order to overcome its degeneracies with age, metallicity, and the slope and scale of dust attenuation. Therefore we leave a deeper exploration of the SFH and, in general, an increased parameterization of galaxy SEDs for a future consideration.

6.2. Results from the Spectroscopic Redshift Sample

6.2.1. Bayes Factors on the $\text{IRX} - \beta$ Relation: spec- z sample

Figure 6 shows the selection of Bayes-factor evidence for individual galaxies as a function of stellar mass. As expected, most galaxies lack enough evidence from their broadband data alone to distinguish their underlying dust law. However, there are examples of galaxies that display strong evidence towards having an SMC-like or starburst-like attenuation. Figure 6 also shows the plane of $\text{IRX} - \beta$, where the total infrared luminosities were calculated as described in §2.5, and β in §2.6. As noted in Figures 4 and 5, the band closest to the $\text{Ly}\alpha$ is the most sensitive to determining the evidence towards a given dust law because it is at the wavelength where the dust prescriptions differ the most.

The Bayes-factor evidence for different dust laws among is consistent with the galaxies' positions in the $\text{IRX} - \beta$ plane. The Bayes-factor evidence is derived from the rest UV-to-NIR photometry and shows that some galaxies have very strong evidence against the starburst law or SMC92 law. Those same galaxies have $\text{IRX} - \beta$ measurements consistent with the Bayes-factor evidence. This is significant because the L_{TIR} data provide an independent measure on the dust law.

Though the results of Figure 6 seemingly identify galaxies with two types of underlying dust scenarios, we must recognize the possibility that neither dust-attenuation curve is appropriate, even for some of the strongest evidence objects. In the next section, we pursue this possibility using the methods described in §5 to parameterize the dust-attenuation curve as a new variable in the fitting process.

6.2.2. Fitting the Curve of the Dust Law:

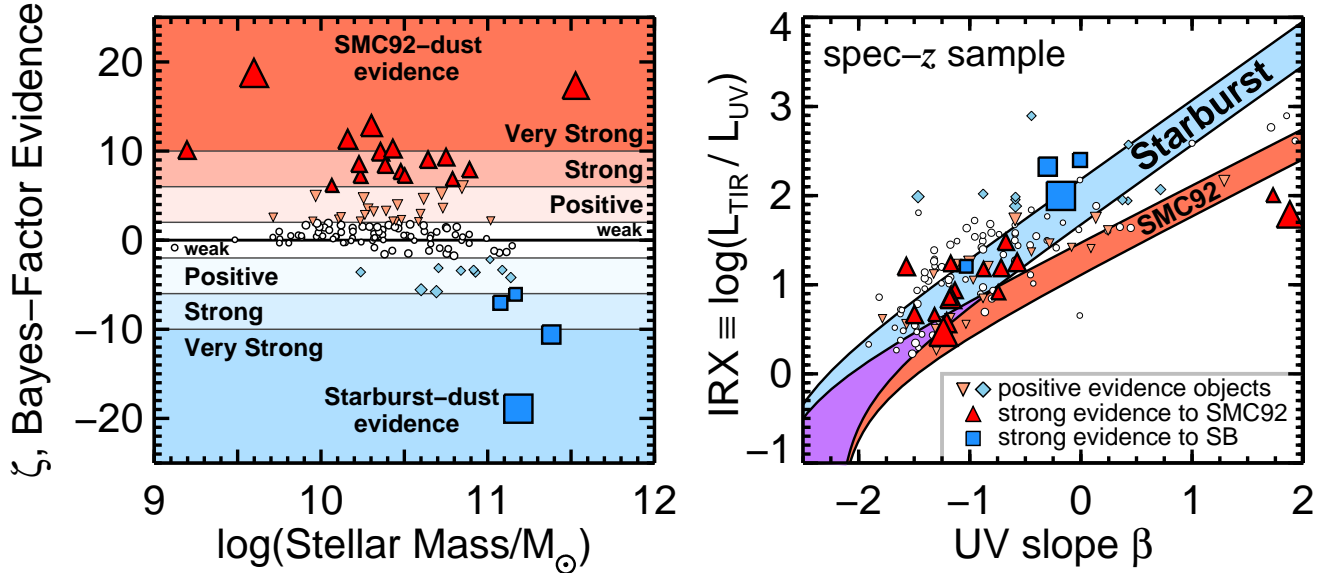


Figure 6. Left: The Bayes-factor evidence as a function of stellar mass for galaxies in the spec- z sample with $1.5 \leq z \leq 2.5$ and MIPS $> 24 \mu\text{m}$ detections of $S/N > 3$. Lighter shaded regions indicate levels of increasing evidence and are used to select objects that show strong preference between SMC92 (red triangles) or starburst (blue squares) dust curves. No mid-IR information was used in the left figure; these values were achieved by modeling rest-frame UV-to-NIR fluxes only. Right: Measured UV slope versus IR excess to test results inferred from the UV/NIR SED. Prediction curves from stellar population models for SMC92 (red) and starburst (blue) dust laws are shown. Objects selected by the strength of their Bayes-factor evidence follow the curve of their predicted dust-attenuation curve with some scatter. The independent measurements of the $\text{IRX} - \beta$ relation supports the Bayesian evidence from the modeling of the UV/NIR SED: galaxies with (very-)strong Bayes-factor evidence follow the correct $\text{IRX} - \beta$ relation.

spec- z sample

Figure 7 shows the results of fitting to the parameterized dust-attenuation curve (Equation 7). The selection of galaxies with strong-evidence towards a starburst-like dust-attenuation curve agrees with the results from fitting to the dust-attenuation curve directly. Similarly, SMC-like galaxies are better described by a steeper dust-attenuation curve ($\delta < -0.2$), albeit at varying degrees. The galaxies selected to have strong evidence towards an SMC92 dust law exhibit a marked steepness in their fitted dust-attenuation curve that contrasts a starburst dust law.

In §4, we mentioned how the Bayes factor is formally promoting the *null hypothesis* of the opposing model. For example, the Bayesian evidence formally does not favor model 1, but provides evidence against the competing model 2 compared to model 1. However, taken together, the results in Figure 7 imply that galaxies with negative δ really do have steeper attenuation curves like that of the SMC92. In this case, we may consider the evidence towards the null hypothesis of the opposing dust law as being the same as positive evidence for the hypothesis of the dust law itself.

One of the main results of this work is seen in Figure 8: there is a strong relation between $E(B - V)$ and δ . Figure 8 shows the derived values of $E(B - V)$ and δ for galaxies with high Bayes-factor evidence. Because both axes are derived quantities with associated posteriors, we combine the posteriors into a two-dimensional posterior for the whole sample. In both cases, a clear trend emerges such that galaxies with steeper, SMC-like dust laws also have lower levels of attenuation, whereas galaxies with high attenuation have greyer, starburst-like dust laws. This correlation agrees with the $\text{IRX} - \beta$ relation in Figure 3; galaxies with low IRX are expected

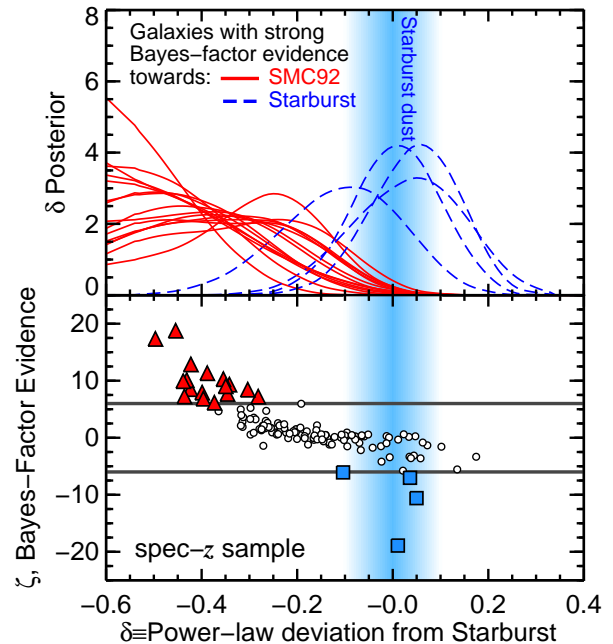


Figure 7. Top: The posterior probability of the fitted parameter δ , the power-law deviation from a starburst (Calzetti et al. 2000) dust-attenuation curve, for galaxies in the spec- z sample and a broadband filter near Ly α . Each curve represents a galaxy that was selected in Figure 6 as having strong Bayes-factor evidence towards an SMC-like (red, solid) or a starburst-like (blue, dashed) dust-attenuation curve. The width of the blue hazed region shows the typical $1-\sigma$ uncertainty in the median value of δ , centered on $\delta = 0$ where a galaxy would have a starburst dust-attenuation curve. Bottom: The evidence from the Bayes factors between the SMC92 and starburst dust laws as a function of the δ posterior median. Symbols and colors are the same as Figure 6. The Bayes factors of galaxies with strong evidence broadly agree with the median δ , as would be expected.

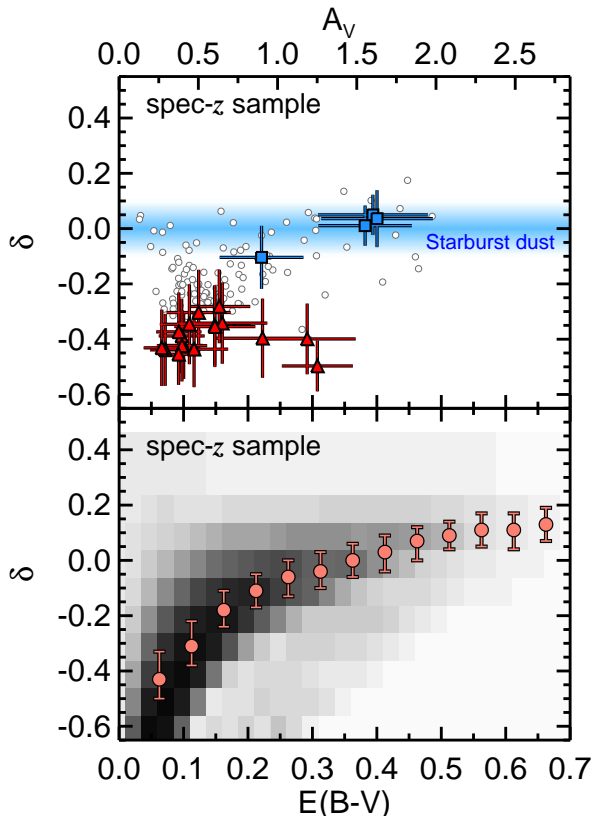


Figure 8. Top: The median of the posterior on the dust-attenuation curve slope, δ , as a function of the median color excess, $E(B - V)$, for galaxies in the spec- z sample. Red triangles and blue squares are galaxies with strong Bayes-factor evidence towards SMC-like and starburst-like dust laws, respectively. Galaxies with low Bayes-factor evidence are shown as open white circles. For reference, a blue haze is shown where δ represents a starburst attenuation, where the width represents typical $1-\sigma$ uncertainties on the posteriors of δ . Bottom: The joint probability between the δ and $E(B - V)$ posteriors. Medians in bins of $E(B - V)$ and their 68% limits are shown as salmon-colored points and error bars respectively. The spec- z sample suggests a relation between the scale of dust attenuation and the dust-attenuation slope, such that galaxies with higher attenuation have a flatter (or grey) starburst-like dust law, and galaxies with relatively lower attenuation have a steeper, SMC-like dust law.

to have steeper dust laws.

6.3. Results from the Photometric Redshift Sample

6.3.1. Bayes Factors on the $IRX - \beta$ Relation: phot- z sample

Figure 9 shows the $IRX - \beta$ plot for the phot- z sample (see §2.3). The phot- z sample includes galaxies from the spec- z sample but with their redshifts assigned to their photometric-redshift value. Figure 9 also shows the results from directly substituting the photometric redshifts for the spec- z sample, in order to explore how photometric-redshift accuracy can effect the main results. In this case, the calculation of the UV slope is also sensitive to the photometric-redshift uncertainty because the bands used to find the slope may differ for large changes in redshift (see the details on the calculation of β in §6.2.1). It is plausible that galaxies in the spec- z sample have better photometric-redshift accuracies than those for the full phot- z sample. However, we assume that the selection bias to the right panel of Figure 9 is

negligible because the trends of Bayes-factor evidence on the $IRX - \beta$ plane are the same for the phot- z sample.

Figure 9 shows that the phot- z sample of this work is able to reproduce the main result derived for the spec- z sample. In most cases, the Bayes-factor evidence promotes the same dust law that the observations suggest, based on their location in the $IRX - \beta$ plane. However, there is significant scatter on an individual galaxy basis, especially for the galaxies that seemingly promote an SMC92 attenuation (or discredit the starburst attenuation). This is to be expected; it is unlikely that all galaxies divide into two specific types of dust laws. For example, the SMC92-favored galaxies may have a range of attenuations that are, in different ways, steeper than the starburst dust law.

6.3.2. Fitting the Curve of the Dust Law: phot- z sample

Figure 10 shows the Bayes-factor evidence of the galaxies in the phot- z sample as a function of their δ posterior median. The median dust-attenuation curve slope, marginalized over all combinations of stellar population age, metallicity, and $E(B - V)$, agrees with the trends suggested by the Bayes-factor evidence. Galaxies with high SMC92 evidence tend to allocate their likelihood around steeper attenuation slopes ($\delta < -0.2$), and galaxies with high starburst evidence allocate towards shallower attenuation slopes ($\delta > 0$).

Figure 10 again shows that the results of the phot- z sample are an extension of the results from the spec- z sample (Figure 8). This figure shows that the steepness of the dust-attenuation curve correlates with the galaxy's attenuation optical depth, as parameterized by the color excess. Galaxies that seem to scatter away from the main trend have poor wavelength coverage of rest-UV wavelengths and have relatively broad posteriors in $E(B - V)$ and δ .

Figure 10 also shows the posterior joint probability between δ and $E(B - V)$ for all galaxies in the phot- z sample. In this depiction, the galaxies with poor constraints on δ or $E(B - V)$, which appear as outliers according to their median posteriors, get suppressed relative to the trend of the whole sample. The distribution shows a probability covariance such that galaxies with low attenuation optical depths have steeper dust laws and are well-fit by the relation

$$\delta = (0.62 \pm 0.05) \log(E(B - V)) + 0.26 \pm 0.02 \quad (8)$$

7. DISCUSSION

7.1. Origins of the relation between $E(B - V)$ and δ

In §5, we use the Noll et al. (2009) parameterization of the dust law, δ , which was an analytically motivated way to change the shape of the dust law. The δ dust laws are defined to tilt at the wavelength of the Johnson V band, meaning they each have an R_V of the starburst law, $R_V=4.07$. However, local dust laws suggest that extinction curves steeper in the UV (e.g., the SMC) have lower R_V . This makes intuitive sense because R_V , in principle, is inversely proportional to the slope of the dust law around $\lambda = \lambda_V$, assuming $k_\lambda \rightarrow 0$ as $\lambda \rightarrow \infty$. Therefore, the single assumption of R_V for all δ dust laws has consequences for the relation in Figure 10. For example, recall that for all stellar population models, the most

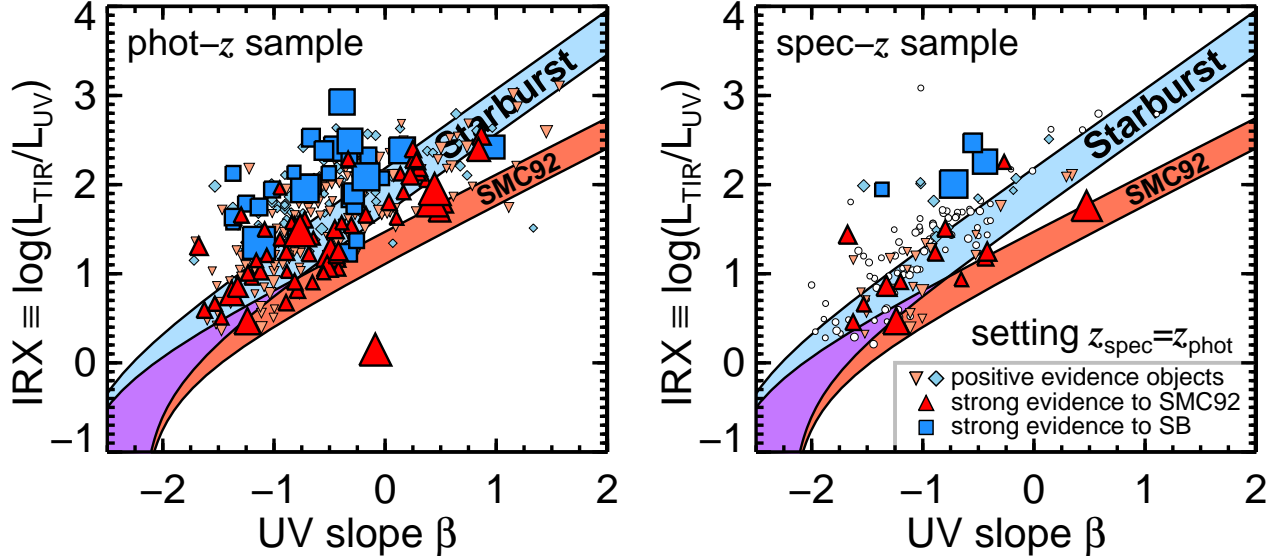


Figure 9. Left: The same as the right panel of Figure 6, but for the phot- z sample (see §2.3). For clarity, only galaxies with positive and strong Bayes-factor evidence are shown, with the symbol size scaling with the evidence. Curves show the predicted location of a variety of stellar populations according to an SMC92 or starburst dust-attenuation law. This panel shows that the galaxies in the phot- z sample selected by the strength of their Bayes-factor evidence follow the curve of their predicted dust-attenuation law with some scatter. Right: The same as the right panel of Figure 6 (galaxies from the spec- z sample), but with β and the Bayes-factor evidence recalculated when the photometric redshift is used for the spec- z sample. This panel shows that the selection methods and Bayes-factor evidence can overcome the errors from photometric-redshift estimates to predict galaxy dust laws, verified by their position in the $IRX - \beta$ plane.

likelihood will always go to the A_λ that best matches the observed broadband flux densities, f_λ . In this sense, our procedure is actually sensitive to the combination of R_V and $E(B - V)$, because $A_\lambda = R_V E(B - V)$. If lower values of δ correspond to lower R_V , then the galaxies in our samples with low δ should have a likelihood shift towards higher $E(B - V)$, and vice versa. If that were the case, then the trend in Figure 10 represents a relation with δ and R_V , not δ and $E(B - V)$. This would still be an interesting result, as R_V has been linked, at least on local scales, to the average dust grain size (Gordon et al. 2000).

Furthermore, the strong relation between $E(B - V)$ and δ is at least partially due to each galaxy’s covariance between those parameters. For example, imagine an SED well represented by some δ and then applying a very small increase in δ towards a flatter dust curve, keeping other parameters fixed. This would produce less attenuation to UV bands, and the models respond by applying more likelihood to higher values of $E(B - V)$ in order to attenuate the UV. This is a known parameter degeneracy that is unavoidable with the current data set. Nevertheless, Figure 6 independently confirms with IR data that the slope of the dust law correlates with the amount of attenuation. Therefore, we leave it to future consideration to explore ways to break the modeling degeneracy between δ and $E(B - V)$ to recover a more robust relationship.

7.2. Physical Origins of Non-Universal Attenuation

The ways that dust grain type, size, and distribution affect the observed UV-to-NIR attenuation are enigmatic. There are many physically motivated explanations for how the relationship between stellar emission and the scattering and absorption by dust manifest to an observed attenuation (Witt & Gordon 2000). One

possible explanation for the change in observed attenuation for different galaxies is their orientation. There is evidence that galaxy inclination correlates with the strength of Ly α emission, such that we observe less Ly α equivalent width for more edge-on galaxies (Charlot & Fall 1993; Laursen & Sommer-Larsen 2007; Yajima et al. 2012; Verhamme et al. 2012; U et al. 2015). Resonant scattering and absorption by dust is likely the primary impediment to the escape of UV light from star-forming regions, which was predicted by Charlot & Fall (1993) to be exacerbated in edge-on galaxies. This qualitatively agrees with radiative transfer simulations that show an increasing attenuation optical depth with galaxy inclination (Chevallard et al. 2013). Therefore, based on physical models, one expects that galaxies with “greyer” dust laws and larger overall attenuation should have higher inclinations, on average.

However, we find no correlation with the scale or shape of attenuation and the axis ratios in either the phot- z or spec- z samples. Figure 11 shows the selection of galaxies in the phot- z sample with strong Bayes-factor evidence. The inset image stamps are a few examples that show similar morphologies among SMC92-like and starburst-like galaxies. Compact red, large axis ratio, and clumpy extended galaxies are found in both samples. A more detailed study with a wider mass range may be needed to find correlations with inclination, axis ratio, or ser-sic index. Alternatively, it may be that neither *HST* or *Spitzer* provides the wavelength coverage with high enough angular resolution to discern the trends between attenuation and morphology. Future observations with *JWST* (with an angular resolution seven times higher than *Spitzer* at similar wavelengths) may be needed to offer spatial insight on the morphology of warm dust regions.

Even if galaxy orientation/inclination correlates with

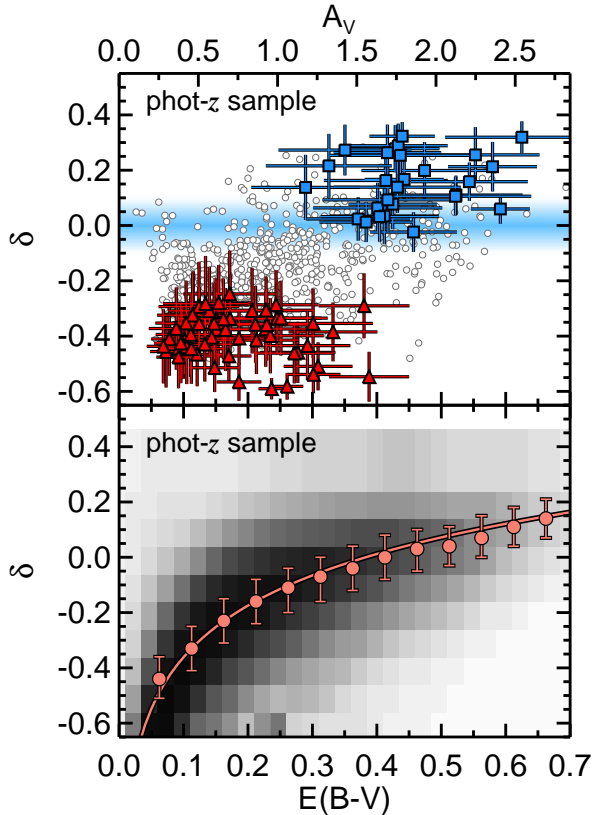


Figure 10. The same as Figure 8 but for the phot- z sample. Top: The medians of the δ and $E(B - V)$ posteriors are shown as grey circles, with strong Bayes-factor-evidence galaxies highlighted as red triangles (SMC92-like) and blue squares (starburst-like). For reference, a blue haze is shown where δ represents a starburst attenuation, given typical uncertainties in δ . Bottom: The joint probability between the δ and $E(B - V)$ posteriors. The salmon-colored circles show the δ at median likelihood in bins of $E(B - V)$ and error bars represent their 68 % range in likelihood. The solid line represents a fit to the medians following Equation 8.

the strength of attenuation, it may not be the fundamental cause of non-universal shapes to the dust-attenuation law. For example, Chevallard et al. (2013) predict the relation between δ and attenuation optical depth at all orientations and assuming only Milky-Way type dust grains. This predicts a physical relationship between the shape of the extinction law (here parameterized by δ) and the dust-attenuation optical depth. We consider this physical relationship in the regime of small and large dust-attenuation optical depths, τ , where the optical depth is related to the color excess by $\tau_\lambda = 0.92 k_\lambda E(B - V)$.

In the low-attenuation scenario, the steep curve of the dust law is likely a product of dust scattering, specifically the asymmetry parameter of the scattering phase function and its dependence with wavelength. The asymmetry parameter, g_λ , describes the degree of scattering in the forward direction Mann et al. (2009). Dust is more forward scattering at UV wavelengths, such that g_λ approaches unity, and more isotropic at optical-to-IR wavelengths, such that g_λ approaches zero (Gordon et al. 1994; Witt & Gordon 2000; Draine 2003). This means that in the small-optical-depth regime, red light will tend to scatter isotropically and escape the galaxy, while blue light will tend to forward scatter until absorption. There-

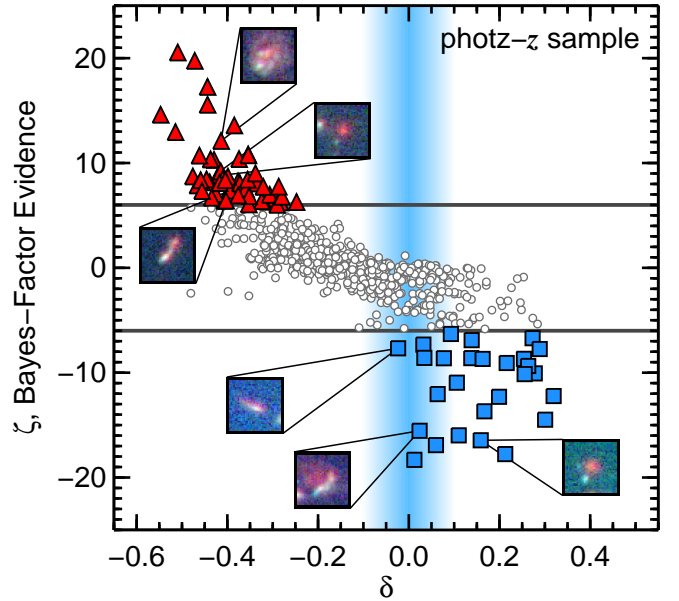


Figure 11. Top: The same as the bottom panel of Figure 7 but for the phot- z sample. Galaxies with strong Bayes-factor evidence are highlighted as red triangles (SMC92-like) and blue squares (starburst-like). Example RGB image stamps (H_{160} , V_{606} , and B_{435} , respectively) of galaxies from both subsamples are shown as insets. This figure demonstrates that there are no distinct morphological trends with δ or Bayes-factor evidence.

fore, relatively more optical-to-IR light and less UV light escapes the galaxy, resulting in a steepening of the curve of dust-attenuation ($\delta < 0$). This only applies at small optical depths where light has a chance to scatter out of the galaxy before absorption.

Also in the low-attenuation scenario, dust is more transparent and scattering is less frequent, so the scattering asymmetry parameter may not be the only source of a steeper dust law. Galaxies with smaller dust optical depths may have steeper dust laws because they produce less scattering into the line of sight, causing the galaxy's dust-attenuation law to appear more like a dust-extinction law. In that case, the effects of dust grain size and composition become more pronounced. For example, the steepness of the SMC extinction law has been attributed to its observed underabundance of carbon, which implies fewer heavy-element graphite grains than silicate interstellar grains (Prevot et al. 1984). This picture is consistent with the trend of finding galaxies with more SMC-like dust at very high redshifts (e.g., $z > 5$ by Capak et al. 2015), where the metallicity of galaxies, in a broad sense, is expected to be lower (Madau & Dickinson 2014). The low δ for small $E(B - V)$ in this work can, at least in part, be attributed to lower R_V . Thus, the relation between $E(B - V)$ and δ could be a product of underlying relations in grain size or composition, averaged over the surface brightness of the galaxy.

In the regime of large attenuation optical depths, attenuation becomes ubiquitous with wavelength. The flatter curve of the dust-attenuation law resulting from high attenuation is consistent with the picture proposed by Charlot & Fall (2000) whereby galaxies have a mixed distribution of stars and dust. In this case, any escaping UV light must come from regions of small optical depth,

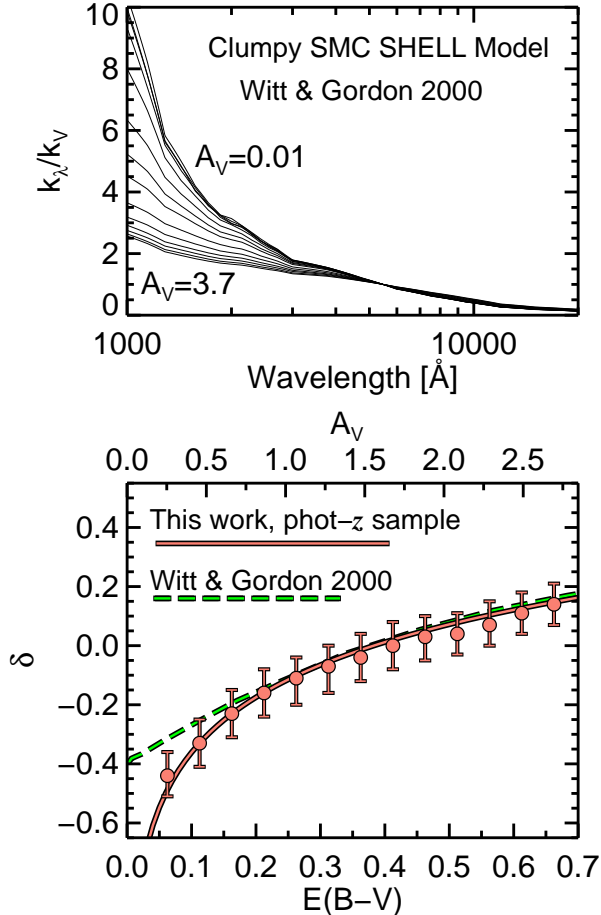


Figure 12. Top: attenuation curves from the radiative transfer calculations by Witt & Gordon (2000) assuming SMC-like dust grains, a clumpy density distribution, and a spherical shell geometry. Bottom: The relation between $E(B - V)$ and δ from Figure 10. The salmon-colored circles show the δ at median likelihood in bins of $E(B - V)$ and error bars represent their 68 % range in likelihood. The solid line represents a fit to the medians following Equation 8. The dashed green line represents radiative transfer predictions from the above dust-attenuation models.

which corresponds to UV light at the outer “skin” of the mixed distribution (Calzetti 2001). Conversely, redder light will come from deeper physical locations within the region. The resulting attenuation function is grey, or flatter with wavelength, which translates to $\delta \geq 0$.

7.3. Comparison with Dust Theory

Figure 12 shows the predictions from radiative transfer calculations by Witt & Gordon (2000). In general, the curves of dust-attenuation become greyer at increasing optical depths for models assuming SMC-like dust grains, a clumpy density distribution, and a spherical shell geometry. We determine δ for each curve using the definition in Equation 7 and compare its evolution with $E(B - V)$ to the results of Figure 10. The steepest curves in Figure 12 are poorly represented by the δ parameterization (their curvature is higher than a power-law can reproduce), which explains the disagreement between $E(B - V)$ and δ at the low end. The radiative transfer relations at high and low attenuation optical depths scenarios are consistent with the observed correlation between $E(B - V)$ and δ found in this work.

Although the agreement in Figure 12 seems obvious given the prevalent predictions of dust theory (Bruzual et al. 1988; Witt et al. 1992; Gordon et al. 2001; Charlot & Fall 2000), radiative transfer simulations (Witt & Gordon 2000; Gordon et al. 2000; Chevillard et al. 2013), and observations of local nebular regions (Draine & Li 2001; Draine 2003), this is the first time the trend has been found from only UV-to-NIR broadband photometry of distant galaxies. Indeed, investigating origins of the relation between $E(B - V)$ and δ elucidates provocative explanations, as a result of similar correlations in stellar population age, metallicity, and dust grain composition from dust theory.

7.4. Comparisons with Recent Literature

Several studies have noted populations of galaxies that lie off of the nominal Meurer et al. (1999) $IRX - \beta$ relation, suggesting galaxies with younger ages have steeper, SMC-like dust laws (Siana et al. 2009; Reddy et al. 2006, 2010, 2012; Buat et al. 2012; Sklias et al. 2014). Other recent studies find galaxies at high redshift harbor dust laws that, at least in large subsets of their samples, agree with the assumption of a starburst dust law (Scoville et al. 2015; de Barros et al. 2015; Zeimann et al. 2015; Kriek & Conroy 2013). Our results suggest that these studies are not in conflict but provide clues to the overall non-universality of how dust attenuates light in star-forming galaxies. For example, the studies that find evidence for starburst-like dust laws do so with galaxies selected by their strong nebular emission lines (e.g., $H\alpha$ and $H\beta$), by a recent star-formation activity (strong CIV absorption), and/or by SEDs with appreciable reddening, allowing the underlying dust law to be tested. A common thread to these starburst-dust galaxies is their large dust-attenuation optical depths, assuming galaxies with strong nebular features also have high levels of stellar attenuation by dust, averaged over the whole galaxy as foreground screen (see Penner et al. 2015, for a discussion on alternatives to the foreground screen).

The trend with δ and $E(B - V)$ (or with IRX) was also found by Buat et al. (2012) and Kriek & Conroy (2013), while the latter attributed the change in δ more to a change in the strength of $H\alpha$ equivalent width. The difference in this study is the evolution of δ is determined for individual galaxies based on rest-frame UV-to-NIR broadband photometry, giving credence that the methods can be used at even high redshifts.

7.5. Implications for SED-derived properties of galaxies

The determination that individual galaxies at $z \sim 2$ have different dust laws has several implications for determinations of distant galaxy evolution. At relatively low $E(B - V)$ (≈ 0.1), this manifests as a factor of ≈ 2 underprediction in the 1500 \AA luminosity dust correction ($10^{0.4k_\lambda E(B - V)}$), and therefore UV SFR, compared to the $\delta = 0$ starburst assumption. Higher SFRs for SMC92-like galaxies agrees with the determination of stellar population ages: galaxies with an SMC92-like attenuation, are on average half the age of galaxies with a starburst-like attenuation, consistent with the results of previous studies (Siana et al. 2009; Reddy et al. 2010). At the high $E(B - V)$ end ($E(B - V) > 0.6$), UV luminosity dust corrections are overestimated by a factor of 2 – 5 compared to the starburst-dust assumption at fixed $E(B - V)$.

Lastly, the relationship between δ and $E(B - V)$ does not translate to a relationship between the UV spectral slope, β , and the dust law. At fixed β there is high scatter in IRX (see Figures 6 and 9). Even at relative modest UV slopes, $-1 < \beta < 0$, the scatter in L_{TIR}/L_{UV} is more than 1 dex depending on the assumption of the dust attenuation law (Buat et al. 2012). This may have a substantive impact on the interpretation of the intrinsic UV luminosity function if the dust-corrections to the observed UV luminosity densities assume a unique relationship between M_{UV} and β .

8. CONCLUSIONS

We investigate the shape of the dust-attenuation law in star-forming galaxies at $z \sim 2$ in the CANDELS GOODS-N and GOODS-S deep fields. We apply a Bayesian SED-fitting technique to galaxies with spectroscopic and photometric redshifts, and determine the evidence for their underlying dust law and its correlation with other galaxy physical properties. Our results can be summarized as follows:

- IR luminous galaxies at $z \sim 2$ can be characterized by a range of dust laws bounded by two types: (1) A starburst-like (Calzetti et al. 2000) attenuation that is greyer (flatter) across UV-to-NIR wavelengths and (2) a dust law that steepens towards the FUV like the curve of the SMC extinction law (Pei 1992).
- The dust law inferred from rest-frame UV-to-NIR photometry of galaxies is supported by their position along the $IRX - \beta$ relations. This result gives credibility that a Bayesian analysis of rest-frame UV-to-NIR fluxes is capable of broadly distinguishing between dust laws that are grey or steep in the rest-frame FUV.
- The steepness of the dust law, parameterized by a δ power-law deviation from the starburst dust law, is correlated with their color excess, $E(B - V)$, for IR-bright galaxies at $z \sim 2$. Galaxies with lower levels of dust attenuation have dust laws that are steeper in FUV, following $\delta = (0.62 \pm 0.05) \log(E(B - V)) + 0.26 \pm 0.02$
- The relation between $E(B - V)$ and δ is further supported by predictions from radiative transfer. The agreement with dust theory offers possible interpretations for the relation and its origins from different dust production mechanisms. For example, the change in the shape of the dust law may be a result of star-dust geometry, properties of dust grains, and/or stellar population age, emphasizing the non-universality of the dust law in star-forming galaxies.

APPENDIX

A. USING HERSCHEL TO CALCULATE THE TOTAL INFRARED LUMINOSITIES

The determinations of L_{TIR} used in this work come from conversions of $24 \mu\text{m}$ luminosity calibrated by Rujopakarn et al. (2013). However, $\approx 40\%$ of our sample

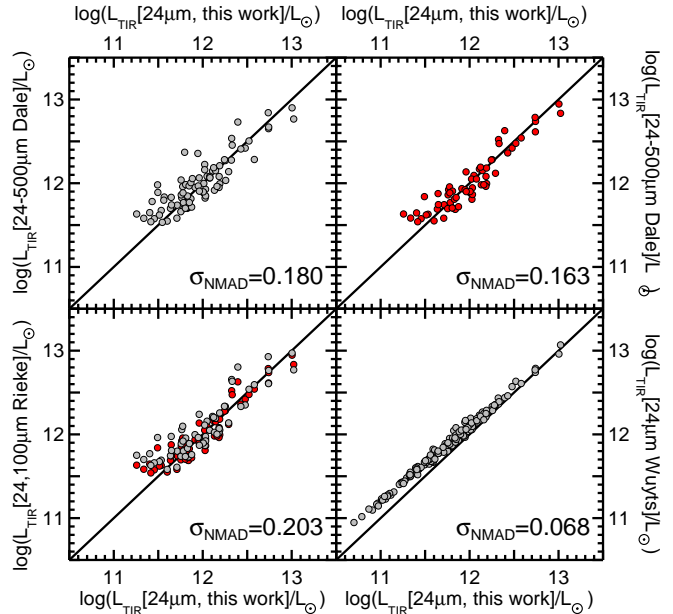


Figure 13. Galaxies in the spec- z sample with *Herschel* PACS and/or SPIRE detections are shown with several determinations of L_{TIR} as a function of the fiducial $24 \mu\text{m}$ method. The top panels assume Dale & Helou (2002) fitting templates for all available FIR detections (top left) or 24 and $100 \mu\text{m}$ only (top right). The bottom left panel assumes Rieke et al. (2009) templates for 24 and $100 \mu\text{m}$ bands (grey), as well the Dale et al. assumption (red). The bottom right panel uses the $24 \mu\text{m}$ conversion to L_{TIR} from Wuyts et al. (2008).

have detections further in the IR, providing the opportunity to internally test our L_{TIR} measurements. We determined L_{TIR} by fitting several different suites of FIR SED templates to the observed MIPS $24 \mu\text{m}$, and/or *Herschel* PACS and SPIRE detections of galaxies in our spec- z sample.

Figure 13 shows several L_{TIR} calculations compared to our fiducial L_{TIR} determined from the $24 \mu\text{m}$ luminosity. We compare fits to Dale & Helou (2002) and Rieke et al. (2009) templates, as well as comparing fits to fluxes at $24 - 100 \mu\text{m}$ only. In addition, we compare the $24 \mu\text{m}$ conversion to L_{TIR} proposed by Wuyts et al. (2008). In all cases, the scatter in determining L_{TIR} is within $\sigma_{NMAD} \approx 0.2$ dex. This scatter is smaller than the correlations in $IRX - \beta$ found in our primary results, and therefore our approximation of $24 \mu\text{m}$ luminosity to L_{TIR} is reasonable.

B. CHANGING THE ASSUMED STAR-FORMATION HISTORY

For the primary results of this work, we used stellar population models that assume a constant star-formation history. However, we must consider if our choice of parameter space is missing models that could mimic the SED-fitting evidence towards certain dust laws. In this appendix, we allow the e -folding timescale (τ), the time interval over which the SFR is increased by a factor of e , to vary as a parameter. We consider SFRs that rise and decline with cosmic time with ranges described in Table 1. We also include the fits to rising histories in Figure 4 and Figure 5 to illustrate that the additional parameter does not create SED shapes that mimic the evidence towards different dust laws.

Figure 14 shows how fitting the spec- z sample with a range of star-formation histories affects the selection of galaxies based off of their Bayes-factor evidence, and how that selection propagates to the $IRX - \beta$ plane. While the distribution of Bayes-evidence shifts under the influence of a new parameter, there are still galaxies with convincing evidence between dust laws. In addition, no galaxy switches evidence from favoring the SMC92-like dust to favoring starburst-like dust or vice versa. We conclude that the evidence between dust laws is not an artifact of different star-formation histories, at least for simple rising and declining τ -models.

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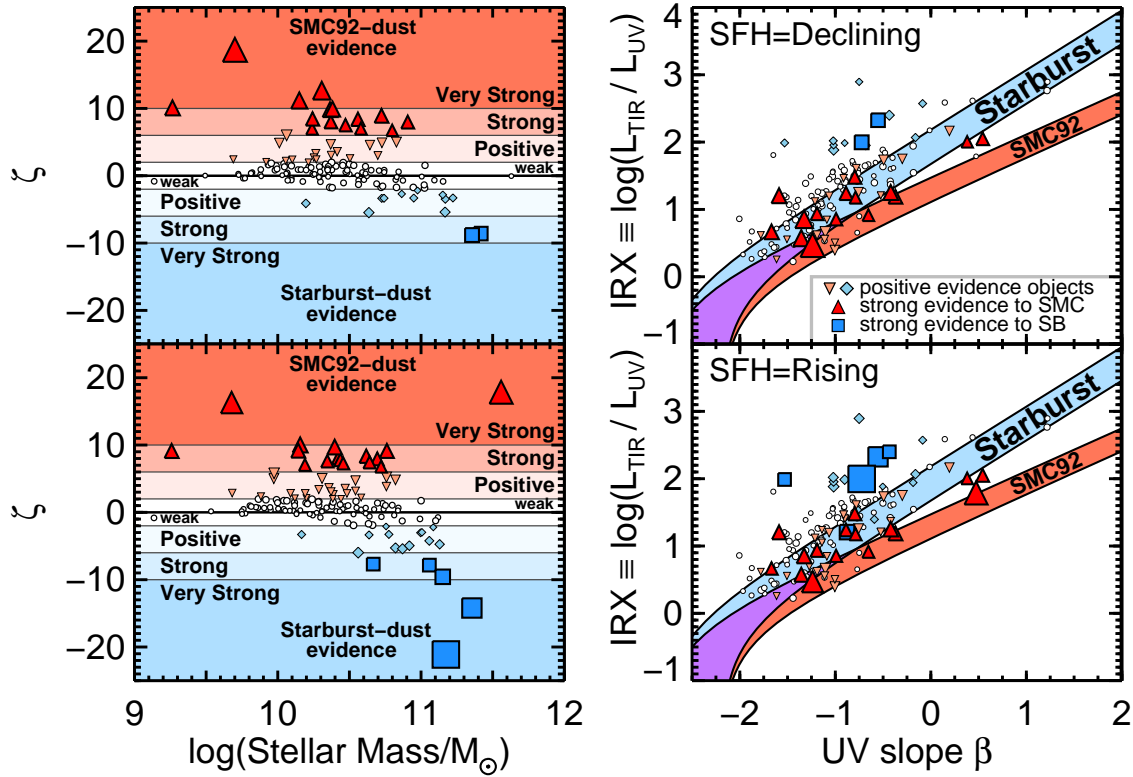


Figure 14. Same as Fig. 6, but allowing the star formation history to vary as fitted parameter for star formation rates that decline (top) and rise (bottom) with time. Several colored tiers indicate the selection of galaxies to have strong Bayes-factor evidence towards an SMC92 (red triangles) or starburst (blue squares) dust law. Although the strength of evidence shifts when allowing the SFH to be free, galaxies only ever lose or gain favorance towards a single dust law; no galaxy changes the direction of its evidence.

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