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## On multifield inflation, adiabaticity, and the speed of sound of the curvature perturbations

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# On Multifield Inflation, Adiabaticity, and the Speed of Sound of the Curvature Perturbations

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On the front cover: View from Utrechtse Veer 22, Leiden, by HIME.

Witrantükuneyenngé chongnoam kitra.

Inhale, deeply, to stop the pipe from going out.

Mapuche proverb



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