Annihilation of Colliding Bogoliubov Quasiparticles Reveals their Majorana Nature

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The single-particle excitations of a superconductor are coherent superpositions of electrons and holes near the Fermi level, called Bogoliubov quasiparticles. They are Majorana fermions, meaning that pairs of quasiparticles can annihilate. We calculate the annihilation probability at a beam splitter for chiral quantum Hall edge states, obtaining a $1 \pm \cos \phi$ dependence on the phase difference ϕ of the superconductors from which the excitations originated (with the $\pm$ sign distinguishing singlet and triplet pairing). This provides for a nonlocal measurement of the superconducting phase in the absence of any supercurrent.

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Condensed matter analogies of concepts from particle physics are a source of much inspiration, and many of these involve superconductors or superfluids [1]. Majorana's old idea [2] that a spin-1/2 particle (such as a neutrino) might be its own antiparticle has returned [3] in the context of low-dimensional superconductors, inspiring an intense theoretical and experimental search for condensed matter realizations of Majorana fermions [4]. The search has concentrated on Majorana zero modes [5–7]—midgap states (at the Fermi level $E = 0$) bound to a defect in a superconductor with broken spin-rotation and time-reversal symmetry (a so-called topological superconductor [8,9]). The name Majorana zero mode (or Majorino [10]) is preferred over Majorana fermion, since they are not fermions at all but have a non-Abelian exchange statistics [11].

Majorana fermions, in the original sense of the word, do exist in superconductors. In fact they are ubiquitous: the time-dependent four-component Bogoliubov–de Gennes wave equation for quasiparticle excitations (so-called Bogoliubov quasiparticles) can be brought to a real form by a 4×4 unitary transformation $\mathcal{U}$ [12], in direct analogy to the real Eddington-Majorana wave equation of particle physics [2,13]. A real wave equation implies the linear relation $\Psi^\dagger(\mathbf{r}, t) = \mathcal{U}\Psi(\mathbf{r}, t)$ between the particle and antiparticle field operators, which is the hallmark of a Majorana fermion. As argued forcefully by Chamon *et al.* [14], fermionic statistics plus superconductivity by itself produces Majorana fermions, irrespective of considerations of dimensionality, topology, or broken symmetries.

Here we propose an experiment to probe the Majorana nature of Bogoliubov quasiparticles in conventional, non-topological, superconductors. Existing proposals apply to topological superconductors [15–25], where Majorana fermions appear as charge-neutral edge states with a distinct signature in DC transport experiments. In contrast, the Bogoliubov quasiparticles of a nontopological superconductor have charge expectation value $\bar{q} \neq 0$, so their Majorana nature remains hidden in the energy domain probed by DC transport.

It is in the time domain that the wave equation takes on a real form and that particle and antiparticle operators are linearly related. We will show that the Majorana relation manifests itself in high-frequency shot noise correlators that can detect the annihilation of a pair of Bogoliubov quasiparticles originating from two identical superconductors (differing only in their phase). These quasiparticles can annihilate for nonzero $\bar{q}$ because of quantum fluctuations of the charge (with variance $\text{var}(q)$). We calculate the annihilation probability $\mathcal{P}$ and find that it oscillates with the phase difference ϕ ,

$$\mathcal{P} = \frac{1}{2}(1 + \cos \phi)\text{var}(q/e). \quad (1)$$

This could provide a way to detect the nonlocal Josephson effect [26], existing in the absence of any supercurrent flowing between the superconductors.

We consider the beam splitter geometry of Fig. 1, in which electrons are injected from two voltage sources at one side of the beam splitter and the fluctuating currents $I_1(t)$ and $I_2(t)$ are correlated at the other side at microwave frequencies $\omega > 0$,

$$P(\omega) = \int_{-\infty}^{\infty} dt e^{i\omega t} \langle I_1(0)I_2(t) \rangle. \quad (2)$$

Such two-particle interferometers have been implemented using the quantum Hall edge channels of a two-dimensional electron gas as chiral (unidirectional) wave guides, to realize the electronic analogues of the Hanbury Brown–Twiss (HBT) experiment [27–29] and the Hong–Ou–Mandel (HOM) experiment [30,31].

The setup we propose here differs in one essential aspect: before reaching the beam splitter, the electrons are partially Andreev reflected at a superconducting electrode. Andreev reflection in the quantum Hall effect regime has been reported in InAs quantum wells [32,33] and in graphene monolayers [34–36]. In graphene, which has small spin-orbit coupling, the Andreev reflected hole is in the opposite

FIG. 1 (color online). Two-particle interferometer for Bogoliubov quasiparticles. Shown is a two-dimensional electron gas in a perpendicular magnetic field (light blue), with chiral edge channels at the edges (arrows indicate the direction of motion and a, b, c_p denote the quasiparticle operators). A constriction at the center forms a beam splitter. Current is injected at the two ends (red), biased at voltages V_1 and V_2 . Upon passing along a superconducting electrode (grey, labeled S), repeated Andreev reflection converts the electrons into a coherent superposition of electrons and holes. The collision and pairwise annihilation of these Bogoliubov quasiparticles is detected by correlating the AC currents I_1 and I_2 .

spin band as the electron (spin-singlet pairing). The strong spin-orbit coupling in InAs permits spin-triplet pairing (electron and hole in the same spin band).

We contrast these two cases by taking a twofold spin-degenerate edge channel for spin-singlet pairing and one single spin-polarized edge channel for spin-triplet pairing. For spin-singlet pairing we therefore need a vector of four annihilation operators $a = (a_{e\uparrow}, a_{e\downarrow}, a_{h\uparrow}, a_{h\downarrow}) = \{a_{\tau\sigma}\}$, to accommodate electrons and holes ($\tau = e, h$) in both spin bands ($\sigma = \uparrow, \downarrow$), while for spin-triplet pairing the two operators $a = (a_{e\uparrow}, a_{h\uparrow})$ suffice. The creation and annihilation operators of these Bogoliubov quasiparticles are related by particle-hole symmetry [37],

$$a(E) = \tau_x a^\dagger(-E). \quad (3)$$

The Pauli matrices τ_i and σ_i act, respectively, on the electron-hole and spin degree of freedom. The anticommutation relations thus have an unusual form,

$$\{a_{\tau\sigma}(E), a_{\tau'\sigma'}^\dagger(E')\} = \delta(E - E')\delta_{\tau\tau'}\delta_{\sigma\sigma'}, \quad (4a)$$

$$\begin{aligned} & \{a_{\tau\sigma}(E), a_{\tau'\sigma'}(E')\} \\ &= \begin{cases} \delta(E + E')\delta_{\sigma\sigma'} & \text{if } \tau, \tau' \text{ is } e, h \text{ or } h, e \\ 0 & \text{otherwise.} \end{cases} \end{aligned} \quad (4b)$$

The nonzero anticommutator of two annihilation operators is the hallmark of a Majorana fermion [14].

The electrical current operator is represented by

$$I(t) = ea^\dagger(t)\tau_z a(t), \quad a(t) = \frac{1}{\sqrt{4\pi}} \int_{-\infty}^{\infty} dE e^{-iEt} a(E). \quad (5)$$

The Pauli matrix τ_z accounts for the opposite charge of electron and hole. (For notational convenience we set $\hbar = 1$ and take the electron charge $e > 0$.) To distinguish the currents I_1 and I_2 , we will denote the quasiparticle operators at contact 2 by a and those at contact 1 by b . The current correlator (2) then takes the form

$$P(\omega) = \frac{1}{4} G_0 \int_{-\infty}^{\infty} dE \int_{-\infty}^{\infty} dE' \int_{-\infty}^{\infty} dE'' \times \langle b^\dagger(E')\tau_z b(E'')a^\dagger(E - \omega)\tau_z a(E) \rangle, \quad (6)$$

with $G_0 = e^2/h$ the conductance quantum.

Using the Majorana relation (3) we can rewrite Eq. (6) so that only positive energies appear [38]. Only products of an equal number of creation and annihilation operators contribute, resulting in

$$\begin{aligned} P(\omega) &= G_0 \int_0^{\infty} dE \int_0^{\infty} dE' \int_0^{\infty} dE'' \\ &\times \langle b^\dagger(E')\tau_z b(E'')a^\dagger(E)\tau_z a(E + \omega) \\ &+ \frac{1}{4}\theta(\omega - E)b^\dagger(E')\tau_y b^\dagger(E'')a(\omega - E)\tau_y a(E) \rangle, \end{aligned} \quad (7)$$

with $\theta(x)$ the unit step function. Both terms describe an inelastic process accompanied by the emission of a photon at frequency ω . The difference is that the term with τ_z is a single-particle process (relaxation of a quasiparticle from energy $E + \omega \mapsto E$), while the term with τ_y is a two-particle process (pairwise annihilation of quasiparticles at energy E and $\omega - E$). The appearance of this last term is a direct consequence of the Majorana relation (3), which transforms $a^\dagger(E - \omega)\tau_z a(E) \mapsto a(\omega - E)\tau_x \tau_z a(E)$.

The quasiparticle operators c_p injected towards the beam splitter by voltage contact $p = 1, 2$ are related to their counterparts a, b behind the beam splitter by a scattering matrix. Since the voltage contacts are in local equilibrium, the expectation value of the c_p operators is known, and in this way one obtains an expression for the noise correlator in terms of scattering matrix elements—an approach pioneered by Büttiker [39] and used recently to describe the electronic Hanbury Brown–Twiss and Hong–Ou–Mandel experiments [40–42].

Our new ingredient is the effect of the superconductor on the injected electrons. Propagation of the edge channel along the superconductor transforms the quasiparticle operators $c_p(E) \mapsto M_p(E)c_p(E)$ through a unitary transfer matrix constrained by particle-hole symmetry,

$$M_p(E) = \tau_x M_p^*(-E)\tau_x. \quad (8)$$

The effect of the beam splitter is described by the unitary transformation

$$\begin{aligned} a &= \sqrt{RM_1}c_1 + \sqrt{1 - RM_2}c_2, \\ b &= \sqrt{1 - RM_1}c_1 - \sqrt{RM_2}c_2. \end{aligned} \quad (9)$$

(For simplicity, we take an energy independent reflection probability R .) The voltage contacts inject quasiparticles in local equilibrium at temperature T and chemical potential $eV > 0$ (the same at both contacts), corresponding to expectation values

$$\langle c_{p,\tau\sigma}^\dagger(E) c_{q,\tau'\sigma'}(E') \rangle = \delta_{\tau\tau'} \delta_{\sigma\sigma'} \delta_{pq} \delta(E - E') f_\tau(E), \quad (10)$$

with electron and hole Fermi functions,

$$f_e(E) = \frac{1}{1 + e^{(E - eV)/k_B T}}, \quad f_h(E) = 1 - f_e(-E). \quad (11)$$

In what follows we focus on the low-temperature regime $k_B T \ll eV$, when only electrons are injected by the voltage contacts: $f_e(E) = \theta(eV - E) \equiv f(E)$, while $f_h(E) = 0$ for $E, V > 0$.

The full correlator (7) decomposes into four terms,

$$P(\omega) = P_{11}(\omega) + P_{22}(\omega) + P_{12}(\omega) + P_{21}(\omega), \quad (12)$$

$$\begin{aligned} P_{pq}(\omega) &= -G_0 R (1 - R) (-1)^{p+q} \int_0^\infty dE f(E) \\ &\quad \times \text{Tr}[f(E + \omega) Z_{pq}(E + \omega, E) Z_{qp}(E, E + \omega) \\ &\quad + \frac{1}{2} \theta(\omega - E) f(\omega - E) Y_{pq}^*(E, \omega - E) \\ &\quad \times Y_{qp}(\omega - E, E)], \end{aligned} \quad (13)$$

$$Z_{pq}(E, E') = \frac{1}{4} (1 + \tau_z) M_p^\dagger(E) \tau_z M_q(E') (1 + \tau_z), \quad (14)$$

$$Y_{pq}(E, E') = \frac{1}{4} (1 + \tau_z) M_p^T(E) \tau_y M_q(E') (1 + \tau_z). \quad (15)$$

The partial correlators P_{11} and P_{22} can be measured separately by biasing only voltage contact 1 or 2, respectively.

The terms P_{12} and P_{21} describe the collision at the beam splitter of particles injected from contacts 1 and 2.

Transfer matrices of quantum Hall edge channels propagating along a superconducting contact (so-called Andreev edge channels) have been calculated in Ref. [43]. Their general form is constrained by unitarity and by the electron-hole symmetry relation (8). A single spin-degenerate Andreev edge channel has transfer matrix

$$M_p = e^{iEt_p} e^{i\gamma_p \tau_z} U(\alpha_p, \phi_p, \beta_p) e^{i\gamma'_p \tau_z}, \quad (16)$$

$$U(\alpha, \phi, \beta) = \exp[i\alpha \sigma_y \otimes (\tau_x \cos \phi + \tau_y \sin \phi) + i\beta \tau_z]. \quad (17)$$

The τ_z terms account for relative phase shifts of electrons and holes in the magnetic field, while the terms $\sigma_y \otimes \tau_x \cos \phi_p$ and $\sigma_y \otimes \tau_y \sin \phi_p$ describe the electron-hole mixing by a spin-singlet pair potential with phase ϕ_p . For a superconducting interface of width W one has $\alpha \simeq W/l_S$ and $\beta \simeq W/l_m$, with $l_m = (\hbar/eB)^{1/2}$ the magnetic length and $l_S = \hbar v_{\text{edge}}/\Delta$ the superconducting coherence length (for induced gap Δ and edge velocity v_{edge}).

The presence of a τ_z term in the electron-hole rotation matrix (17) is inconvenient. With some algebra, it can be eliminated, resulting in

$$M_p = e^{iEt_p} e^{i(\gamma_p + \delta\gamma_p)\tau_z} U(\bar{\alpha}_p, \phi_p, 0) e^{i(\gamma'_p + \delta\gamma'_p)\tau_z}, \quad (18)$$

$$\sin \bar{\alpha}_p = (\alpha_p/\xi_p) \sin \xi_p, \quad \tan 2\delta\gamma_p = (\beta_p/\xi_p) \tan \xi_p. \quad (19)$$

We have abbreviated $\xi_p = (\alpha_p^2 + \beta_p^2)^{1/2}$. Typically one has $l_m \lesssim l_S$, which implies $\bar{\alpha} \simeq (l_m/l_S) \sin(W/l_m)$ and $\delta\gamma \simeq W/2l_m$.

Substitution into Eq. (13) gives the partial correlators

$$\begin{aligned} P_{pq}(\omega) &= -G_0 R (1 - R) (-1)^{p+q} \int_0^\infty dE f(E) \\ &\quad \times \left[f(E + \omega) (g_{pq} + 1) \right. \\ &\quad \left. + \frac{1}{2} \theta(\omega - E) f(\omega - E) (g_{pq} - 1) \right], \end{aligned} \quad (20)$$

$$g_{pq} = \cos 2\bar{\alpha}_p \cos 2\bar{\alpha}_q - \cos \phi_{pq} \sin 2\bar{\alpha}_p \sin 2\bar{\alpha}_q, \quad (21)$$

$$\phi_{pq} = \phi_p - \phi_q - 2(\gamma_p + \delta\gamma_p - \gamma_q - \delta\gamma_q). \quad (22)$$

The phase ϕ_{12} represents the gauge invariant phase difference between the two superconductors. Substituting $f(E) = \theta(eV - E)$, the integral over energy evaluates to

$$\begin{aligned} P_{pq}(\omega) &= -G_0 R (1 - R) (-1)^{p+q} \\ &\quad \times \left[2\Theta(eV - \omega) + \frac{1}{2} \Theta(2eV - \omega) (g_{pq} - 1) \right], \end{aligned} \quad (23)$$

where we have defined the function $\Theta(x) = x\theta(x)$. Substitution into Eq. (12) then gives the full correlator

$$P(\omega) = -\frac{1}{2} G_0 R (1 - R) \Theta(2eV - \omega) (g_{11} + g_{22} - 2g_{12}). \quad (24)$$

In Fig. 2 we compare the collision term $P_{\text{coll}} = 2P_{12}$ and the full correlator $P_{\text{full}} = 2P_{12} + P_{11} + P_{22}$. The linear voltage dependence of P_{full} shown in Fig. 2(a), with a

FIG. 2 (color online). Noise correlator as a function of frequency (a) and as a function of superconducting phase difference (b). Panel a shows both the collision term $P_{\text{coll}} = 2P_{12}$ and the full correlator $P_{\text{full}} = P_{\text{coll}} + P_{11} + P_{22}$, while panel b shows only P_{coll} (the full correlator differs by a phase-independent offset, such that $P_{\text{full}} = 0$ at $\phi_{12} = 0$). The curves are calculated from the general result (23) for spin-singlet pairing, with parameters $\bar{\alpha}_1 = \bar{\alpha}_2 = \pi/4$.

singularity (discontinuous derivative) at $\omega = 2$ eV, is known from two-terminal normal-superconducting junctions [44]. The collision term has an additional singularity at $\omega = \text{eV}$, signaling the frequency beyond which only pairwise annihilation of Bogoliubov quasiparticles contributes to the noise.

Figure 2(b) shows the dependence on the superconducting phase difference of the collision term, for the case of two identical superconductors, $\bar{\alpha}_1 = \bar{\alpha}_2 \equiv \bar{\alpha}$. In the annihilation regime $\text{eV} < \omega < 2$ eV the general formula (23) then simplifies to

$$P_{12}(\omega) = -\frac{1}{2}G_0R(1-R)(2\text{ eV} - \omega) \times (1 + \cos \phi_{12})\sin^2 2\bar{\alpha}. \quad (25)$$

The factor $\sin^2 2\bar{\alpha} = \text{var}(q/e)$ is the variance of the quasiparticle charge, cf. Eq. (1). The annihilation probability is maximal for vanishing phase difference. This “nonlocal Josephson effect” is the superconducting analogue of the nonlocal Aharonov-Bohm effect [45] and the solid-state counterpart of the interferometry of superfluid Bose-Einstein condensates [26].

The spin-singlet pairing considered so far corresponds to a spin-1/2 Bogoliubov quasiparticle (electron and hole

from opposite spin bands). The spin-up quasiparticle then annihilates with its spin-down counterpart. This is closest in analogy to the spin-1/2 Majorana fermion from particle physics (where neutrinos of opposite helicities would annihilate). In superconductors with strong spin-orbit coupling one can also consider a spinless Majorana fermion, with electron and hole from the same spin band (spin-triplet pairing). It is instructive to contrast the two cases.

The transfer matrix for a spin-triplet Andreev edge channel has the form (18) with a different electron-hole rotation matrix [43],

$$U(\alpha, \phi, \beta) = \exp[i\alpha(\tau_x \cos \phi + \tau_y \sin \phi) + i\beta\tau_z]. \quad (26)$$

The Pauli matrix σ_y is no longer present, because electron and hole are from the same spin band. To preserve the particle-hole symmetry (8), the mixing strength α should be an odd function of energy: $\alpha(E) = -\alpha(-E)$. In particular, electron and hole are uncoupled at the Fermi energy ($E = 0$). If we consider frequencies $\omega = 2\text{ eV} - \delta\omega$ near the upper cutoff, this energy dependence does not play a role (since the annihilating Bogoliubov quasiparticles then have the same energy eV). If we again take two identical superconductors we arrive at

$$P_{12} = -\frac{1}{4}G_0R(1-R)\delta\omega(1 - \cos \phi_{12})\sin^2 2\bar{\alpha}. \quad (27)$$

The factor of 2 difference with Eq. (25) is due to the absence of spin degeneracy. The annihilation probability now vanishes for $\phi_{12} = 0$. We interpret this in terms of Pauli blocking, operative because two Bogoliubov quasiparticles from the same spin band are indistinguishable for $\phi_{12} = 0$. In the spin-singlet case, in contrast, they remain distinguished by their opposite spin.

To detect the nonlocal Josephson effect in an experiment, one would like to vary the superconducting phase difference $\phi_{12} = 0$ without affecting the edge channels. This could be achieved by joining the two superconductors via a ring in the plane perpendicular to the two-dimensional electron gas and then varying the flux through this ring. The resulting $\hbar/2e$ oscillations in the noise correlator would have the largest amplitude for $\bar{\alpha}_1 = \bar{\alpha}_2 = \pi/4$, but there is no need for fine tuning of these parameters. For example, if only $\bar{\alpha}_1 = \pi/4$, the amplitude of the oscillations varies as $\sin^2 2\bar{\alpha}_2$, so it remains substantial for a broad interval of $\bar{\alpha}_2$ around $\pi/4$.

The main experimental bottleneck is the coupling strength of the edge channel to the superconductor, which is of order l_m/l_S (magnetic length over proximity-induced superconducting coherence length). The amplitude of the nonlocal Josephson oscillations depends quadratically on this ratio, so for $l_m \approx 10$ nm (in a 4 T magnetic field) one would hope for a l_S below 100 nm.

In summary, we have proposed an experiment for Bogoliubov quasiparticles that is the condensed matter

analogue of the way in which Majorana fermions are searched for in particle physics [46]: by detecting their pairwise annihilation upon collision. The Majorana fermions in a topologically trivial superconductor lack the non-Abelian statistics and the associated nonlocality of Majorana zero modes in a topological superconductor [11], but a different kind of nonlocality remains. We have found that the annihilation probability of quasiparticles originating from two identical superconductors depends on their phase difference—even in the absence of any supercurrent coupling. Observation of the $h/2e$ oscillations of the annihilation probability would provide a striking demonstration of the Majorana nature of Bogoliubov quasiparticles.

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