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COMMUNICATION FROM THE OBSERVATORY AT LEIDEN.

On the longitude of the sun in the years 1864—1900, and the rotation of the earth, by W. de Sitter.

In B. A. N. 124 it was found that from about 1865 to 1895 the longitudes of the sun taken from Dr. JONES's paper in M. N. lxxxvii, p. 4 show an apparent systematic error of about $+ o"\cdot 6$. In a conversation which I had lately at Greenwich with Sir FRANK DYSON and Mr. CULLEN, it was remarked that this interval practically coincides with that during which LEVERRIER's tables were used in the Nautical Almanac. Dr. JONES derived formulas for the correction: Leverrier minus Newcomb, which are given in M. N. 1xxxvi, p. 428. Now experience shows that such corrections are always more or less subject to doubt *), and it would have been safer to compute the place of the sun for every month, as Dr. Jones did for the years 1836-1863. This is, of course, a rather considerable piece of work, and I have contented myself with taking a few samples distributed equally over the interval in question as well as over the different months of the year. The quantities $\Delta (L-N)$ given below are the differences: (Nautical Atmanac—Newcomb's tables) minus (Jones's formulas M.N.lxxvi, p. 428).

Δ	(L	-N
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1864 Jan.	I — 0.7	1876 Apr.	15 — o.i	1889 May	15 — o.4
65 Feb.	14 - 0.7		15 — 0 1		15 -0.3
	15 - 0.3	79 July	15 — 0.3	92 Jan.	15 - 1.1
69 Jan.	15 0.0	80 Dec.	15 - 0.5	94 Oct.	15 -0.5
70 Aug.	15 -0.5	82 Oct.	15 - 0.4	95 Aug.	15 -0.5
	15 - 0.4	85 Apr.	15 0.4	96 Sep.	15 -0.5
73 Feb.	14 0.1	86 Sep.	15 - 0.3	97 Mar.	15 -0.2
74 Ian	TF 0.2	87 Dec	TT 0'4	TOOT Jan	T 0.3

The corrections are rather irregular, and do not show any decided correlation with the time. The general mean is

$$\Delta (L-N) = -0".36$$

If this is applied to the mean epochs 1869 to 1896.5 of B. A. N. 124, TABLE 2, and one third of it to the two epochs 1863 and 1900.5. and if then a further

correction of -0" 16 T is applied to the mean longitude of the sun, the residuals become:

RESIDUALS OF SUN'S LONGITUDE.

1767 89 1804 17 27 34 39 47.5 55.5	- 1'36 + '07 - 1'52 - 3'83 - 1'39 + '19 - '05 - '05	1863 69 73 78 83 88 92.5 96.5	- 0°12 + '27 + '16 + '17 + '10 + '13 - '09 - '34 - '21	1903.5 06.5 09.5 12.5 18.0 20.0 22.0 24.0 26.0	-0"14 - '10 + '14 - '04 - '16 - '20 - '15 - '14
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The residuals have become much less systematic. The residual for 1896.5, which was very small, has been made large negative, and that of 1900.5 also in a smaller degree.*) The correction applied is, of course, not entitled to great confidence, but the result seems to show that a more careful reduction would probably lead to still smaller residuals, and that consequently the interpretation of the observed fluctuations as given in B. A. N. 124 is confirmed.

It was shown in B.A.N. 124 that the observed fluctuations in the longitudes of the moon, the sun and the planets Mercury and Venus, can be explained by assuming two kinds of changes in the rotation of the earth, viz: (A) discontinuous changes of the moment of inertia, and (B) discontinuous changes of the coefficient of tidal friction. The cause (A) affects only the length of the day, the cause (B) also produces a change in the true mean motion of the moon, the consequent ratio of the changes in the apparent longitudes of the sun and planets and of the moon being $Q = Q_s$, while for the cause (A) it is Q = I. According to B.A.N. 124, p. 36, footnote, the most probable value of Q_s is $Q_s = 4.4$.

Expressing the effect of both causes (A) and (B) in time, we adopt for the correction to be applied

^{*)} Cf. Newcomb, Astronomical Constants, p. 7: "I can not but feel that the application of such corrections involves more or less doubt and uncertainty".

^{*)} These two residuals depend on JONES's Table III (M.N. lxxxvii, p. 9), the others on his table II (p. 8).

to astronomical time in order to get uniform, or 'Newtonian' time:

Epoch of	∂C	Δt by cause (A)
discontinuity	\overline{C}	s
1663 1758 1784 1864 1876 1897	+ 1.54.10 ⁻⁸ - 0.52 - 2.06 - 3.09 + 1.98 + 3.92 - 3.92	$\begin{array}{c} -27.8 \\ -0.5 + 48.7 (T+1.80) \\ +21.4 + 32.1 (T+1.30) \\ +13.9 - 33.0 (T+0.75) \\ -6.5 - 130.1 (T+0.30) \\ -20.4 - 67.6 (T+0.15) \\ -23.7 + 55.8 (T-0.05) \\ -17.1 - 67.6 (T-0.20) \end{array}$

For the cause (B) we have:

The first straight line of (A) has been slightly altered, and the last added, and a smaller coefficient of S in the third parabola of (B) has been adopted. Otherwise these expressions are the same as those given in B.A.N. 124. It will be remembered that $S = T^2 + 1.33$ T - 0.26.

The effect of the cause (B) can be split up in the average (B)_o, which gives the secular accelerations, and the fluctuations (B)' = (B) - (B)_o. The excess of the longitudes of the sun and the planets Mercury and Venus over those given by NEWCOMB's tables are then:

$$\Delta L' = + \text{ i''89} + \text{ i''25} T + \text{ i''65} S + \text{ o·o411} [(A) + (B)']$$

 $\Delta \lambda_{x} = + \text{ 7·65} + \text{ 7·13} T + \text{ 6·86} S + \text{ o·171} [(A) + (B)']$
 $\Delta \lambda_{z} = + \text{ 3·30} + \text{ 2·32} T + \text{ 2·70} S + \text{ o·o67} [(A) + (B)'],$

and for the moon the excess over BROWN's tables is

$$\Delta L = + 6^{"}70 + 4^{"}00 T - 10^{"}71 \sin(140^{\circ}0 T + 240^{\circ}7) + 5^{"}03 S + 0.549 [(A) + 0.23 (B)'].$$

For the transits of Mercury the corrections ΔV and ΔW are as adopted in B.A.N. 124.

The residuals given by these expressions are given in the following table.

The residuals for the sun and planets are in some cases even smaller than those found before, using the observed fluctuations of the moon instead of the computed (A) + (B').

RESIDUALS.

Moon			Moon Meridian obs.			Sun		Venus		Transits of Mercury					
Occultations		November								May					
t	Res.	t	Res.	t	Res.	t	Res.	t	Res.	t	Res.	t	Res.	t	Res.
1637 49 62 81 1710 27 37 47 .55 71 85 92 1801·5 09·5 13·0 21·0 22·5 33·5 39·5	+ 0.7 + 0.8 - 0.4 + 0.1 + 0.4 + 0.6 - 0.3 - 0.3 - 0.3 + 0.5 + 1.0 - 0.5 - 0.5 - 0.5 - 0.6	1847.5 50.0 53.0 57.0 61.0 65.0 69.0 77.0 81.0 85.0 93.0 93.0 93.0 93.0 93.0 93.0 93.0 93	- ·26	1753·6 59·2 64·9 70·6 76·2 81·9 87·6 93·2 98·3 1803·4 09·1 14·8 20·4 43·1 43·1 43·1 45·5 57·5	+ 0.01 65 + .25 + .14 + .52 + .30 24 + .14 169 36 36 36 31 + .75	1862·5 67·5 72·5 77·5 82·5 87·5 91·5 97·5 1900·5 03·5 06·5 12·5 18·5 21·5 24·0	+ c"53 + '19 - '24 - '47 + '09 - '34 + '01 - '16 + '16 - '14 + '03 - '33 - '07 - '19 + '56 - '30 + '83 + '10 + '29	1767 89 1804 17 27 34 39 47.5 55.5 63 69 73 78 83 88 92.5 96.5 190.5 09.5 09.5 12.5 12.5 18.0 20.0 24.0 26.0	"31	1840 45 50 55 60 65 70 75 80 84 88 92 96 1900 04 07 10 13 16 19 22	- "14 - '60 - '30 + '10 + '24 + '18 + '05 + '35 + '47 - '11 - '13 - '15 - '11 + '07 + '02 - '06 + '12 + '30	1677'9 90'9 97'9 1723'9 36'9 43'9 56'9 82'9 89'9 1802'9 22'9 48'9 68'9 21'9 94'9 14'9	- '44 - 4'44 + 1'14 + 1'14 + '17 - '05 - 1'28 + 8'24 - '56	86·4 99·4	+ ·30 + ·48