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COMMUNICATIONS FROM THE OBSERVATORY AT LEIDEN

Discussion on personal errors in photographic measures of double stars, by *Ejnar Hertzsprung*.

The errors met with in photographic measures of double stars may be classified as follows, though a precise discrimination between the various kinds cannot be made:

- A. Errors inherent in the photographic image,
- B. Errors of measurement,
- C. Personal errors of interpretation of the image.

Each of these types of errors may be divided into a systematic and an accidental part.

The squares of the mean accidental errors of these three kinds are designated respectively by I (image), M (measurement) and P (person).

The separation between I and P is naturally conventional and may vary from one person to another according to the way in which the centre of the image is chosen. E.g. one person may point on the blackest spot he can find in the image even if it is lying eccentrically, while another will try to cut the whole image into two equal parts.

It is well known that marked personal errors are shown by ordinary visual measures of double stars and these errors soon put a limit to the number of nights in which it pays to have a double star visually measured by a single observer. This number of nights is about three.

The question to which extent personal errors also exist in photographic measures of double stars is of equal importance as the systematic character of such errors will determine the maximum accuracy which can be reached by a single person. Otherwise than in the case of visual measures the material for obtaining a judgement of personal errors in photographic measures is very scarce. The same series of photographs of double stars has rarely been measured by more than one person. Only two notable cases of this kind are known, viz. the measures 1° of a number of Potsdam plates of ξ UMa by W. H. VAN DEN BOS and the writer (*Mém. Acad. Roy. de Danemark, section des sciences*, 8e série, t. XII, no. 2; 1928) and 2° of several other plates of 6 different double stars by K. AA. STRÅND and the writer (*Ann. Sterrewacht te Leiden*,

XVIII, part 2). As only three persons are concerned with the measures just mentioned they throw but little light on the question of systematic personal errors. For this reason the writer thought it desirable to have a plate, carrying several exposures of a double star, measured by a number of persons sufficiently large to obtain an idea of the general variation of the systematic error from one individual to another.

The present investigation is based on a single plate, no. 271, of Antares taken with the visual refractor at Johannesburg diaphragmed to 30 cm aperture. The focal length is 1070 cm and the scale on the plate $1 \text{ mm} = 18''\cdot909$. The plate was taken under excellent atmospheric conditions when the object was near to the zenith. A coarse grating, which gave diffraction images of the brighter component nearly equal to the central image of the 4^m fainter companion, was placed in front of the objective. The position angle of the wires of the grating was 81° . The distance between the spectra of the first order and the central image was 259μ or $4''\cdot90$. The constant of the grating, $d + l$, was $23\cdot29 \text{ mm}$ and the effective wavelength of the images 553μ . The diameter of the images measured is about 45μ and of the not measured central image of the brighter component about 147μ . The exposure time was generally about $\cdot4$ seconds and was chosen as short as feasible in order to avoid systematic photographic errors in distance of this close pair. The distance on the plate between the two stars is 159μ and the corresponding clear space between them $159 - \frac{1}{2}(45 + 147) = 63 \mu$. Systematic plate errors are therefore hardly to be expected.

The plate carries two rows of respectively 31 and 35 exposures separated by a trail of Antares for the direction of the daily motion. The last image, no. 66, was for identification purposes exposed distinctly longer than the rest. The plate was taken 1931 April 24th round $17^{\text{h}}5^{\text{m}}$ sid. time Johannesburg or in the conventional counting of years 1931·311. The temperature was 12° C and the focal reading $48\cdot6 \text{ mm}$. A

TABLE I.

| | date | n_f | n_g | $\Delta z \cos \delta$ | Δ | 2M+I | n_f | n_g | $\Delta \delta$ | Δ | 2M+I |
|--------------------|---------|-------|-------|------------------------|----------|------|-------|-------|-----------------|----------|------|
| E. HERTZSPRUNG | 1932'38 | 44 | 50 | 158'84 | — '04 | 10'1 | 53 | 50 | 13'32 | '04 | 11'6 |
| G. P. KUIPER | '39 | 51 | 56 | 8'80 | — '09 | 7'3 | 57 | 52 | 3'16 | — '11 | 8'5 |
| P. TH. OOSTERHOFF | '39 | 51 | 54 | 8'28 | — '60 | 9'0 | 55 | 58 | 2'87 | — '40 | 10'2 |
| W. H. VAN DEN BOS | 35'47 | 63 | 63 | 9'04 | '16 | 7'5 | 65 | 64 | 3'00 | — '27 | 7'1 |
| D. REUYL | '87 | 46 | 45 | 9'35 | '46 | 8'6 | 44 | 39 | 2'85 | — '43 | 5'5 |
| M. SCHWARZSCHILD | '94 | 64 | 64 | 8'46 | — '42 | 11'4 | 63 | 63 | 3'37 | '10 | 10'0 |
| K. AA. STRAND | '97 | 58 | 59 | 8'04 | — '84 | 11'6 | 60 | 60 | 2'27 | — 1'00 | 12'6 |
| J. MERGENTALER | 36'44 | 54 | (53) | (8'70) | (— '18) | | 57 | 54 | 3'68 | '41 | 9'2 |
| F. DE HAAS | '50 | 61 | 60 | 8'93 | '04 | 15'2 | 62 | 61 | 3'45 | '18 | 16'4 |
| MISS H. A. KLUYVER | '64 | 63 | 63 | 8'61 | — '27 | 20'4 | 60 | 60 | 2'73 | — '54 | 11'3 |
| J. M. ABRAMS | '65 | 52 | 54 | 9'51 | '63 | 10'1 | 61 | 56 | 2'51 | — '76 | 13'1 |
| J. DE KORT | '66 | 46 | 57 | 9'42 | '54 | 15'5 | 51 | 55 | 3'40 | '13 | 15'4 |
| D. GAYKEMA | '71 | 64 | 62 | 9'41 | '53 | 9'7 | 62 | 61 | 3'14 | — '14 | 6'8 |
| A. VAN HOOFF | '73 | 45 | 48 | 9'91 | 1'02 | 6'0 | 50 | 49 | 3'53 | '26 | 6'5 |
| J. ZEEMAN | '74 | 52 | 52 | 9'45 | '57 | 8'1 | 48 | 53 | 4'06 | '79 | 7'6 |
| C. J. KOOREMAN | '74 | 46 | 52 | 9'79 | '91 | 6'8 | 51 | 53 | 3'49 | '21 | 5'8 |
| A. J. WESSELINK | '75 | 46 | 33 | 9'22 | '34 | 7'1 | 36 | 35 | 3'55 | '28 | 7'2 |
| L. PLAUT | '75 | 65 | 65 | 8'63 | — '25 | 8'8 | 65 | 65 | 2'42 | — '86 | 7'9 |
| A. DE SITTER | '75 | 55 | 51 | 9'05 | '17 | 8'6 | 56 | 55 | 3'09 | — '18 | 10'1 |
| G. VAN HERK | '76 | 65 | 65 | 9'04 | '16 | 13'6 | 65 | 65 | 2'91 | — '36 | 10'7 |
| R. PRAGER | '77 | 63 | 65 | 8'90 | '02 | 4'3 | 64 | 63 | 3'62 | '35 | 9'2 |
| J. H. OORT | 37'11 | 50 | 48 | 8'78 | — '10 | 4'9 | 45 | 42 | 3'43 | '16 | 5'9 |
| C. H. HINS | '27 | 58 | 47 | 9'48 | '60 | 8'6 | 55 | 53 | 4'27 | 1'00 | 8'0 |
| A. BLAAUW | '28 | 64 | 64 | 8'86 | — '02 | 14'1 | 65 | 65 | 3'29 | '02 | 10'9 |
| J. UITTERDYK | '29 | 58 | 58 | 8'81 | — '08 | 7'3 | 60 | 58 | 3'36 | '09 | 8'5 |
| W. CHR. MARTIN | '30 | 62 | 64 | 8'45 | — '44 | 8'3 | 63 | 64 | 2'80 | — '47 | 6'1 |
| G. PELS | '31 | 65 | 65 | 8'21 | — '67 | 11'8 | 65 | 65 | 3'22 | — '05 | 12'7 |
| C. SANDERS | '34 | 62 | 64 | 8'52 | — '37 | 13'3 | 64 | 64 | 3'41 | '13 | 10'4 |
| L. BINNENDYK | '37 | 65 | 65 | 8'54 | — '34 | 11'3 | 65 | 65 | 3'61 | '34 | 10'6 |
| H. KLEIBRINK | '39 | 62 | 64 | 8'53 | — '35 | 14'9 | 64 | 64 | 2'72 | — '56 | 11'6 |
| H. VAN GENT | '44 | 60 | 62 | 9'29 | '41 | 8'3 | 63 | 63 | 3'31 | '03 | 7'7 |
| J. G. FERWERDA | '53 | 52 | 52 | 9'06 | '17 | 10'4 | 52 | 53 | 3'67 | '40 | 9'5 |
| R. ROELOFS | '53 | 64 | 65 | 8'88 | — '00 | 10'2 | 64 | 65 | 3'53 | '26 | 10'9 |
| F. NISOLI | 38'41 | 64 | 64 | 9'07 | '19 | 10'3 | 64 | 65 | 2'52 | — '75 | 10'0 |
| J. SCHILT | '51 | 44 | 44 | 8'19 | — '70 | 11'9 | 43 | 40 | 3'33 | '06 | 8'1 |
| W. J. LUYTEN | '53 | 65 | 65 | 8'15 | — '74 | 9'5 | 65 | 65 | 3'30 | '02 | 10'7 |
| H. M. JEFFERS | '73 | 42 | 44 | 9'90 | 1'01 | 7'0 | 47 | 41 | 3'97 | '69 | 3'9 |
| J. M. KRIEST | '84 | 65 | 65 | 9'27 | '39 | 19'4 | 65 | 65 | 2'93 | — '34 | 9'9 |
| H. W. R. KRAUSS | '86 | 63 | 55 | 8'22 | — '66 | 7'6 | 63 | 63 | 3'80 | '53 | 10'0 |
| G. V. SIMONOV | 39'32 | 64 | 59 | 8'93 | '04 | 13'0 | 62 | 62 | 3'98 | '71 | 16'4 |
| M. RUDKJØBING | '45 | 66 | 66 | 8'16 | — '73 | 19'4 | 66 | 66 | 2'97 | — '30 | 13'4 |
| A. D. THACKERAY | '49 | 53 | 60 | 8'41 | — '47 | 9'0 | 58 | 51 | 3'24 | — '03 | 8'3 |
| P. SÉMIROT | '62 | 64 | 65 | 8'55 | — '34 | 10'8 | 65 | 65 | 3'03 | — '24 | 11'0 |
| W. H. DIRKS | '78 | 57 | 65 | 8'84 | — '04 | 13'1 | 62 | 61 | 3'77 | '50 | 8'3 |
| D. BENNINK | 40'03 | 59 | 65 | 9'08 | '19 | 16'1 | 57 | 63 | 3'37 | '09 | 9'3 |

yellow screen was used in combination with an Eisenberger erythrosine plate.

This plate was measured by 45 different persons. The main results are given in Tables 1 and 2 in the form of mean values respectively for each person and for each image. The measurement was carried out separately in the two rectangular co-ordinates $\Delta z \cos \delta$ and $\Delta \delta$ and made in Leiden with the Toepfer machine of the Danish Carlsberg Foundation. The plate was moved micrometrically in one direction and measured both with the film turned toward the microscope and through the glass, the plate being turned 180° round an axis parallel to the pointing wire. In this way certain errors of measurement are eliminated.

In Table 1 mean results obtained by each person are given in chronological order of measurement. The choice of the images to be used was left to the person

who had to do the measures. The images measured in the two positions of the plate were not always the same so that images of inferior quality automatically obtained half weight.

Between the two measures of $\Delta z \cos \delta$ made by MERGENTALER the plate was erroneously turned round an axis parallel to the trail. These measures have therefore been used only partially. They are placed in parentheses in Table 1.

All the readings were made in microns.

In Table 2 the results are given separately for each image. It includes all measures made, also those which were rejected in Table 1. The total number of single settings used is 31332.

The relative weights given in Table 2 are rather arbitrary. They are mainly based on the indication

TABLE 2.

| no. of image | number of exposures measured | | | $\Delta z \cos \delta$ | rel. p | Δ | M+P | M | number of exposures measured | | | $\Delta \delta$ | rel. p | Δ | M+P | M |
|--------------|------------------------------|-------|------------|------------------------|----------|----------|-------|---------|------------------------------|-------|------------|-----------------|----------|----------|-------|---------|
| | n_2 | n_1 | $2n_2+n_1$ | | | | | | n_2 | n_1 | $2n_2+n_1$ | | | | | |
| 1 | 29 | 6 | 64 | 158'88 | 5 | 0'00 | 8'29 | 8'98 | 29 | 10 | 68 | 9'70 | 6 | -3'71 | 9'39 | 4'62 |
| 2 | 31 | 7 | 69 | 55'40 | 6 | -3'48 | 4'42 | 3'99 | 33 | 7 | 73 | 9'25 | 7 | -4'16 | 3'20 | 3'74 |
| 3 | 38 | 6 | 82 | 63'59 | 10 | 4'71 | 4'56 | 2'41 | 39 | 1 | 79 | 16'76 | 10 | 3'35 | 3'96 | 3'48 |
| 4 | 39 | 4 | 82 | 58'06 | 10 | -82 | 7'24 | 4'33 | 45 | 0 | 90 | 16'01 | 18 | 2'60 | 2'08 | 1'99 |
| 5 | 42 | 1 | 85 | 57'38 | 15 | -1'50 | 3'24 | 2'90 | 41 | 2 | 84 | 16'07 | 13 | 2'66 | 3'88 | 3'24 |
| 6 | 42 | 3 | 87 | 60'66 | 17 | 1'78 | 2'68 | 2'96 | 44 | 1 | 89 | 15'57 | 18 | 2'16 | 2'15 | 3'06 |
| 7 | 1 | 1 | 3 | 58'50 | 0 | -38 | | (33'06) | 1 | 0 | 2 | 8'00 | 0 | -5'41 | | (12'21) |
| 8 | 44 | 1 | 89 | 59'06 | 18 | 1'18 | 2'60 | 1'13 | 45 | 0 | 90 | 14'54 | 18 | 1'13 | 3'84 | 1'80 |
| 9 | 27 | 5 | 59 | 61'82 | 4 | 2'94 | 6'17 | 4'88 | 27 | 13 | 67 | 12'00 | 6 | -1'41 | 5'91 | 2'25 |
| 10 | 40 | 5 | 85 | 57'56 | 15 | -1'32 | 2'96 | 2'25 | 43 | 1 | 87 | 12'49 | 17 | -92 | 2'17 | 2'01 |
| 11 | 36 | 8 | 80 | 56'66 | 10 | -2'22 | 2'90 | 2'66 | 27 | 15 | 69 | 16'77 | 6 | 3'36 | 4'91 | 1'95 |
| 12 | 31 | 10 | 72 | 54'49 | 7 | -4'39 | 3'32 | 2'77 | 39 | 2 | 80 | 12'88 | 10 | -53 | 3'70 | 1'33 |
| 13 | 40 | 5 | 85 | 61'32 | 15 | 2'44 | 3'24 | 2'98 | 41 | 4 | 86 | 13'87 | 16 | 4'46 | 1'55 | 2'65 |
| 14 | 44 | 1 | 89 | 59'31 | 18 | 4'3 | 1'81 | 2'34 | 45 | 0 | 90 | 12'23 | 18 | -1'18 | 2'28 | 1'05 |
| 15 | 44 | 1 | 89 | 62'41 | 18 | 3'53 | 2'65 | 3'08 | 42 | 1 | 85 | 14'51 | 15 | 1'10 | 1'57 | 2'77 |
| 16 | 43 | 2 | 88 | 60'86 | 18 | 1'98 | 1'92 | 2'11 | 40 | 5 | 85 | 13'43 | 15 | 0'02 | 2'47 | 2'96 |
| 17 | 29 | 10 | 68 | 59'92 | 6 | 1'04 | 4'02 | 3'26 | 37 | 6 | 80 | 14'23 | 10 | 82 | 1'93 | 1'90 |
| 18 | 43 | 2 | 88 | 58'39 | 18 | -49 | 1'96 | 1'99 | 45 | 0 | 90 | 15'47 | 18 | 2'06 | 5'02 | 1'00 |
| 19 | 39 | 5 | 83 | 56'26 | 10 | -2'62 | 3'90 | 2'43 | 39 | 6 | 84 | 11'68 | 13 | -1'73 | 2'76 | 1'86 |
| 20 | 44 | 1 | 89 | 60'26 | 18 | 1'38 | 1'25 | 1'83 | 45 | 0 | 90 | 12'28 | 18 | -1'13 | 1'07 | 1'36 |
| 21 | 37 | 7 | 81 | 57'50 | 10 | -1'38 | 2'08 | 1'59 | 38 | 5 | 81 | 12'70 | 10 | -71 | 2'77 | 1'34 |
| 22 | 44 | 1 | 89 | 58'94 | 18 | 06 | 3'56 | 1'85 | 45 | 0 | 90 | 12'91 | 18 | -50 | 1'43 | 2'21 |
| 23 | 43 | 2 | 88 | 59'93 | 18 | 1'05 | 2'09 | 1'35 | 45 | 0 | 90 | 13'87 | 18 | 4'46 | 2'40 | 1'64 |
| 24 | 43 | 2 | 88 | 55'29 | 18 | -3'59 | 3'13 | 2'29 | 43 | 2 | 88 | 9'72 | 18 | -3'69 | 2'69 | 1'49 |
| 25 | 16 | 8 | 40 | 50'58 | 2 | -8'30 | 11'30 | 7'71 | 20 | 11 | 51 | 5'62 | 3 | -7'79 | 6'58 | 2'97 |
| 26 | 44 | 1 | 89 | 60'72 | 18 | 1'84 | 1'38 | 1'99 | 44 | 1 | 89 | 14'40 | 18 | 99 | 1'30 | 1'38 |
| 27 | 44 | 1 | 89 | 57'12 | 18 | -1'76 | 1'07 | 1'26 | 45 | 0 | 90 | 14'38 | 18 | 97 | 2'50 | 1'96 |
| 28 | 26 | 8 | 60 | 63'55 | 4 | 4'67 | 2'03 | 2'70 | 32 | 9 | 73 | 10'42 | 7 | -2'99 | 1'68 | 2'77 |
| 29 | 44 | 1 | 89 | 59'96 | 18 | 1'08 | 1'49 | 1'82 | 45 | 0 | 90 | 16'69 | 18 | 3'28 | 2'81 | 2'68 |
| 30 | 43 | 2 | 88 | 59'88 | 18 | 1'00 | 1'77 | 1'79 | 44 | 0 | 88 | 10'88 | 18 | -2'53 | 2'61 | 2'60 |
| 31 | 33 | 8 | 74 | 60'35 | 8 | 1'47 | 3'21 | 1'85 | 27 | 7 | 61 | 12'02 | 5 | -1'39 | 11'87 | 4'43 |
| 32 | 34 | 7 | 75 | 62'89 | 8 | 4'01 | 5'25 | 4'82 | 43 | 1 | 87 | 13'45 | 17 | 04 | 2'60 | 1'80 |
| 33 | 42 | 3 | 87 | 59'28 | 17 | 40 | 3'39 | 3'09 | 41 | 3 | 85 | 17'16 | 15 | 3'75 | 3'99 | 3'01 |
| 34 | 19 | 18 | 56 | 51'65 | 4 | -7'23 | 4'64 | 3'12 | 30 | 7 | 67 | 9'46 | 6 | -3'95 | 4'39 | 3'38 |
| 35 | 37 | 5 | 79 | 60'90 | 10 | 2'02 | 2'68 | 2'71 | 40 | 3 | 83 | 14'73 | 12 | 1'32 | 1'47 | 1'92 |
| 36 | 30 | 7 | 67 | 63'22 | 6 | 4'34 | 2'66 | 4'36 | 31 | 9 | 71 | 11'12 | 7 | -2'29 | 2'94 | 3'00 |
| 37 | 39 | 6 | 84 | 55'94 | 15 | -2'94 | 2'57 | 2'47 | 43 | 2 | 88 | 15'98 | 18 | 2'57 | 1'88 | 1'48 |
| 38 | 44 | 1 | 89 | 58'78 | 18 | -10 | 1'47 | 2'26 | 44 | 1 | 89 | 12'39 | 18 | -1'02 | 1'72 | 2'45 |
| 39 | 44 | 1 | 89 | 57'46 | 18 | -1'42 | 1'95 | 1'45 | 44 | 1 | 89 | 12'46 | 18 | -95 | 96 | 1'13 |
| 40 | 28 | 3 | 59 | 60'29 | 4 | 1'41 | 6'61 | 3'10 | 27 | 1 | 55 | 12'83 | 4 | -58 | 5'27 | 4'83 |
| 41 | 37 | 8 | 82 | 56'95 | 10 | -1'93 | 2'16 | 1'63 | 39 | 2 | 80 | 13'46 | 10 | 05 | 3'43 | 2'86 |
| 42 | 44 | 1 | 89 | 55'47 | 18 | -3'41 | 1'62 | 1'49 | 44 | 1 | 89 | 16'38 | 18 | 2'97 | 1'60 | 1'47 |
| 43 | 41 | 4 | 86 | 60'72 | 16 | 1'84 | 2'56 | 1'76 | 45 | 0 | 90 | 13'81 | 18 | 40 | 1'89 | 1'33 |
| 44 | 44 | 1 | 89 | 58'67 | 18 | -21 | 1'55 | 1'85 | 45 | 0 | 90 | 13'03 | 18 | -38 | 2'98 | 2'71 |
| 45 | 42 | 3 | 87 | 58'07 | 17 | -81 | 1'35 | 2'51 | 40 | 5 | 85 | 12'86 | 15 | -55 | 6'95 | 2'91 |
| 46 | 43 | 2 | 88 | 58'92 | 17 | 04 | 1'40 | 1'85 | 45 | 0 | 90 | 13'79 | 18 | 38 | 78 | 1'79 |
| 47 | 37 | 3 | 77 | 61'31 | 9 | 2'43 | 4'38 | 2'54 | 40 | 4 | 84 | 11'15 | 13 | -2'26 | 3'52 | 3'30 |
| 48 | 44 | 1 | 89 | 56'29 | 18 | -2'59 | 2'62 | 2'02 | 45 | 0 | 90 | 12'76 | 18 | -65 | 2'88 | 1'91 |
| 49 | 44 | 1 | 89 | 57'11 | 18 | -1'77 | 4'84 | 1'00 | 45 | 0 | 90 | 11'28 | 18 | -2'13 | 2'52 | 1'32 |
| 50 | 43 | 1 | 87 | 61'34 | 17 | 2'46 | 2'41 | 1'33 | 44 | 0 | 88 | 11'77 | 18 | -1'64 | 1'70 | 1'38 |
| 51 | 30 | 5 | 65 | 60'65 | 6 | 1'77 | 2'88 | 3'31 | 31 | 7 | 69 | 8'39 | 6 | -5'02 | 5'45 | 2'67 |
| 52 | 10 | 9 | 29 | 54'10 | 0 | -4'78 | 13'92 | 3'71 | 12 | 8 | 32 | 10'58 | 0 | -2'83 | 5'60 | 2'99 |
| 53 | 23 | 9 | 55 | 57'40 | 4 | -1'48 | 3'54 | 3'64 | 26 | 6 | 58 | 15'41 | 4 | 2'00 | 7'19 | 3'75 |
| 54 | 44 | 1 | 89 | 55'14 | 18 | -3'74 | 3'59 | 1'89 | 45 | 0 | 90 | 13'49 | 18 | 08 | 2'47 | 1'96 |
| 55 | 37 | 9 | 83 | 59'92 | 10 | 1'04 | 3'39 | 1'84 | 39 | 5 | 83 | 18'62 | 12 | 5'21 | 2'37 | 1'40 |
| 56 | 36 | 7 | 79 | 59'37 | 10 | 49 | 3'14 | 1'99 | 44 | 0 | 88 | 13'88 | 18 | 47 | 2'70 | 2'33 |
| 57 | 32 | 13 | 77 | 61'62 | 11 | 2'74 | 1'75 | 1'40 | 42 | 3 | 87 | 10'59 | 17 | -2'82 | 2'16 | 1'65 |
| 58 | 44 | 1 | 89 | 57'60 | 18 | -1'28 | 1'60 | 1'42 | 45 | 0 | 90 | 13'22 | 18 | -19 | 1'42 | 1'36 |
| 59 | 38 | 4 | 80 | 58'07 | 10 | -81 | 5'80 | 2'32 | 37 | 6 | 80 | 12'45 | 10 | -96 | 8'89 | 3'57 |
| 60 | 42 | 3 | 87 | 61'31 | 17 | 2'43 | 3'00 | 1'39 | 34 | 8 | 76 | 11'76 | 9 | -1'65 | 3'63 | 2'60 |
| 61 | 44 | 1 | 89 | 58'17 | 18 | -71 | 1'28 | 1'74 | 45 | 0 | 90 | 12'11 | 18 | -1'30 | 1'27 | 89 |
| 62 | 44 | 1 | 89 | 59'80 | 18 | 92 | 1'52 | 1'57 | 45 | 0 | 90 | 12'66 | 18 | -75 | 2'07 | 1'81 |
| 63 | 29 | 9 | 67 | 59'92 | 6 | 1'04 | 3'26 | 3'06 | 31 | 6 | 68 | 15'57 | 6 | 2'16 | 2'37 | 1'88 |
| 64 | 44 | 1 | 89 | 57'97 | 18 | -91 | 2'00 | 1'52 | 44 | 1 | 89 | 13'48 | 18 | 07 | 2'10 | 2'06 |
| 65 | 44 | 1 | 89 | 59'62 | 18 | 74 | 2'73 | 4'59 | 42 | 3 | 87 | 14'89 | 17 | 1'48 | 3'35 | 2'47 |
| 66 | 23 | 4 | 50 | 56'57 | 3 | -2'31 | 2'39 | 2'01 | 24 | 5 | 53 | 12'08 | 3 | -1'33 | 7'55 | 2'63 |

of the quality of the image given by the frequency with which it has been chosen for measurement.

The deviations Δ from the weighted mean as they are given in Table 2 are practically only due to defects of the image concerned. Arranged according to the weight p and divided into three groups the following mean values are obtained:

| number of images $n_{\Delta z \cos \delta} + n_{\Delta \delta}$ | weight | $\Delta^2 = I$ | $2 M$ |
|--|--------|----------------|-------|
| 54 | 18.0 | 3.0 | 3.6 |
| 42 | 13.2 | 4.2 | 4.7 |
| 32 | 5.5 | 13.0 | 7.1 |

Here it is again confirmed (comp. *Potsdam Publ.* 63, Vol. 22, p. 16) that the square of the mean error of one

TABLE 3.
Image no. 22.

| measured by | $\Delta z \cos \delta$ | | | | $\Delta \delta$ | | | |
|--------------------|------------------------|--------------|----------|----------|-----------------|------|----------|----------|
| | $2f$ -300 | $2g$ -300 | Σ | Δ | $2f$ | $2g$ | Σ | Δ |
| E. HERTZSPRUNG | 11 | 6 | 17 | 5 | 24 | 36 | 60 | 12 |
| G. P. KUIPER | 23 | 12 | 35 | 11 | 19 | 31 | 50 | 12 |
| P. TH. OOSTERHOFF | 6 | 17 | 23 | 11 | 22 | 26 | 48 | 4 |
| W. H. VAN DEN BOS | 20 | 16 | 36 | 4 | 23 | 24 | 47 | 1 |
| D. REUYL | 25 | 16 | 41 | 9 | 23 | 28 | 51 | 5 |
| M. SCHWARZSCHILD | 22 | 25 | 47 | 3 | 31 | 28 | 59 | 3 |
| K. AA. STRAND | 12 | 13 | 25 | 1 | 25 | 22 | 47 | 3 |
| J. MERGENTALER | 21 | (18) | | | 31 | 30 | 61 | 1 |
| F. DE HAAS | 19 | 18 | 37 | 1 | 28 | 26 | 54 | 2 |
| MISS H. A. KLUYVER | 15 | 23 | 38 | 8 | 25 | 25 | 50 | 0 |
| J. M. ABRAMS | 22 | 24 | 46 | 2 | 28 | 13 | 41 | 15 |
| J. DE KORT | 27 | 18 | 45 | 9 | 22 | 31 | 53 | 9 |
| D. GAYKEMA | 15 | 9 | 24 | 6 | 22 | 27 | 49 | 5 |
| A. VAN HOOF | 16 | 22 | 38 | 6 | 22 | 29 | 51 | 7 |
| J. ZEEMAN | 24 | 19 | 43 | 5 | 30 | 27 | 57 | 3 |
| C. J. KOOREMAN | 21 | 18 | 39 | 3 | 22 | 28 | 50 | 6 |
| A. J. WESSELINK | 17 | 15 | 32 | 2 | 26 | 30 | 56 | 4 |
| L. PLAUT | 17 | 11 | 28 | 6 | 26 | 25 | 51 | 1 |
| A. DE SITTER | 18 | 25 | 43 | 7 | 25 | 22 | 47 | 3 |
| G. VAN HERK | 18 | 21 | 39 | 3 | 32 | 26 | 58 | 6 |
| R. PRAGER | 18 | 20 | 38 | 2 | 26 | 29 | 55 | 3 |
| J. H. OORT | 23 | 23 | 46 | 0 | 25 | 25 | 50 | 0 |
| C. H. HINS | 20 | 22 | 42 | 2 | 28 | 25 | 53 | 3 |
| A. BLAAUW | 21 | 22 | 43 | 1 | 22 | 25 | 47 | 3 |
| J. UITTERDYK | 21 | 25 | 46 | 4 | 26 | 27 | 53 | 1 |
| W. CHR. MARTIN | 12 | 18 | 30 | 6 | 30 | 25 | 55 | 5 |
| G. PELS | 11 | 13 | 24 | 2 | 20 | 25 | 45 | 5 |
| C. SANDERS | 9 | 19 | 28 | 10 | 27 | 25 | 52 | 2 |
| L. BINNENDYK | 17 | 22 | 39 | 5 | 22 | 26 | 48 | 4 |
| H. KLEIBRINK | 18 | 14 | 32 | 4 | 23 | 37 | 60 | 14 |
| H. VAN GENT | 20 | 22 | 42 | 2 | 24 | 27 | 51 | 3 |
| J. G. FERWERDA | 22 | 20 | 42 | 2 | 26 | 31 | 57 | 5 |
| R. ROELOFS | 16 | 19 | 35 | 3 | 24 | 26 | 50 | 2 |
| F. NISOLI | 14 | 21 | 35 | 7 | 26 | 24 | 50 | 2 |
| J. SCHILT | 14 | 19 | 33 | 5 | 16 | 27 | 43 | 11 |
| W. J. LUYTEN | 19 | 7 | 26 | 12 | 25 | 31 | 56 | 6 |
| H. M. JEFFERS | 24 | 19 | 43 | 5 | 27 | 25 | 52 | 2 |
| J. M. KRIEST | 18 | 21 | 39 | 3 | 22 | 28 | 50 | 6 |
| H. W. R. KRAUSS | 9 | 14 | 23 | 5 | 27 | 33 | 60 | 6 |
| G. V. SIMONOV | 19 | 16 | 35 | 3 | 21 | 33 | 54 | 12 |
| M. RUDKJØBING | 16 | 15 | 31 | 1 | 24 | 29 | 53 | 5 |
| A. D. THACKERAY | 20 | 19 | 39 | 1 | 24 | 25 | 49 | 1 |
| P. SÉMIROT | 16 | 10 | 26 | 6 | 23 | 24 | 47 | 1 |
| W. H. DIRKS | 23 | 18 | 41 | 5 | 22 | 28 | 50 | 6 |
| D. BENNINK | 18 | 18 | 36 | 0 | 21 | 22 | 43 | 1 |

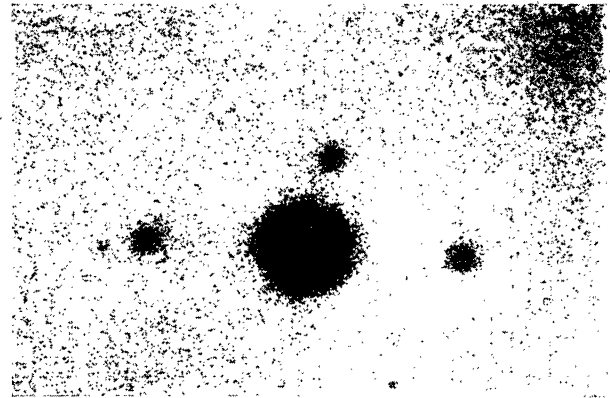


FIGURE 1.

Image of Antares 61 times enlarged, thus corresponding to an equivalent focal length of 665 metre.

setting is about equal to that arising from defects of the image.

In Table 3 the complete measures on the image no. 22 as made by different persons are listed. One setting was made on each of the two diffraction images of the brighter component. The difference between the sum of these two settings and twice the setting on the central image of the companion is for each person given in Table 3 separately for $\Delta z \cos \delta$ and $\Delta \delta$ and for measures with the film turned toward the microscope (f) and through the glass (g). The sums of the powers 0, 1 and 2 of $2f - 300 + 2g - 300$ for $\Delta z \cos \delta$ are respectively 44, 1570 and 58472. The square of the mean deviation in $2f + 2g$ for one person therefore is $(44 \times 58472 - 1570^2) / 44 \times 43 = 57$ or in $(f + g) / 2$ $57 / 16 = 3.56 \mu^2$. This is the figure entered under the heading $M + P$ in the 8th column of Table 2. The mean square of the difference between $2f$ and $2g$ is $1300 / 44 = 29.5$. The figure $29.5 / 16 = 1.85 \mu^2$ is found under the heading M in the 9th column of Table 2. M is thus the square of the mean error of setting involved in the mean value of $(f + g) / 2$ and P is the square of the mean personal error.

In Table 4 the measures executed by RUDKJØBING, the only person who made complete measures of all the images, are given. The sums of the powers 0, 1 and 2 of $2f$ and $2g$ for $\Delta \delta$ are respectively for f : 66, 1764 and 51162 and for g : 66, 1660 and 44876. The sum of the squares of the deviations from the mean therefore is for $2f$: $(66 \times 51162 - 1764^2) / 66 = 4015$ and for $2g$: $(66 \times 44876 - 1660^2) / 66 = 2924$. The square of the mean deviation therefore is in the mean for $2f$ and $2g$: $(4015 + 2924) / (66 + 66 - 2) = 53.4$ or for f and g $53.4 / 4 = 13.4 \mu^2$. This is the figure entered in the last column of Table 1 under the heading $2M + I$, where I is the square of the mean error due to imperfections of the image.

TABLE 4.
Measures by RUDKJØBING.

| image no. | $\Delta\alpha \cos \delta$ | | | | $\Delta\delta$ | | | |
|-----------|----------------------------|---------------|----------|----------|----------------|------|----------|----------|
| | $2f$ — 300 | $2g$ — 300 | Σ | Δ | $2f$ | $2g$ | Σ | Δ |
| 1 | 19 | 24 | 43 | 5 | 17 | 21 | 38 | 4 |
| 2 | 10 | 15 | 25 | 5 | 15 | 15 | 30 | 0 |
| 3 | 18 | 17 | 35 | 1 | 47 | 29 | 76 | 18 |
| 4 | 8 | 1 | 9 | 7 | 25 | 30 | 55 | 5 |
| 5 | 18 | 10 | 28 | 8 | 28 | 32 | 60 | 4 |
| 6 | 22 | 26 | 48 | 4 | 33 | 24 | 57 | 9 |
| 7 | 1 | —22 | —21 | 23 | 9 | 23 | 32 | 14 |
| 8 | 12 | 13 | 25 | 1 | 18 | 22 | 40 | 4 |
| 9 | 24 | 22 | 46 | 2 | 27 | 25 | 52 | 2 |
| 10 | 24 | 16 | 40 | 8 | 22 | 30 | 52 | 8 |
| 11 | 14 | 14 | 28 | 0 | 29 | 27 | 56 | 2 |
| 12 | 6 | 4 | 10 | 2 | 32 | 27 | 59 | 5 |
| 13 | 40 | 24 | 64 | 16 | 30 | 29 | 59 | 1 |
| 14 | 18 | 13 | 31 | 5 | 21 | 24 | 45 | 3 |
| 15 | 19 | 32 | 51 | 13 | 32 | 17 | 49 | 15 |
| 16 | 23 | 20 | 43 | 3 | 20 | 21 | 41 | 1 |
| 17 | 12 | 15 | 27 | 3 | 35 | 32 | 67 | 3 |
| 18 | 13 | 22 | 35 | 9 | 36 | 27 | 63 | 9 |
| 19 | 13 | 18 | 31 | 5 | 26 | 24 | 50 | 2 |
| 20 | 23 | 25 | 48 | 2 | 28 | 20 | 48 | 8 |
| 21 | 21 | 18 | 39 | 3 | 29 | 31 | 60 | 2 |
| 22 | 16 | 15 | 31 | 1 | 24 | 29 | 53 | 5 |
| 23 | 24 | 23 | 47 | 1 | 35 | 29 | 64 | 6 |
| 24 | 14 | 9 | 23 | 5 | 16 | 20 | 36 | 4 |
| 25 | 16 | 2 | 18 | 14 | 19 | 6 | 25 | 13 |
| 26 | 14 | 23 | 37 | 9 | 28 | 25 | 53 | 3 |
| 27 | 12 | 14 | 26 | 2 | 19 | 33 | 52 | 14 |
| 28 | 28 | 30 | 58 | 2 | 24 | 12 | 36 | 12 |
| 29 | 22 | 21 | 43 | 1 | 39 | 29 | 68 | 10 |
| 30 | 13 | 22 | 35 | 9 | 21 | 28 | 49 | 7 |
| 31 | 23 | 23 | 46 | 0 | 15 | 28 | 43 | 13 |
| 32 | 27 | 29 | 56 | 2 | 20 | 25 | 45 | 5 |
| 33 | 17 | 21 | 38 | 4 | 40 | 30 | 70 | 10 |
| 34 | — 8 | — 1 | — 9 | 7 | 23 | 11 | 34 | 12 |
| 35 | — 28 | — 28 | — 56 | 0 | 38 | 29 | 67 | 9 |
| 36 | 22 | 32 | 54 | 10 | 37 | 23 | 60 | 14 |
| 37 | 15 | 14 | 29 | 1 | 31 | 30 | 61 | 1 |
| 38 | 15 | 14 | 29 | 1 | 23 | 24 | 47 | 1 |
| 39 | 11 | 19 | 30 | 8 | 29 | 22 | 51 | 7 |
| 40 | 28 | 27 | 55 | 1 | 24 | 12 | 36 | 12 |
| 41 | 6 | 14 | 20 | 8 | 27 | 25 | 52 | 2 |
| 42 | 12 | 10 | 22 | 8 | 31 | 35 | 66 | 4 |
| 43 | 22 | 18 | 40 | 4 | 27 | 28 | 55 | 1 |
| 44 | 12 | 27 | 39 | 15 | 39 | 27 | 66 | 12 |
| 45 | 15 | 13 | 28 | 2 | 8 | 24 | 32 | 16 |
| 46 | 11 | 21 | 32 | 10 | 19 | 34 | 53 | 15 |
| 47 | 19 | 21 | 40 | 2 | 24 | 11 | 35 | 13 |
| 48 | 11 | 14 | 25 | 3 | 22 | 33 | 55 | 11 |
| 49 | 9 | 12 | 21 | 3 | 28 | 23 | 51 | 5 |
| 50 | 22 | 24 | 46 | 2 | 20 | 15 | 35 | 5 |
| 51 | 21 | 22 | 43 | 1 | 15 | 13 | 28 | 2 |
| 52 | — 10 | — 9 | — 19 | 1 | 30 | 23 | 53 | 7 |
| 53 | 30 | 6 | 36 | 24 | 23 | 35 | 58 | 12 |
| 54 | 4 | 7 | 11 | 3 | 22 | 31 | 53 | 9 |
| 55 | 13 | 17 | 30 | 4 | 40 | 35 | 75 | 5 |
| 56 | 7 | 19 | 26 | 12 | 30 | 25 | 55 | 5 |
| 57 | 24 | 32 | 56 | 8 | 25 | 26 | 51 | 1 |
| 58 | 21 | 15 | 36 | 6 | 29 | 23 | 52 | 6 |
| 59 | 12 | 10 | 22 | 2 | 37 | 37 | 74 | 0 |
| 60 | 12 | 17 | 29 | 5 | 26 | 25 | 51 | 1 |
| 61 | 10 | 16 | 26 | 6 | 24 | 19 | 43 | 5 |
| 62 | 12 | 20 | 32 | 8 | 19 | 24 | 43 | 5 |
| 63 | 18 | 17 | 35 | 1 | 36 | 38 | 74 | 2 |
| 64 | 13 | 17 | 30 | 4 | 36 | 23 | 59 | 13 |
| 65 | 20 | 15 | 35 | 5 | 35 | 23 | 58 | 12 |
| 66 | 10 | 15 | 25 | 5 | 28 | 30 | 58 | 2 |

FIGURE 2.

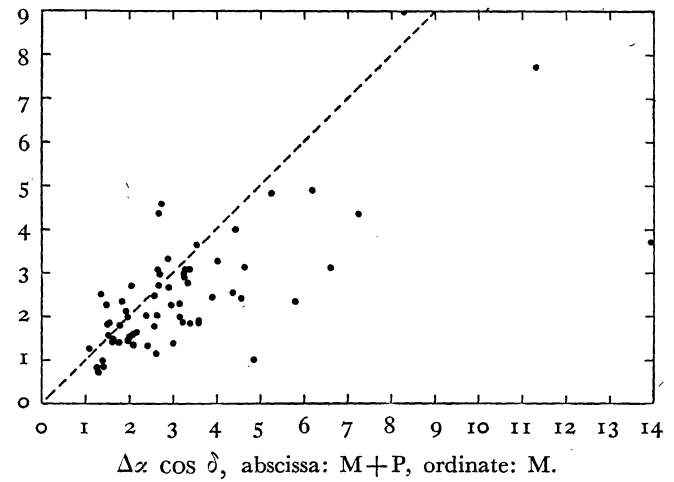
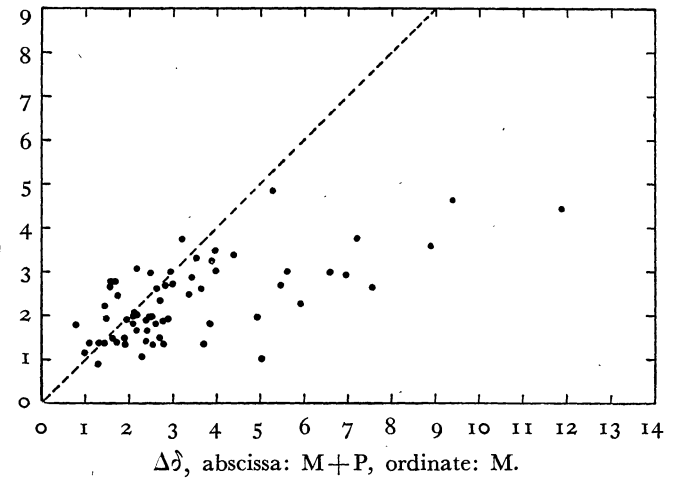


FIGURE 3.



In Figures 2 and 3 the relation between $M + P$ as abscissa and M as ordinate is represented by a point for each image as measured by different persons. The existence of personal errors will therefore manifest itself by a preference of the points to lie below the 45° line.

Though no general conclusion can be drawn from a single plate measured by a number of persons small from a statistical point of view the evidence available supports the idea that personal errors exist also in photographic measures of double stars and that they are of two kinds, viz. 1° personal errors mainly in distance (in casu practically in $\Delta\alpha \cos \delta$) due to the presence of an image close to the one pointed at and 2° personal differences in the interpretation of faint