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Stroboscopic model of transport through a quantum dot with spin-orbit scattering

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We present an open version of the symplectic kicked rotator as a stroboscopic model of electrical conduction through an open ballistic quantum dot with spin-orbit scattering. We demonstrate numerically and analytically that the model reproduces the universal weak localization and weak antilocalization peak in the magnetoconductance, as predicted by random-matrix theory (RMT). We also study the transition from weak localization to weak antilocalization with increasing strength of the spin-orbit scattering, and find agreement with RMT.

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I. INTRODUCTION

Electrical conduction in semiconductor heterostructures is affected by the spin degree of freedom through spin-orbit scattering. In quantum dots with chaotic scattering a statistical approach is appropriate. The spin-orbit Hamiltonian (of either Rashba or Dresselhaus form) has a special structure, that of a non-Abelian vector potential. By a gauge transformation Aleiner and Fal'ko identified all possible symmetry classes and described the crossovers between them by means of random-matrix theory (RMT).¹ This RMT has been extended by Brouwer *et al.* to the case that the spin-orbit scattering is nonuniform and thus the gauge transformation cannot be made.^{2,3} Experiments are in good agreement with the predictions of the theory.^{4,5} Recently a semiclassical theory of quantum dots with spin-orbit scattering has been developed.^{6,7} Exact quantum mechanical calculations of such "Rashba billiards" have also been reported.⁸ In this paper we will focus on the regime of strong chaos, where RMT and semiclassics agree.

Here we present a fully quantum mechanical computer simulation to test the theory. In the case of spinless chaotic quantum dots, the stroboscopic model known as the quantum kicked rotator has been proven to be quite successful.^{9–15} This model exploits the fact that, although the phase space of the open quantum dot is four dimensional, the dynamics can be described, on time scales greater than the time of flight across the dot, as a mapping between points on a two-dimensional Poincaré surface of section. The kicked rotator gives a map on a two-dimensional phase space that has the same phenomenology as open quantum dots.

In this paper we extend the model of the open kicked rotator to include spin-orbit scattering in a perpendicular magnetic field. We begin by describing the known model for a closed chaotic quantum dot¹⁶ with spin-orbit scattering in Sec. II A, before discussing the opening up of the model in Sec. II B. The relation of the model to RMT is given in Sec. III. This relation will give us a mapping between the model parameters and the microscopic parameters of a chaotic quantum dot. Numerical results for the weak (anti)localization peak and its dependence on magnetic field and spin-orbit scattering strength are presented in Sec. IV and compared with the analytical predictions from Sec. III.

II. DESCRIPTION OF THE MODEL

A. Closed system

The symplectic kicked rotator has been introduced by Scharf¹⁶ and studied extensively in Refs. 17–19. We summarize this known model of the closed system before proceeding to the open system in the next subsection.

The symplectic kicked rotator describes an electron moving along a circle with moment of inertia I_0 , kicked periodically at time intervals τ_0 with a kicking strength that is a function of position and spin. We choose units such that $\tau_0 \equiv 1$ and $\hbar \equiv 1$. The Hamiltonian H is given by^{16,17}

$$H = \frac{1}{2}(p + p_0)^2 + V(\theta) \sum_{n=-\infty}^{\infty} \delta_s(t - n), \quad (2.1a)$$

$$V(\theta) = K \cos(\theta + \theta_0) + K_{SO}(\sigma_1 \sin 2\theta + \sigma_3 \sin \theta). \quad (2.1b)$$

We have introduced the symmetrized delta function $\delta_s(t) = [\delta(t + \epsilon) + \delta(t - \epsilon)]/2$, with ϵ an infinitesimal. The dimensionless angular momentum operator $p = -i\hbar_{\text{eff}}\partial/\partial\theta$, with $\hbar_{\text{eff}} = \hbar\tau_0/I_0$ the effective Planck constant, is canonically conjugate to the angle $\theta \in [0, 2\pi)$. The kicking potential $V(\theta)$ contains the Pauli spin matrices

$$\sigma_1 = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \quad \sigma_2 = \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \quad \sigma_3 = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}. \quad (2.2)$$

Potential scattering is parameterized by the kicking strength K and spin-orbit scattering by K_{SO} . We choose smoothly varying functions of θ , corresponding to a smooth potential. Disorder can be added via a rapidly varying function of θ , see Ref. 20.

Spin rotation symmetry is broken if $K_{SO} \neq 0$. The generalized time-reversal symmetry¹⁶

$$\mathcal{T}: \theta \mapsto -\theta, \quad p \mapsto p, \quad \sigma_i \mapsto -\sigma_i, \quad t \mapsto -t, \quad (2.3)$$

is preserved if $\theta_0 = 0$ and is broken if $\theta_0 \in (0, \pi)$. A nonzero p_0 ensures that the Hamiltonian has no other unitary or antiunitary symmetries.¹⁶

Notice that the roles of p and θ are interchanged in T compared to the conventional time-reversal symmetry of the Rashba Hamiltonian and the spinless kicked rotator, which reads

$$T: \theta \mapsto \theta, \quad p \mapsto -p, \quad \sigma_i \mapsto -\sigma_i, \quad t \mapsto -t. \quad (2.4)$$

For this reason time-reversal symmetry in the symplectic kicked rotator is broken by a displacement of θ , rather than by a displacement of p as in the spinless kicked rotator.²¹

The stroboscopic time evolution of a wave function is governed by the Floquet operator

$$\mathcal{F} = T \exp \left[-\frac{i}{\hbar_{\text{eff}}} \int_{t_0}^{t_0+1} H(t) dt \right], \quad (2.5)$$

where T denotes time ordering of the exponential. In the range $[-1/2, 1/2]$ only $t_0=0$ and $t_0=-1/2$ preserve T -symmetry for $\theta_0=0$. We will find it convenient to choose $t_0=-1/2$ for numerical calculations and $t_0=0$ for analytical work.

For $p_0=0$ the reduction of the Floquet operator to a discrete finite form is obtained for special values of \hbar_{eff} , known as resonances.²¹ For $\hbar_{\text{eff}}=4\pi/M$, with M an integer, the Floquet operator is represented by an $M \times M$ matrix of quaternions. (A quaternion is a 2×2 matrix $q=q_0\mathbb{1}+iq_1\sigma_1+iq_2\sigma_2+iq_3\sigma_3$ with q_i a complex number and $\mathbb{1}$ the 2×2 unit matrix.) For this value of \hbar_{eff} the momentum is restricted to $p \in [0, 4\pi)$, i.e., one can think of the Floquet operator as describing a map on a torus. For $t_0=-1/2$ the matrix elements in the p representation are given by

$$\mathcal{F}_{ll'} = (\Pi U X U^\dagger \Pi)_{ll'}, \quad l, l' = 0, 1, \dots, M-1, \quad (2.6a)$$

$$\Pi_{ll'} = \delta_{ll'} e^{-i\pi l^2/M} \mathbb{1}, \quad (2.6b)$$

$$U_{ll'} = M^{-1/2} e^{-i2\pi ll'/M} \mathbb{1}, \quad (2.6c)$$

$$X_{ll'} = \delta_{ll'} e^{-i(M/4\pi)V(2\pi ll'/M)}. \quad (2.6d)$$

For $t_0=0$ one has instead

$$\mathcal{F} = U X^{1/2} U^\dagger \Pi^2 U X^{1/2} U^\dagger. \quad (2.7)$$

These maps (2.6) and (2.7) are equivalent to the Hamiltonian (2.1) with $p_0=0$. A nonzero p_0 may be introduced into the map by replacing Π with²¹

$$\Pi_{ll'} = \delta_{ll'} e^{-i\pi(l+l_0)^2/M} \mathbb{1}, \quad l_0 = \frac{p_0 M}{4\pi}. \quad (2.8)$$

This map is not rigorously equivalent to the Hamiltonian (2.1), but it has the same classical limit (for $K_{\text{SO}}=0$).¹³

The generalized time-reversal symmetry (2.3) is expressed by the identity

$$\mathcal{F} = \mathcal{F}^R, \quad \text{if } \theta_0 = 0. \quad (2.9)$$

The superscript R denotes the dual of a quaternionic matrix

$$\mathcal{F}^R \equiv \sigma_2 \mathcal{F}^T \sigma_2.$$

Here T denotes the transpose in the basis of eigenstates of p (p representation). To verify Eq. (2.9) note that

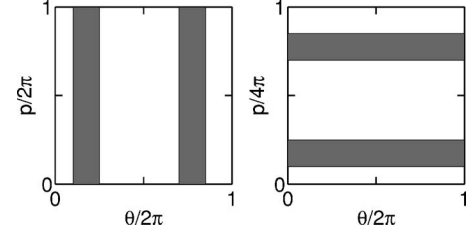


FIG. 1. Location of the absorbing boundary conditions (grey rectangles) in the classical phase space of the open kicked rotator. To ensure that the openings do not break the time reversal symmetry they are oriented parallel to the p axis in the spinless kicked rotator (left panel) and parallel to the θ axis in the symplectic kicked rotator (right panel).

$\sigma_2 \sigma_i^T \sigma_2 = -\sigma_i$ and that the transpose in p representation takes θ to $-\theta$.

B. Open system

To describe electrical conduction we open up the kicked rotator, following the general scheme of Refs. 9–12. We model a pair of N -mode ballistic point contacts that couple the quantum dot to electron reservoirs, by imposing open boundary conditions in a subspace of Hilbert space represented by the indices $l_k^{(\mu)}$. The subscript $k=1, 2, \dots, N$, with $N=N_1+N_2$, labels the modes (both spin directions), and the superscript $\mu=1, 2$ labels the point contacts. The $N \times M$ quaternionic projection matrix P is given by

$$P_{kk'} = \begin{cases} 1 & \text{if } k' = l_k^{(\mu)}, \\ 0 & \text{otherwise.} \end{cases} \quad (2.10)$$

The matrices P and \mathcal{F} together determine the scattering matrix

$$S(\varepsilon) = P(e^{-i\varepsilon} - \mathcal{F} Q^T Q)^{-1} \mathcal{F} P^T, \quad (2.11)$$

where $\varepsilon \in [0, 2\pi)$ is the quasi-energy and $Q^T Q = 1 - P^T P$. One readily verifies that S is unitary.

We need to ensure that the introduction of the point contacts does not break the T -symmetry

$$S(\varepsilon) = S^R(\varepsilon) \quad \text{if } \theta_0 = 0 \quad (2.12)$$

or for nonzero θ_0 the more general duality relation

$$S(\theta_0) = S^R(-\theta_0). \quad (2.13)$$

This is assured by choosing the absorbing boundary conditions in a strip parallel to the θ axis, rather than parallel to the p axis as in the spinless kicked rotator (see Fig. 1). The difference is due to the exchange of the roles of p and θ in the time-reversal symmetry operation, compare Eqs. (2.3) and (2.4).

By grouping together the N_μ indices belonging to the same point contact, the $N \times N$ quaternionic matrix S can be decomposed into 4 sub-blocks containing the quaternionic transmission and reflection matrices

$$S = \begin{pmatrix} r & t \\ t' & r' \end{pmatrix}. \quad (2.14)$$

The value of ε is arbitrary; we will take $\varepsilon=0$ in the analytical calculations and average over ε in the numerics. The T symmetry (2.12) requires that $r = \sigma_2 r^T \sigma_2$, $r' = \sigma_2 r'^T \sigma_2$, and $t' = \sigma_2 t^T \sigma_2$.

The conductance G follows from the Landauer formula

$$G = \frac{e^2}{h} \text{Tr} t t^\dagger, \quad (2.15)$$

where the trace Tr is over channel indices as well as spin indices. Unitarity of S ensures that $\text{Tr} t t^\dagger = \text{Tr} t' t'^\dagger$. For $\theta_0=0$ the eigenvalues of $t t^\dagger$ are doubly degenerate due to the T symmetry (Kramers degeneracy). It will prove useful to write the Landauer formula in the form^{2,3}

$$G = \frac{2e^2}{h} \frac{N_1 N_2}{N} - \frac{e^2}{h} \text{Tr} S \Lambda S^\dagger \Lambda \equiv G_0 + \delta G, \quad (2.16)$$

with Λ a diagonal matrix having diagonal elements

$$\Lambda_{jj} = \begin{cases} N_2/N, & j = 1, \dots, N_1, \\ -N_1/N, & j = N_1 + 1, \dots, N. \end{cases} \quad (2.17)$$

The term $G_0 = (2e^2/h) N_1 N_2 / N$ is the classical conductance and the term δG , of order e^2/h , is the quantum correction from the weak localization effect.

III. RELATION TO RANDOM-MATRIX THEORY

Random-matrix theory (RMT) gives universal predictions for the quantum correction δG in Eq. (2.16). We calculate this quantity for the symplectic kicked rotator and compare with RMT. This will give us the relation between the parameters of the stroboscopic model and the microscopic parameters of the quantum dot.

The three universality classes of RMT are labeled by $\beta = 1, 2, 4$, with²²

$$\delta G_{\text{RMT}} = \frac{\beta - 2}{2\beta} \frac{e^2}{h}. \quad (3.1)$$

In the absence of T symmetry one has $\beta=2$. In the presence of T symmetry one has $\beta=1$ (4) in the presence (absence) of spin rotation symmetry. We will investigate the three symmetry breaking transitions $\beta=1 \rightarrow 2$, $\beta=1 \rightarrow 4$, and $\beta=4 \rightarrow 2$ in separate subsections.

A. $\beta=1 \rightarrow 2$ transition

The $\beta=1 \rightarrow 2$ transition takes place in the absence of spin-orbit scattering ($K_{\text{SO}}=0$). This transition was studied in Ref. 13 for the case that the symmetry T' rather than T is broken. To fully characterize the model we need to reconsider this transition for the case of T -symmetry breaking.

For small θ_0 , $\cos(\theta + \theta_0) \approx \cos \theta - \theta_0 \sin \theta$ and the Floquet matrix (2.7) takes the form

$$\mathcal{F}(K_{\text{SO}}=0, \theta_0 \rightarrow 0) = e^{\theta_0 W} \mathcal{F}_0 e^{\theta_0 W}, \quad (3.2a)$$

$$W = UYU^\dagger, \quad Y_{ll'} = \delta_{ll'} i(KM/8\pi) \sin(2\pi l/M). \quad (3.2b)$$

Here $\mathcal{F}_0 = \mathcal{F}(K_{\text{SO}}=0, \theta_0=0)$ is unitary symmetric and W is real antisymmetric. The scattering matrix (2.11) (at $\varepsilon=0$) becomes

$$S = T(1 - \mathcal{F}_0 R)^{-1} \mathcal{F}_0 T', \quad (3.3a)$$

$$T = P e^{\theta_0 W}, \quad (3.3b)$$

$$T' = e^{\theta_0 W} P^T, \quad (3.3c)$$

$$R = e^{\theta_0 W} Q^T Q e^{\theta_0 W}. \quad (3.3d)$$

Substitution of S into Eq. (2.16) gives the conductance G .

To make contact with RMT we assume that \mathcal{F}_0 is a random matrix from the circular orthogonal ensemble (COE), expand the expression for G in powers of \mathcal{F}_0 and average \mathcal{F}_0 over the COE. In the regime $1 \ll N \ll M$, we can perform the average over the unitary group with the help of the diagrammatic technique of Ref. 23. Since $\text{Tr} \Lambda = 0$ only the maximally crossed diagrams contribute to leading order in N . The result for the average quantum correction becomes

$$\langle \delta G \rangle = -\frac{2e^2}{h} \text{tr} T^\dagger \Lambda T (T' \Lambda T'^\dagger)^T \frac{1}{M - \text{tr} R^\dagger R}. \quad (3.4)$$

The factor of 2 comes from the spin degeneracy and the trace tr is over channel indices only. The two remaining traces are evaluated in the limit $N, M \rightarrow \infty$ at fixed N/M . We find

$$M^{-1} \text{tr} T^\dagger \Lambda T (T' \Lambda T'^\dagger)^T = \frac{N_1 N_2}{N^2} \frac{N}{M}, \quad (3.5)$$

$$M^{-1} \text{tr} R^\dagger R^T = 1 - N/M - \theta_0^2 (KM/4\pi)^2 (1 - N/M). \quad (3.6)$$

Substitution into Eq. (3.4) gives the average quantum correction

$$\langle \delta G \rangle = -\frac{e^2}{h} \frac{2N_1 N_2}{N^2} \frac{1}{1 + (\theta_0/\theta_c)^2}, \quad (3.7a)$$

$$\theta_c = \frac{4\pi\sqrt{N}}{KM^{3/2}}. \quad (3.7b)$$

The RMT result has the same Lorentzian profile^{22,24}

$$\delta G_{\text{RMT}} = -\frac{e^2}{h} \frac{2N_1 N_2}{N^2} \frac{1}{1 + (B/B_c)^2}, \quad (3.8a)$$

$$B_c = C \frac{h}{eL^2} \left(\frac{NL\Delta}{\hbar v_F} \right)^{1/2}, \quad (3.8b)$$

with C a numerical constant of order unity, $L = \sqrt{A}$ the size of the dot, A the area of the dot, $\Delta = 2\pi\hbar^2/mA$ the mean spacing

of the Kramers degenerate levels, and v_F the Fermi velocity. Comparison of Eqs. (3.7) and (3.8) allows us to identify

$$\theta_0/\theta_c = B/B_c. \quad (3.9)$$

B. $\beta=1 \rightarrow 4$ transition

The $\beta=1 \rightarrow 4$ transition is realized by turning on spin-orbit scattering (K_{SO}) in the absence of a magnetic field ($\theta_0=0$). In this transition the quaternionic structure of the Floquet matrix plays a role. The Floquet matrix (2.7) has the form

$$\mathcal{F}(K_{SO}, \theta_0=0) = e^{K_{SO}A} \mathcal{F}_0 e^{K_{SO}A}, \quad (3.10a)$$

$$A = U(\sigma_1 Y_1 + \sigma_3 Y_3) U^\dagger, \quad (3.10b)$$

$$(Y_1)_{ll'} = -\delta_{ll'} i(M/8\pi) \sin(4\pi l/M), \quad (3.10c)$$

$$(Y_3)_{ll'} = -\delta_{ll'} i(M/8\pi) \sin(2\pi l/M). \quad (3.10d)$$

The matrix A is real antisymmetric and thus $A^* = -A$, where the asterisk denotes quaternion complex conjugation. (The complex conjugate of a quaternion q is defined as $q^* = q_0^* + i q_1^* \sigma_1 + i q_2^* \sigma_2 + i q_3^* \sigma_3$.) The scattering matrix takes the same form (3.3a), but now with

$$T = P e^{K_{SO}A}, \quad (3.11a)$$

$$T' = e^{K_{SO}A} P^T, \quad (3.11b)$$

$$R = e^{K_{SO}A} Q^T Q e^{K_{SO}A}. \quad (3.11c)$$

The average of \mathcal{F}_0 over the ensemble of unitary symmetric matrices only involves the channel indices and not the spin indices. To keep the quaternions in the correct order we adopt the tensor product notation of Brouwer *et al.*^{2,3} The average of δG over \mathcal{F}_0 gives, to leading order in N ,

$$\langle \delta G \rangle = \frac{e^2}{h} \sum_{\mu\nu} \left[\tau \frac{\text{tr} E \otimes E'^*}{M \mathbb{1} \otimes \mathbb{1} - \text{tr} R \otimes R^*} \tau \right]_{\mu\nu, \mu\nu}, \quad (3.12)$$

where $\tau = \mathbb{1} \otimes \sigma_2$, $E = T^\dagger \Lambda T$, and $E' = T' \Lambda T'^\dagger$. The tensor product has a backward multiplication in the second argument

$$(a \otimes b)(c \otimes d) \equiv ac \otimes db, \quad (3.13)$$

and the indices μ and ν are the spin indices.

The two traces are calculated in the limit $K_{SO} \rightarrow 0$, $N, M \rightarrow \infty$ at fixed N/M , leading to

$$M^{-1} \text{tr} E \otimes E'^* = \frac{N_1 N_2}{N^2} \frac{N}{M} \mathbb{1} \otimes \mathbb{1}, \quad (3.14a)$$

$$\begin{aligned} M^{-1} \text{tr} R \otimes R^* &= (1 - N/M) [1 - 4K_{SO}^2 (M/8\pi)^2] \mathbb{1} \otimes \mathbb{1} \\ &\quad + 2K_{SO}^2 (M/8\pi)^2 (1 - N/M) \\ &\quad \times (\sigma_1 \otimes \sigma_1 + \sigma_3 \otimes \sigma_3). \end{aligned} \quad (3.14b)$$

After substitution into Eq. (3.12) there remains a matrix structure that can be inverted, resulting in

$$\langle \delta G \rangle = \frac{e^2}{h} \frac{N_1 N_2}{N^2} \left(1 - \frac{2}{1 + 2a^2} - \frac{1}{1 + 4a^2} \right), \quad (3.15a)$$

$$a = K_{SO}/K_c, \quad K_c = \frac{4\pi\sqrt{2N}}{M^{3/2}}. \quad (3.15b)$$

The RMT result has the same functional form,² with $a = (2\pi\hbar N / \tau_{SO} \Delta)^{1/2}$. Here τ_{SO} is the spin-orbit scattering time. Thus we identify

$$K_{SO}/K_c = (2\pi\hbar N / \tau_{SO} \Delta)^{1/2}. \quad (3.16)$$

C. $\beta=4 \rightarrow 2$ transition

In the presence of strong spin-orbit scattering ($K_{SO} \gg K_c$) the Floquet matrix takes for small θ_0 the same form as in Eq. (3.2a) for $K_{SO}=0$, but now $\mathcal{F}_0 = \mathcal{F}(K_{SO} \gg K_c, \theta_0=0)$ is a unitary self-dual matrix rather than a unitary symmetric matrix. We can repeat exactly the same steps as we did for $K_{SO}=0$ but with \mathcal{F}_0 a random matrix in the circular symplectic ensemble (CSE). We then average \mathcal{F}_0 over the CSE. This leads to

$$\langle \delta G \rangle = \frac{e^2}{h} \frac{N_1 N_2}{N^2} \frac{1}{1 + (\theta_0/\theta_c)^2}, \quad (3.17)$$

with θ_c as in Eq. (3.7b). The width of the Lorentzian is therefore the same in the $\beta=1 \rightarrow 2$ and $\beta=4 \rightarrow 2$ transitions, in agreement with RMT.²²

IV. NUMERICAL RESULTS

The numerical technique we use is the same as has been used before for the spinless kicked rotator.^{12,13} A combination of an iterative procedure for matrix inversion and the fast-Fourier-transform algorithm allows for an efficient calculation of the scattering matrix from the Floquet matrix.

The average conductance $\langle G \rangle$ was calculated with the Landauer formula (2.15) by averaging over 60 different uniformly distributed quasi-energies and 40 randomly chosen lead positions. The quantum correction $\langle \delta G \rangle$ is obtained by subtracting the classical conductance G_0 . The numerical data is shown in Figs. 2 and 3. The magnetic field parameter θ_0 is given in units of θ_c from Eq. (3.7b) and the spin-orbit scattering strength parameter K_{SO} is given in units of K_c from Eq. (3.15b). The solid lines are the analytical predictions (3.7), (3.15), and (3.17) without any fitting parameter.

The small difference between the data and the predictions can be attributed to an uncertainty in the value G_0 of the classical conductance. A small vertical offset (corresponding to a change in G_0 of about 0.1%) can correct for this (dotted lines in Fig. 2). The strongly non-Lorentzian lineshape seen by Rahav and Brouwer^{14,15} in the spinless kicked rotator is not observed here.

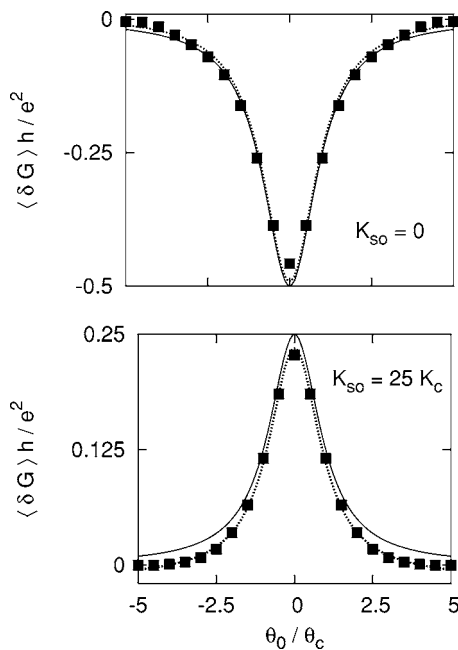


FIG. 2. Average quantum correction $\langle \delta G \rangle$ to the conductance as a function of the T -symmetry breaking parameter θ_0 . The data points are for the symplectic kicked rotator characterized by $K=41$, $M=500$, $N_1=N_2=10$, $l_0=0.2$. The solid lines are the analytical predictions (3.7) and (3.17) in the absence and presence of spin-orbit scattering. The dotted lines are the solid lines with a vertical offset, to account for a difference between the predicted and actual value of the classical conductance G_0 .

V. CONCLUSION

We have presented a numerically highly efficient model of transport through a chaotic ballistic quantum dot with spin-orbit scattering, extending the earlier work on the spinless kicked rotator. Through a simple assumption of a random Floquet matrix we have derived analytical predictions for the conductance of the model as a function of spin-orbit scattering strength and magnetic field. The functional form

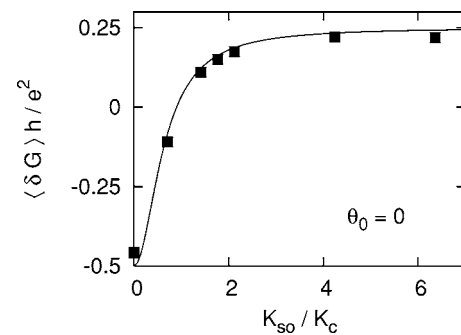


FIG. 3. Average quantum correction $\langle \delta G \rangle$ to the conductance as a function of spin-orbit scattering strength K_{so} at zero magnetic field. Other parameters are the same as in Fig. 2. The solid line is the analytical prediction (3.15) for the crossover from weak localization to weak antilocalization.

of the conductance coincides with random-matrix theory (RMT) and through this correspondence we obtain a mapping from microscopic parameters to model parameters. Numerical calculations are in good agreement with the analytical predictions.

In this paper we have applied the model in a parameter regime where the transport properties of the system are analytically known through RMT, in order to test the validity of the model. In future work this model may provide a starting point for studies of transport properties in parameter regimes where RMT is known to break down. In certain cases, for example, in the study of the effect of a finite Ehrenfest time on weak antilocalization, very large system sizes are required (see Refs. 14 and 15). An efficient dynamical model, as the one presented in this paper, is then a valuable tool.

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