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COMMUNICATIONS FROM THE OBSERVATORY AT LEIDEN.

Photographic Photometry of VW Cephei, by *H. van Gent*.

The star VW Cep = B.D. + 75° 752 = H.D. 197433 was found by ADAMS to have a spectrum similar to that of WUMa and for this reason it was examined for variability by SCHILT, who in fact found a lightcurve of the expected character with a range of $m.35$ (*Ap. J.* 64, 221; 1926).

VW Cep has a remarkable proper motion, viz. $.632$ yearly in the direction $32^{\circ}.8$. The parallax has been found to be $+''044 \pm ''013$ (m. e.) and is thus hardly measurable. From the spectrum: G5 (dwarf), visual magnitude: $7^m.62$, and duplicity ($\Delta m = +^m.75$) a parallax of about $''031$ may be expected. This corresponds to a lateral velocity of $4.75 \times .632 / .031 = 97$ km/s, so that the star very probably belongs to those of high velocity above OORT's limit of 63 km/s.

By the courtesy of Dr. SCHILT observations of this interesting object could be started in Leiden soon after establishment of its variability. The considerable brightness and high declination of the variable make it an easy object to observe during a great part of the year at this latitude.

The instrument used was the 33 cm photographic Leiden refractor, the scale being $1 \text{ mm} = 39''.37$. A coarse grating consisting of wires 3.9 mm thick, separated by free spaces of 3.7 mm width, was placed in front of the objective. The difference in magnitude between the central image and the spectra of the first order, which has been found to be $m.92$, was provisionally taken as unit, the reduction factor $.92$ having only been applied to the final results.

The diameter of the grating was 294 mm. Eastman 40 plates were used throughout.

The variable and the comparison star B. D. + 74° 877 were alternately placed next to each other in a row on the plate, the distance between two consecutive exposures being $.8 \text{ mm}$ or $30''$. The time of exposure was 80 sec. with 40 sec. in between.

After my departure to Johannesburg the plates have been measured at Leiden in the Schilt microphotometer by C. J. KOOREMAN. The galvanometer readings for the central image and the diffraction

images of the first order were registered for both VW Cep and the comparison star. For each of the two stars the sum and the difference between these two galvanometer readings were formed. Usually the difference in magnitude between the two stars was then simply calculated as the difference between the two sums divided by the sum of the two differences. In this procedure it is assumed that the galvanometer reading is a quadratic function of the magnitude, which in most cases is true with sufficient accuracy for the present purpose.

Only in the case of the 4 plates 1183, 1194, 1197 and 1198 the galvanometer readings were first converted into provisional magnitudes.

Of each exposure the images of both stars were measured, not only, as was originally intended, those placed next to each other in a row. The measures of the outside images were reduced to the principal row by a graphical procedure, thus eliminating systematic differences arising from unequal sensitiveness of the plate and similar causes.

The distance between the variable and the comparison star was 31 mm on the plate or $20'$.

The results for each exposure are given in the first and third column of Table 2. Here and elsewhere in this paper

J. D. means J. D. hel. M. astr. T. Grw.

The period was determined from the 9 epochs of minimum given in Table 3.

TABLE 3.

J. D.	epoch	O—C	observer
^d 2424658.7586	0	+ ^d .0005	SCHILT
4695.4934	264	— 28	VAN GENT
4656.4719	271	+ 16	»
4711.4982	379	— 14	»
4757.4245	709	+ 22	»
4758.3963	716	— 1	»
4907.7154	1789	+ 6	»
4955.5854	2133	— 4	»
5632.3195	6996	— 1	OOSTERHOFF

The first of these epochs was derived from the 105 observations given by SCHILT (*l. c.*) The phases of these observations were, after reduction of the J. D. to the sun, calculated from the formula:

$$\text{phase} = 7^{\text{d}^{-1}} \cdot 18596 \text{ (J. D. - 2420000)}$$

The observations were then arranged according to phase and divided into 21 groups of 5 observations each. The mean values thus obtained are given in Table 4. Through these 21 points a curve was drawn and, using the method described in *B. A. N.* 147 and 166, the phase of minimum was found to be $P \cdot 653$, corresponding to the epoch J. D. 2424658^d·7586.

TABLE 4.

Mean values of every 5 observations made by SCHILT

P	m	P	m	P	m
·019	8·12	·290	8·21	·612	8·46
·062	8·18	·327	8·21	·677	8·45
·102	8·19	·368	8·28	·723	8·44
·144	8·14	·407	8·26	·787	8·39
·187	8·18	·447	8·27	·852	8·31
·223	8·15	·498	8·37	·912	8·27
·257	8·17	·552	8·41	·975	8·19

From the differences between observations following each other in phase the mean error of a single of SCHILT's observations was found to be $\pm \text{m} \cdot 071$ and their total weight $105/(\pm 071)^2 = 20700 \text{ m}^{-2}$.

(The only individual minimum thoroughly observed by SCHILT is that of 1926 June 13. The epoch derived from this minimum alone is J. D. 2424680^d·7461).

From my own material 7 epochs of individual minima were determined by the aid of series of consecutive observations covering both the descending and ascending branch of the lightcurve.

Furthermore the epoch of a recent minimum, more than doubling the interval of time covered by the observations, was kindly determined by P. TH. OOSTERHOFF.

From the 9 minima of Table 3 the period was found by a least squares solution to be $\text{d} \cdot 13915974 \pm \text{d} \cdot 00000026$ (m. e.) and the reciprocal period $7^{\text{d}^{-1}} \cdot 185986 \pm \text{d}^{-1} \cdot 000014$ (m. e.). In reality the phase was calculated for each individual observation of Table 2 from the formula

$$\text{phase} = 7^{\text{d}^{-1}} \cdot 18598 \text{ (J. D. - 2420000)}$$

For each plate the last figure of the number of epochs calculated by this formula has been indicated in order to distinguish the even from the odd minima. The odd minima were found to be deeper than the even ones by $\text{m} \cdot 04 \pm \text{m} \cdot 02$ (m. e.). The difference therefore is not warranted and has been neglected.

All the 1340 observations were then arranged according to phase and divided into 134 groups of 10 observations each. The mean results thus obtained are given in Table 5, were also 26 groups of 50 or 60 observations each are formed. These are represented in figure 1.

A curve was drawn through these 26 points and read off on 100 places equidistant in phase. Then for each provisionally assumed value of the phase of the minimum the sum of the squares of the differences between the magnitude on the descending and ascending branch of the lightcurve was computed. From the 5 values of this sum indicated in Table 6 the phase of minimum found according to the formula given on page 39 of *B. A. N.* 166 is $P \cdot 7446$. This value was finally adopted.

FIGURE 1.

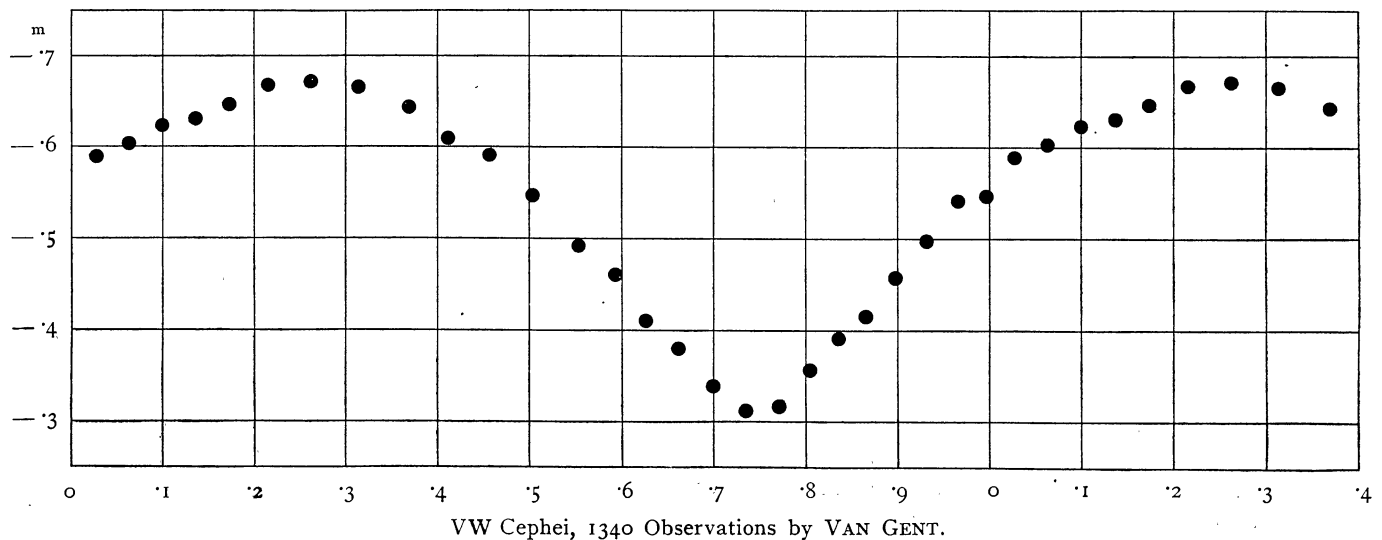


TABLE 6.

assumed phase of minimum	$\Sigma (\Delta m_{pr})^2$	calculated
P		
.735	.017921	.017931
.740	8656	8627
.745	5841	5866
.750	9651	9647
.755	19975	19973

The 134 mean values of 10 observations each as given in Table 5 were then arranged according to the phase counted from minimum. Strictly the individual observations ought to be arranged in this way, but practically the rearrangement of only the mean values of 10 observations is sufficient.

This new arrangement of the 134 mean values is presented in Table 7, where also mean values of 13 greater groups of 100 or 120 observations each are given. These 13 mean values are represented in Figure 2. After multiplication of the provisional magnitudes by .92, and assuming that the even and odd minima are equally deep and symmetrical, they form the final results presented in Table 8.

FIGURE 2.

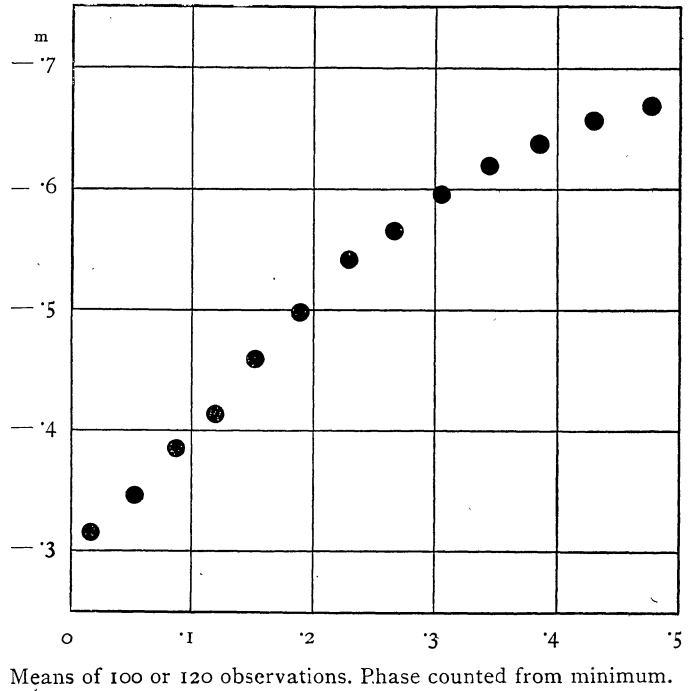


TABLE 8.

number of exposures	phase counted from minimum	.92 m_{pr}	magnitude counted from maximum	$\cos 4\pi P$	square of the intensity of the light received in units of its maximum value $1 - .3625 \cos^2 2\pi P$			"rectified" magnitude
					O	C	O-C	
	P	m	m					m
100	.0177	-.2894	.3270	+.994	.5475	.6386	+.0911	+.0835
100	.0530	-.3182	.2982	+.945	.5774	.6475	+.701	+.0622
100	.0876	-.3554	.2610	+.852	.6183	.6643	+.460	+.0390
100	.1195	-.3797	.2367	+.731	.6466	.6863	+.397	+.0323
100	.1520	-.4219	.1945	+.578	.6989	.7140	+.151	+.0116
100	.1888	-.4573	.1591	+.375	.7460	.7508	+.48	+.0035
100	.2291	-.4977	.1187	+.131	.8036	.7950	-.86	-.0058
100	.2665	-.5198	.0966	-.103	.8370	.8374	+.4	+.0003
100	.3052	-.5480	.0684	-.340	.8816	.8804	-.12	-.0008
100	.3446	-.5699	.0465	-.560	.9179	.9203	+.24	+.0014
100	.3854	-.5868	.0296	-.752	.9469	.9551	+.82	+.0047
120	.4298	-.6041	.0123	-.904	.9776	.9826	+.50	+.0028
120	.4765	-.6157	.0007	-.989	.9987	.9980	-.7	-.0004

The total range is only $m.33$ and the question arises if this is not merely due to ellipticity of the stars, the eclipse itself being only small.

According to H. N. RUSSELL (*Ap. J.* **36**, 63; 1912) the change in brightness caused by ellipticity of the stars can be written in the form

$$I^2 = 1 - \epsilon^2 \sin^2 i \cos^2 \vartheta,$$

where I is the intensity of the light received in units of its maximum value, ϵ the excentricity of the equatorial section of the stars, i the inclination of the orbit and ϑ the phase angle counted from minimum light.

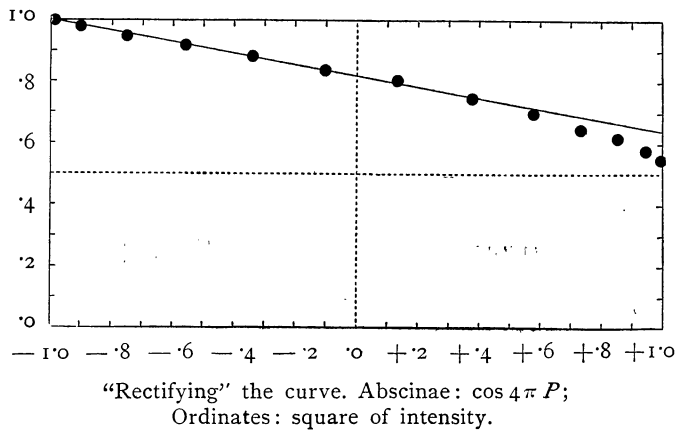
From the last 8 mean values of Table 8 the coefficient

$\epsilon^2 \sin^2 i$ was found by least squares to be .3625. The minimum value of ϵ is accordingly $\sqrt{.3625} = .60$.

Putting $\epsilon^2 \sin^2 i = .3625$ the lightcurve was then "rectified". The variation thus left to be explained by eclipse is indicated in the last column of Table 8. Its range is only $m.09$. Figure 3 represents the sixth column of Table 8. The form of the system remains rather uncertain. It only seems safe to state that there is no evidence of the difference between the present lightcurve and that of WUMa having any other important cause than difference in the inclinations of the orbits.

In the last column of Table 2 the deviation of each observed magnitude from a mean lightcurve is

FIGURE 3.



indicated. It will be seen, that some series of observations show systematic differences from the mean curve. (see Table 1, sixth column). As to the possible cause of these differences I want to call attention to the fact, that on the plate 1194 there are two series of exposures from two different nights. The systematic difference between these two series is $13 \times .92 = .12$, thus suggesting that the differences in question are merely due to changes in the atmospheric conditions. On the night (1926 Aug. 4), when VW Cep was found comparatively bright, mist was noted. As the spectrum of the comparison star is A2 against G5 for VW Cep, the sign of the difference mentioned seems reasonable.

The mean square of the difference between two consecutive mean values of m_{pr} in Table 7 is $.000461 m_{pr}^2$. Accordingly the mean error of a single observation is found to be $\pm .92 \sqrt{10 \times .000461/2} = \pm .0442$ and the total weight of all the observations $1340/(\pm .0442)^2 = 686400 m^{-2}$.

The root of the mean square of the differences given in Table 2 of the individual observations from a mean lightcurve indicate a greater m. e. than the above, viz. $.92 \times \sqrt{38.1} = \pm .0568$, corresponding to a total weight of $415000 m^{-2}$. In this connection it should be considered that a systematic deviation only increases the mean error as calculated in the second way. When these systematic deviations are taken into account to their full amount (which is somewhat exaggerating) the m. e. of one observation is found to be $\pm .0440$ and the total weight $694000 m^{-2}$.

In either way the lightcurve here presented appears to be the most accurate one that has so far been published of a variable of the WUMa type.

The mean epoch of minimum derived from the 1340 observations is

$$J. D. 2424798^d.4749.$$

I want to thank Mr. KOOREMAN and Mr. OOSTERHOFF for their kind co-operation, and especially Prof. HERTZSPRUNG for his very valuable advice and help during the preparation of this paper.

TABLE I.

plate no.	astronomical date	beginning of first and last exposure		number of exposures used	mean deviation of plate from general mean	mean square of deviation from general mean	mean square of deviation corrected for plate error	reduction to heliocentric time		
		h	m						h	m
1181 ¹⁾	1926 June 28	17	20	19	28	65	^m prov. + .015	^{m²} pr. .0019	^{m²} pr. .0017	d — .00110
1182	29	17	0	19	44	83	— 23	36	32	— 108
1183 ²⁾	30	16	48	20	8	92	— 64	92	52	— 106
1185 ³⁾	July 6	19	16	20	38	41	+ 9	17	17	— 95
1187	12	17	0	21	20	120	— 8	22	22	— 82
1188	12	21	40	21	48	5	+ 18	9	7	— 82
1189	13	17	10	21	18	40	— 13	22	21	— 80
1190	13	21	38	21	50	7	+ 73	68	18	— 80
1191	14	17	10	21	42	134	— 64	69	28	— 78
1193	17	17	20	21	52	129	— 21	26	21	— 71
1194 ⁴⁾	Aug. 4	18	18	18	32	7	— 126	172	16	— 28
1194 ⁵⁾	16	18	36	20	36	57	+ 4	17	17	+ 3
1195	29	19	40	23	52	102	+ 35	30	17	+ 36
1197	29	0	8	1	28	40	+ 68	57	12	+ 36
1198	30	19	4	22	8	89	+ 16	30	27	+ 38
1211 ⁶⁾	1927 Jan. 13	3	20	3	34	8	+ 20	11	8	+ 73
1211	26	13	8	14	44	49	+ 37	21	8	+ 42
1225	March 15	13	18	16	6	84	+ 8	14	13	— 80
1265 ⁷⁾	June 16	16	30	17	30	31	+ 74	71	17	— 129
1266 ⁸⁾	16	17	50	18	0	6	+ 48	29	7	— 129
1267 ⁹⁾	22	17	0	17	56	28	+ 31	22	12	— 120
1283	Aug. 2	19	56	22	54	45	+ 52	45	19	— 34
1285	Oct. 9	21	14	22	14	31	+ 19	30	27	+ 121
1286	9	23	8	23	48	21	+ 60	52	16	+ 121
1290	Dec. 6	23	50	0	40	26	+ 32	48	39	+ 138

¹⁾ stopped by dawn, ²⁾ smoke from electricity works, ³⁾ stopped by clouds, ⁴⁾ stopped by derangement of shutter, ⁵⁾ mist, ⁶⁾ stopped by clouds, ⁷⁾ somewhat mysty, full moon, bad seeing, ⁸⁾ stopped by mist, ⁹⁾ bad seeing, stopped by mist.

TABLE 2.

J. D. 2424695, plate no. 1181				d	P	m _{pr}	Δ _{m_{pr}}	d	P	m _{pr}	Δ _{m_{pr}}	d	P	m _{pr}	Δ _{m_{pr}}
d	P	m _{pr}	Δ _{m_{pr}}	4266	8428	-60	0	5250	9134	-68	-4	5058	6182	-65	+1
4418	1351	-63	+01	4280	438	60	0	5263	144	63	+1	5071	192	71	-5
4432	361	61	+3	4294	448	50	+9	5277	154	65	0	5085	202	67	-1
4446	371	61	+2	4308	458	59	-1	5291	164	66	-1	5099	212	78	-11
4460	381	61	+2	4322	468	60	-2	5305	174	63	+3	5113	222	70	-3
4473	391	60	+2	4335	478	61	-4	5319	184	61	+5	5127	232	71	-4
4487	401	62	0	4349	487	54	+2	5333	194	66	0	5141	242	71	-4
4501	411	60	+1	4363	497	60	-5	5347	204	67	-1	5155	252	66	+1
4515	421	65	-4	4377	507	63	-8	5360	214	67	0	5168	262	67	0
4529	431	55	+5	4391	517	57	-3	5374	224	70	-3	5182	272	73	-6
4543	440	60	-1	4405	527	53	0	5388	234	60	+7	5196	282	77	-10
4557	450	58	+1	4419	537	51	+1	J. D. 2424697, plate no. 1183							
4570	460	60	-2	4432	547	54	-3	4240	5595	-70	-25	5210	292	73	-7
4584	470	52	+5	4446	557	42	+8	4254	605	69	-25	5224	302	77	-11
4598	480	53	+4	4460	567	55	-6	4268	615	48	-5	5238	312	71	-5
4612	490	50	+6	4474	577	41	+6	4282	625	54	-12	5251	322	73	-8
4626	500	52	+3	4488	587	58	-12	4296	635	55	-14	5265	332	66	-1
4640	510	53	+1	4502	597	57	-12	4310	645	52	-12	5279	342	75	-10
4654	520	41	+12	4516	607	51	-8	4323	655	58	-20	5293	352	76	-12
4667	530	49	+3	4529	617	41	+2	4337	665	50	-13	5307	362	75	-11
4681	540	42	+9	4543	627	47	-5	4351	675	50	-14	5321	372	79	-16
4695	550	51	-1	4557	637	40	0	4365	685	41	-6	5335	381	69	-6
4709	560	42	+7	4571	647	37	+2	4379	695	42	-8	5348	391	69	-7
4723	570	44	+4	4585	657	47	-9	4393	705	29	+4	5362	401	83	-23
4737	580	42	+5	4599	667	36	+1	4407	715	27	+5	5376	411	65	-4
4750	590	41	+5	4612	677	36	0	4420	725	31	+1	5390	421	60	+1
4764	600	43	+2	4626	687	38	-3	4434	735	44	-13	5404	431	60	0
4778	610	45	-2	4640	697	36	-2	4448	744	30	+1	5418	441	60	-1
4792	620	38	+4	4654	706	33	0	4462	754	31	0	5432	451	78	-19
4806	630	36	+5	4668	716	33	-1	4476	764	44	-13	5445	461	73	-15
4820	640	36	+4	4682	726	27	+5	4490	774	48	-16	5459	471	63	-6
4834	650	35	+4	4696	736	33	-2	4504	784	42	-9	5473	481	62	-5
4847	659	33	+5	4709	746	37	-6	4517	794	33	+1	5487	491	55	+1
4861	669	33	+4	4723	756	34	-3	4531	804	37	-2	5501	501	72	-17
4875	679	32	+4	4737	766	30	+2	4545	814	49	-13	5515	511	58	-4
4889	689	34	+1	4751	776	36	-3	4559	824	25	+12	5529	521	62	-9
4903	699	30	+4	4765	786	35	-2	4573	834	48	-10	J. D. 2424703, plate no. 1185			
4917	709	28	+5	4779	796	26	+8	4587	844	39	+1	5006	9261	-71	-04
4931	719	31	+1	4793	806	41	-5	4601	854	46	-5	5019	271	67	0
4944	729	27	+4	4806	816	32	+5	4614	864	49	-7	5033	281	55	+12
4958	739	30	+1	4820	826	44	-6	4628	874	48	-5	5047	291	66	0
4972	749	25	+6	4834	836	38	+1	4642	884	41	+3	5061	301	63	+3
4986	759	33	-2	4848	846	47	-7	4656	894	52	-7	5075	311	65	+1
5000	769	29	+3	4862	856	35	+6	4670	904	63	-17	5089	321	68	-3
5014	779	33	0	4876	866	42	0	4684	914	58	-10	5103	331	70	-5
5027	789	28	+6	4890	876	43	0	4697	924	64	-15	5116	341	71	-6
5041	799	39	-4	4903	886	51	-7	4711	934	52	-2	5130	351	70	-6
5055	809	36	0	4917	896	43	+3	4725	944	54	-4	5144	360	68	-4
5069	819	30	+7	4931	906	53	-6	4739	954	56	-3	5158	370	67	-4
5083	829	39	-1	4945	915	50	-2	4753	963	62	-9	5172	380	61	+2
5097	839	42	-3	4959	925	58	-9	4767	973	52	+2	5186	390	65	-3
5111	849	41	-1	4973	935	51	-1	4781	983	57	-2	5199	400	60	+2
5124	859	39	+2	4986	945	58	-7	4794	993	60	-5	5213	410	61	0
5138	868	52	-10	5000	955	67	-15	4808	6003	54	+2	5227	420	56	+5
5152	878	42	+1	5014	965	62	-9	4822	013	60	-3	5241	430	61	-1
5166	888	45	0	5028	975	59	-5	4836	023	67	-9	5255	440	51	+8
5180	898	55	-9	5242	985	59	-4	4850	033	71	-13	5269	450	64	-5
5194	908	48	-1	5056	995	70	-14	4864	043	66	-7	5283	460	54	+4
5208	918	60	-12	5070	9005	53	+3	4878	053	62	-2	5296	470	59	-2
5221	928	53	-4	5083	015	74	-17	4891	063	67	-7	5310	480	52	+5
5235	938	50	0	5097	025	65	-7	4905	073	54	+7	5324	490	58	-2
5249	948	51	0	5111	035	76	-17	4919	083	68	-7	5338	500	54	+1
5263	958	50	+2	5125	045	60	-1	4933	093	55	+7	5352	510	51	+3
5277	968	53	0	5139	055	69	-9	4961	113	70	-7	5366	520	54	-1
5291	978	53	+1	5153	065	56	+4	4974	123	67	-4	5380	530	51	+1
5305	988	57	-2	5167	075	74	-13	5002	143	68	-4	5393	540	51	0
J. D. 2424696, plate no. 1182				5180	085	63	-1	5016	153	80	-15	5407	550	48	+2
4252	8418	-56	+05	5194	095	69	-7	5030	163	73	-8	5421	560	49	0
				5208	105	64	-1	5044	172	57	+9	5435	569	45	+3
				5222	115	66	-3					5449	579	41	+6
				5236	125	63	+1								

d	P	m _{pr}	Δ _{mpr}	d	P	m _{pr}	Δ _{mpr}	d	P	m _{pr}	Δ _{mpr}	d	P	m _{pr}	Δ _{mpr}
'5463	9'589	—40	+ 6	'4898	2'300	—64	+ 2	'3999	8'839	—43	— 4	'4249	6'205	—65	+ 2
'5476	'599	'45	0	'4912	'310	'66	0	'4013	'849	'34	+ 6	'4262	'215	'78	— 11
'5490	'609	'38	+ 5	'4926	'320	'63	+ 2	'4026	'859	'51	— 10	'4276	'225	'78	— 11
'5504	'619	'43	0	'4940	'330	'66	— 1	'4040	'869	'45	— 3	'4290	'235	'74	— 7
'5518	'629	'36	+ 5	'4954	'340	'69	— 4	'4054	'879	'46	— 3	'4304	'245	'75	— 8
'5532	'639	'42	— 2	'4968	'350	'62	+ 2	'4068	'889	'44	+ 1	'4318	'255	'69	— 2
'5546	'649	'32	+ 7	'4982	'360	'65	— 1	'4082	'899	'46	0	'4332	'265	'75	— 8
'5560	'659	'34	+ 4	'4995	'369	'71	— 8	'4096	'909	'49	— 2	'4346	'274	'83	— 16
J. D. 2424709, plate no. 1187				'5009	'379	'60	+ 3	'4110	'919	'57	— 9	'4359	'284	'73	— 6
'3901	1'583	—50	—03	'5023	'389	'67	— 5	'4123	'929	'46	+ 3	'4373	'294	'69	— 3
'3915	'593	'38	+ 8	'5037	'399	'73	— 11	'4137	'939	'53	— 3	'4387	'304	'77	— 11
'3929	'603	'48	— 4	'5051	'409	'63	— 2	'4151	'949	'63	— 12	'4401	'314	'70	— 4
'3943	'613	'34	+ 9	'5065	'419	'56	+ 5	'4165	'959	'53	— 1	'4415	'324	'66	— 1
'3957	'623	'43	— 1	'5078	'429	'60	0	'4179	'969	'57	— 4	'4429	'334	'66	— 1
'4095	'723	'24	+ 8	'5092	'439	'63	— 3	'4193	'979	'58	— 4	'4442	'344	'69	— 4
'4109	'732	'30	+ 1	'5106	'449	'64	— 5	'4220	'999	'64	— 8	'4456	'354	'74	— 10
'4123	'742	'28	+ 3	'5120	'459	'60	— 2	'5398	9'845	'40	0	'4470	'364	'75	— 11
'4137	'752	'23	+ 8	'5148	'479	'63	— 6	'5412	'855	'43	— 2	'4484	'374	'70	— 7
'4150	'762	'25	+ 7	'5162	'489	'59	— 3	'5425	'864	'40	+ 2	'4498	'384	'67	— 4
'4164	'772	'31	+ 1	'5175	'499	'56	— 1	'5439	'874	'48	— 5	'4512	'394	'79	— 17
'4178	'782	'29	+ 3	'5189	'509	'60	— 6	'5453	'884	'42	+ 2	'4526	'404	'75	— 13
'4192	'792	'33	+ 1	'5203	'519	'57	— 3	'5467	'894	'42	+ 3	'4539	'414	'72	— 11
'4206	'802	'33	+ 2	'5217	'529	'58	— 5	'5481	'904	'43	+ 3	'4553	'424	'58	+ 2
'4220	'812	'31	+ 5	'5231	'539	'53	— 1	'5495	'914	'50	— 2	'4567	'434	'62	— 2
'4234	'822	'33	+ 4	'5245	'549	'62	— 11	'5509	'924	'45	+ 4	'4581	'444	'59	0
'4247	'832	'42	— 4	'5259	'559	'55	— 6	'5522	'934	'47	+ 3	'4595	'454	'64	+ 5
'4261	'842	'34	+ 5	'5272	'569	'55	— 7	'5536	'944	'53	— 2	'4609	'464	'71	— 13
'4275	'852	'38	+ 2	'5286	'578	'47	0	'5550	'954	'56	— 4	'4623	'474	'68	— 11
'4289	'862	'44	— 2	'5300	'588	'53	— 7	'5564	'964	'55	— 2	'4636	'483	'58	— 1
'4303	'872	'38	+ 5	'5314	'598	'50	— 5	'5578	'974	'59	— 5	'4650	'493	'66	— 10
'4317	'882	'42	+ 1	'5328	'608	'49	— 6	'5592	'984	'53	+ 2	'4664	'503	'60	— 5
'4331	'892	'39	+ 6	'5342	'618	'43	0	'5605	'994	'50	+ 6	'4678	'513	'60	— 6
'4344	'902	'50	— 4	'5355	'628	'45	— 4	'5619	0'004	'63	— 7	'4692	'523	'55	— 2
'4358	'912	'51	— 4	'5369	'638	'43	— 3	'5633	'014	'58	— 1	'4706	'533	'55	— 3
'4372	'922	'49	0	'5383	'648	'44	— 5	'5647	'024	'57	+ 1	'4720	'543	'50	+ 1
'4386	'932	'48	+ 2	'5397	'658	'37	+ 1	'5661	'034	'63	— 5	'4733	'553	'47	+ 3
'4400	'941	'46	+ 5	'5411	'668	'42	— 5	J. D. 2424710, plate no. 1190				'4747	'563	'56	— 7
'4414	'951	'49	+ 3	'5425	'678	'42	— 6	'5799	0'133	—52	+ 12	'4761	'573	'55	— 7
'4427	'961	'52	+ 1	'5439	'688	'35	0	'5813	'143	'64	0	'4775	'583	'55	— 8
'4441	'971	'53	+ 1	'5452	'698	'34	0	'5827	'153	'60	+ 5	'4789	'593	'57	— 11
'4455	'981	'53	+ 1	'5466	'708	'35	— 2	'5841	'163	'56	+ 9	'4803	'603	'41	— 3
'4469	'991	'52	+ 3	'5480	'718	'39	— 7	'5855	'173	'60	+ 6	'4816	'613	'43	0
'4483	2'001	'57	— 1	'5494	'728	'30	+ 2	'5869	'183	'54	+ 12	'4830	'623	'39	+ 3
'4497	'011	'58	— 1	'5508	'738	'37	— 6	'5882	'193	'59	+ 7	'4844	'633	'34	+ 7
'4511	'021	'52	+ 6	'5522	'748	'45	— 14	J. D. 2424711, plate no. 1191				'4858	'643	'47	— 7
'4524	'031	'58	0	'5536	'758	'36	— 5	'3916	5'966	—57	—04	'4872	'653	'47	— 8
'4538	'041	'60	— 1	'5549	'768	'35	— 3	'3930	'976	'47	+ 7	'4886	'663	'40	— 2
'4552	'051	'66	— 6	'5563	'778	'27	+ 6	'3944	'986	'56	— 1	'4913	'683	'33	+ 3
'4566	'061	'51	+ 9	'5577	'788	'40	— 6	'3958	'996	'49	+ 7	'4927	'693	'50	— 16
'4580	'071	'63	— 2	'5591	'797	'39	— 4	'3972	6'006	'56	0	'4941	'702	'45	— 12
'4594	'081	'59	+ 2	'5605	'807	'33	+ 3	'3985	'016	'63	— 6	'4955	'712	'50	— 17
'4608	'091	'66	— 4	'5619	'817	'39	— 2	'3999	'026	'61	— 3	'4983	'732	'45	— 14
'4621	'101	'67	— 5	'5633	'827	'43	— 5	'4013	'036	'54	+ 5	'4997	'742	'31	0
'4635	'111	'64	— 1	'5646	'837	'35	+ 4	'4027	'046	'62	— 3	'5010	'752	'42	— 11
'4649	'121	'64	— 1	'5660	'847	'44	— 4	'4041	'055	'57	+ 3	'5024	'762	'40	— 8
'4663	'131	'56	+ 8	'5674	'857	'33	+ 8	'4055	'065	'60	0	'5038	'772	'39	— 7
'4677	'141	'59	+ 5	'5688	'867	'36	+ 6	'4069	'075	'58	+ 3	'5052	'782	'34	— 1
'4691	'151	'71	— 6	'5702	'877	'39	+ 4	'4082	'085	'71	— 9	'5066	'792	'43	— 9
'4704	'160	'68	— 3	J. D. 2424709, plate no. 1188				'4096	'095	'67	+ 5	'5080	'802	'43	— 8
'4718	'170	'67	— 2	'5840	2'977	—56	—02	'4110	'105	'62	+ 1	'5093	'812	'40	— 4
'4732	'180	'70	— 4	'5854	'987	'51	+ 4	'4124	'115	'65	— 2	'5107	'822	'37	0
'4746	'190	'68	— 2	'5868	'997	'52	+ 4	'4138	'125	'68	— 4	'5121	'832	'50	— 12
'4760	'200	'71	— 5	'5882	3'006	'56	0	'4152	'135	'65	— 1	'5135	'842	'41	— 2
'4774	'210	'72	— 5	'5896	'016	'54	+ 3	'4165	'145	'75	— 11	'5149	'852	'50	— 10
'4788	'220	'66	+ 1	J. D. 2424710, plate no. 1189				'4179	'155	'71	— 6	'5163	'862	'45	— 3
'4801	'230	'64	+ 3	'3943	8'799	—33	+02	'4193	'165	'62	+ 3	'5177	'872	'50	— 7
'4815	'240	'65	+ 2	'3957	'809	'46	— 10	'4207	'175	'70	— 4	'5190	'882	'47	— 4
'4829	'250	'80	— 13	'3971	'819	'33	+ 4	'4221	'185	'71	— 5	'5204	'892	'47	— 3
'4843	'260	'68	— 1	'3985	'829	'42	— 4	'4235	'195	'70	— 4	'5218	'902	'52	— 6
'4871	'280	'67	0									'5232	'911	'49	— 2
'4885	'290	'68	— 2									'5246	'921	'53	— 5
												'5260	'931	'66	— 16
												'5274	'941	'62	— 11

d	P	m _{pr}	Δm _{pr}	d	P	m _{pr}	Δm _{pr}	d	P	m _{pr}	Δm _{pr}	d	P	m _{pr}	Δm _{pr}
4749	7119	-61	+ 2	5815	7886	-40	+ 4	4112	3848	-30	+ 10	7124	6723	-31	+ 1
4762	129	60	+ 4	5829	896	42	+ 4	4126	858	37	+ 4	7138	733	34	- 3
4776	139	63	+ 1	5843	906	39	+ 8	4140	868	41	+ 1	7152	743	26	+ 5
4790	149	64	+ 1	5857	915	38	+ 10	4154	878	34	+ 9	7166	753	32	- 1
4804	159	64	+ 1	5871	925	34	+ 15	4168	888	50	- 5	7180	763	28	+ 4
4818	169	62	+ 3	5884	935	47	+ 3	4181	898	50	- 4	7194	773	31	+ 1
4832	179	59	+ 7	5898	945	45	+ 6	4195	908	38	+ 9	7208	783	29	+ 4
4846	189	61	+ 5	5912	955	46	+ 6	4209	917	48	0	7221	793	34	0
4859	199	55	+ 11	5926	965	44	+ 9	4223	927	46	+ 3	7235	803	33	+ 2
4873	209	59	+ 8	5940	975	47	+ 7	4237	937	44	+ 6	7249	813	36	0
4887	219	68	- 1	5954	985	54	+ 1	4251	947	46	+ 5	7263	823	31	+ 6
4901	229	59	+ 8	5968	995	48	+ 8	4292	677	56	- 2	7277	833	33	+ 5
4915	239	57	+ 10	5981	8005	45	+ 11	4306	987	61	- 6	7291	843	37	+ 2
4929	249	58	+ 9	5995	015	45	+ 12	4320	997	62	- 6	7304	853	36	+ 5
4943	259	59	+ 8	6009	025	56	+ 2	4334	4007	54	+ 3	7318	863	34	+ 8
4956	269	69	- 2	6023	035	52	+ 7	4348	017	72	- 15	7332	873	39	+ 4
4970	278	59	+ 8	6037	045	52	+ 7	4361	027	53	+ 5	7346	883	41	+ 2
4984	288	58	+ 8	6051	055	52	+ 8	4375	037	53	+ 6	7360	893	40	+ 4
4998	298	60	+ 6	6064	065	52	+ 8	4389	047	64	- 5	7374	903	44	+ 2
5012	308	60	+ 6	6092	085	53	+ 9	4403	057	68	- 8	7388	913	39	+ 9
5026	318	60	+ 6	6106	095	56	+ 6	4417	067	53	+ 8	7401	923	44	+ 5
5040	328	65	0	6120	105	55	+ 8	4431	077	55	+ 6	7415	932	42	+ 8
5053	338	55	+ 10	J. D. 2424758, plate no. 1198				4445	087	67	- 5	7429	942	49	+ 2
5067	348	66	- 2	3433	3360	-61	+ 03	4458	097	63	- 1	7443	952	49	+ 3
5081	358	58	+ 6	3447	370	63	0	4472	107	64	- 1	7457	962	49	+ 4
5095	368	61	+ 2	3461	380	60	+ 3	4486	117	64	- 1	7471	972	47	+ 7
5109	378	54	+ 9	3475	390	61	+ 1	4500	127	61	+ 3	7485	982	53	+ 2
5123	388	63	- 1	3489	400	60	+ 2	4514	136	63	+ 1	7498	992	48	+ 7
5136	398	61	+ 1	3503	410	61	0	4528	146	67	- 2	7512	7002	53	+ 3
5150	408	54	+ 7	3517	420	61	0	4542	156	67	- 2	7526	012	51	+ 6
5164	418	54	+ 7	3530	430	61	- 1	4555	166	62	+ 3	7540	022	53	+ 5
5178	428	59	+ 1	3544	440	55	+ 4	4569	176	69	- 3	J. D. 2424955, plate no. 1225			
5192	438	54	+ 6	3558	450	60	- 1	4583	186	63	+ 3	5622	0571	-42	+ 06
5206	448	55	+ 4	3572	460	56	+ 2	4597	196	68	- 2	5636	581	44	+ 3
5220	458	58	0	3586	470	58	- 1	4625	216	72	- 5	5649	591	43	+ 3
5233	468	55	+ 3	3600	480	55	+ 2	4638	226	63	+ 4	5663	600	42	+ 3
5247	478	52	+ 5	3614	489	51	+ 5	4652	236	84	- 17	5677	610	44	- 1
5261	487	40	+ 16	3627	499	56	- 1	4666	246	68	+ 3	5691	620	38	+ 4
5275	497	49	+ 6	3641	509	55	- 1	4680	256	68	- 1	5705	630	37	+ 4
5289	507	53	+ 2	3655	519	52	+ 2	4694	266	66	+ 1	5719	640	38	+ 2
5303	517	49	+ 5	3669	529	45	+ 8	4708	276	72	- 5	5732	650	36	+ 3
5317	527	41	+ 12	3683	539	55	- 3	J. D. 2424894, plate no. 1211				5746	660	41	- 3
5330	537	51	+ 1	3697	549	44	+ 7	3158	0455	-61	- 02	5760	670	38	- 1
5344	547	41	+ 10	3710	559	42	+ 7	3172	465	57	+ 1	5774	680	34	+ 2
5358	557	41	+ 9	3724	569	38	+ 10	3186	475	57	0	5788	690	32	+ 3
5372	567	44	+ 5	3738	579	49	- 2	3199	485	52	+ 4	5802	700	36	- 2
5386	577	41	+ 6	3752	589	42	+ 4	3213	495	50	+ 6	5816	710	34	- 1
5400	587	41	+ 5	3766	599	40	+ 5	3227	505	56	- 1	5829	720	32	0
5413	597	41	+ 4	3780	609	41	+ 2	3241	515	50	+ 4	5843	730	30	+ 1
5427	607	32	+ 11	3794	619	47	- 4	3255	525	49	+ 4	5857	740	31	0
5441	617	35	+ 8	3821	639	34	+ 6	J. D. 2424907, plate no. 1211				5871	750	36	- 5
5455	627	30	+ 12	3835	649	47	- 8	6875	6544	-51	0	5885	760	30	+ 1
J. D. 2424757, plate no. 1197				3849	659	35	+ 3	6889	554	45	+ 5	5899	770	32	0
5566	7706	-25	+ 08	3863	669	31	+ 6	6903	564	44	+ 5	5913	780	32	+ 1
5580	716	22	+ 10	3877	679	35	+ 1	6917	574	45	+ 3	5926	790	25	+ 9
5594	726	26	+ 6	3891	689	24	+ 11	6931	584	43	+ 4	5940	800	33	+ 2
5607	736	22	+ 9	3904	699	28	+ 6	6944	594	40	+ 5	5954	809	34	+ 2
5621	746	26	+ 5	3918	708	26	+ 7	6958	604	39	+ 5	5968	819	36	+ 1
5635	756	24	+ 7	3932	718	29	+ 3	6972	614	38	+ 5	5982	829	34	+ 4
5649	766	26	+ 6	3946	728	29	+ 2	6986	624	30	+ 12	5996	839	41	- 2
5663	776	29	+ 4	3960	738	27	+ 4	7000	634	36	+ 5	6009	849	38	+ 2
5677	786	32	+ 1	3974	748	28	+ 3	7014	644	38	+ 2	6023	859	47	- 6
5690	796	32	+ 2	3987	758	24	+ 7	7027	654	37	+ 2	6037	869	43	- 1
5704	806	23	+ 13	4001	768	21	+ 11	7041	664	35	+ 3	6051	879	46	- 3
5718	816	33	+ 4	4015	778	25	+ 8	7055	674	30	+ 6	6065	889	47	- 2
5732	826	30	+ 8	4029	788	28	+ 6	7069	684	33	+ 2	6079	899	50	- 4
5746	836	37	+ 2	4043	798	29	+ 6	7083	694	34	0	6093	909	47	0
5760	846	38	+ 2	4057	808	40	- 4	7097	704	32	+ 1	6106	919	51	- 3
5774	856	34	+ 7	4071	818	31	+ 6	7111	714	31	+ 2	6120	929	48	+ 1
5787	866	38	+ 4	4084	828	29	+ 9					6134	939	50	0
5801	876	30	+ 13	4098	838	40	- 1					6148	949	45	+ 6

TABLE 5.

means of every 10 observations		means of every 50 or 60 observations		means of every 10 observations		means of every 50 or 60 observations		means of every 10 observations		means of every 50 or 60 observations		means of every 10 observations		means of every 50 or 60 observations			
P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}
.0147	— .585			.2585	— .678	.2620	— .672	.5715	— .477			.8109	— .381				
.0216	.592			.2658	.672			.5799	.450			.8176	.365				
.0275	.551	.0279	— .589	.2741	.695			.5872	.476			.8236	.376				
.0342	.610			.2819	.665			.5933	.476	.5935	— .460	.8299	.401				
.0413	.606			.2909	.661			.6002	.433			.8365	.399	.8359	— .391		
.0483	.605			.2995	.654			.6067	.466			.8419	.388				
.0557	.593			.3086	.682	.3137	— .666	.6125	.424			.8477	.391				
.0630	.600	.0630	— .603	.3177	.659			.6196	.421			.8531	.408				
.0703	.596			.3272	.655			.6261	.407	.6262	— .410	.8591	.407				
.0778	.623			.3383	.684			.6327	.397			.8654	.410	.8652	— .415		
.0851	.619			.3492	.653			.6401	.401			.8714	.438				
.0923	.611			.3589	.640			.6477	.396			.8771	.414				
.0994	.628	.0997	— .623	.3683	.659	.3682	— .643	.6543	.412			.8842	.427				
.1072	.612			.3779	.632			.6611	.361	.6619	— .380	.8909	.445				
.1145	.643			.3868	.633			.6689	.374			.8973	.473	.8975	— .457		
.1222	.637			.3950	.645			.6775	.357			.9042	.475				
.1301	.601			.4032	.628			.6851	.349			.9108	.465				
.1372	.613	.1366	— .630	.4116	.600	.4118	— .609	.6923	.369			.9172	.495				
.1433	.643			.4201	.583			.7002	.325			.9245	.489				
.1500	.657			.4289	.589			.7075	.310	.6999	— .338	.9318	.500	.9316	— .498		
.1563	.662			.4379	.570			.7144	.338			.9387	.497				
.1633	.656			.4469	.579			.7214	.308			.9458	.508				
.1704	.647	.1743	— .646	.4563	.622	.4563	— .591	.7286	.290			.9523	.535				
.1769	.626			.4654	.598			.7353	.322	.7353	— .312	.9597	.559				
.1834	.637			.4752	.585			.7420	.315			.9662	.531	.9659	— .541		
.1904	.650			.4839	.527			.7494	.324			.9728	.529				
.1976	.667			.4932	.564			.7566	.314			.9787	.552				
.2050	.649			.5032	.578	.5032	— .547	.7636	.301			.9846	.551				
.2123	.681	.2159	— .668	.5132	.543			.7707	.320	.7708	— .316	.9910	.532				
.2197	.672			.5227	.521			.7780	.314			.9965	.548	.9967	— .546		
.2269	.657			.5333	.514			.7852	.332			1'0027	.559				
.2338	.680			.5444	.508			.7920	.341			1'0086	.541				
.2417	.662			.5539	.482	.5533	— .492	.7989	.342								
.2500	.659			.5635	.480			.8051	.353	.8049	— .356						

TABLE 7.

means of 10 observations		means of 100 or 120 observations		means of 10 observations		means of 100 or 120 observations		means of 10 observations		means of 100 or 120 observations		means of 10 observations		means of 100 or 120 observations			
phase counted from minimum		phase counted from minimum		phase counted from minimum		phase counted from minimum		phase counted from minimum		phase counted from minimum		phase counted from minimum		phase counted from minimum			
P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}	P	m _{pr}
— .0026	— .315			— .0595	— .349			— .1119	— .397			— .1647	— .450				
+ .0048	.324			+ .0605	.353			+ .1145	.407			+ .1662	.465				
— .0093	.322			+ .0663	.381			— .1185	.407			+ .1726	.495				
+ .0120	.314			— .0671	.357			+ .1208	.410	.1195	— .413	— .1731	.477				
— .0160	.290			+ .0730	.365			— .1250	.421			+ .1799	.489				
+ .0190	.301	.0177	— .315	— .0757	.374			+ .1268	.438			— .1811	.480				
— .0232	.308			+ .0790	.376			— .1321	.424			+ .1872	.500	.1888	— .497		
+ .0261	.320			— .0835	.361			+ .1325	.414			— .1907	.482				
— .0302	.338			+ .0853	.401	.0876	— .386	— .1379	.466			+ .1941	.497				
+ .0334	.314			— .0903	.412			+ .1396	.427			— .2002	.508				
— .0371	.310			+ .0919	.399			— .1444	.433			+ .2012	.508				
+ .0406	.332			— .0969	.396			+ .1463	.445			+ .2077	.535				
— .0444	.325			+ .0973	.388			— .1513	.476			— .2113	.514				
+ .0474	.341			+ .1031	.391			+ .1527	.473	.1520	— .459	+ .2151	.559				
— .0523	.369	.0530	— .346	— .1045	.401			— .1574	.476			+ .2216	.531				
+ .0543	.342			+ .1085	.408			+ .1596	.475			— .2219	.521				